# A multi-instrument approach to determining the source-region extent of EEP-driving EMIC waves

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12 Key Points:

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13	•	The extent of an EEP-driving EMIC source region is estimated using conjunctions
14		between in-situ and ground-based observations
15	•	A single EMIC wave event is observed simultaneously by the conjugate RBSP-B
16		and Arase spacecraft, and ground-based instruments
17	•	Conjugate measurements by the AARDDVARK network are used to track the EEP
18		from the event and estimate the extent and drift rate

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#### 19 Abstract

Recent years have seen debate regarding the ability of electromagnetic ion cyclotron (EMIC) 20 waves to drive EEP (Energetic Electron Precipitation) into the Earth's atmosphere. Ques-21 tions still remain regarding the energies and rates at which these waves are able to in-22 teract with electrons. Many studies have attempted to characterise these interactions 23 using simulations, however these are limited by a lack of precise information regarding 24 the spatial scale size of EMIC activity regions. In this study we examine a fortuitous si-25 multaneous observation of EMIC wave activity by the RBSP-B and Arase satellites in 26 conjunction with ground-based observations of energetic electron precipitation by a sub-27 ionospheric VLF network. We describe a simple method for determining the longitudi-28 nal extent of the EMIC source region based on these observations, calculating a width 29 of 0.75 hr MLT and a drift-rate of 0.67 MLT/hr. We describe how this may be applied 30 to other similar EMIC wave events. 31

# 32 Plain Language Summary

The Earth is surrounded by the Van Allen radiation belts, rings of high-energy charged 33 particles trapped by the Earth's magnetic field. These particle populations are constantly 34 changing, driven by forces from the Sun, Earth, and from the belts themselves. One of 35 the most important drivers of this dynamism is the interaction between particles and elec-36 tromagnetic waves. One such wave species, known as Electromagnetic Ion Cyclotron (EMIC) 37 waves, has come under scrutiny recently due to experimental results calling into ques-38 tion the theoretical energy limits of their interactions with radiation belt electrons. Study-39 ing these waves and their interactions is hampered by our inability to accurately deter-40 mine the size of the source region of these waves. In this study, we investigate a single 41 EMIC wave event observed simultaneously by two separate satellites and use a network 42 of ground-based radio wave receivers to estimate the size of the EMIC region. We also 43 explain how the method used in this study may be generalised to other EMIC wave events. 44 This method will allow us to carry out statistical analysis of the size of EMIC wave re-45 gions in general, aiding future research into the impacts of these waves on the radiation 46 belts. 47

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# 48 1 Introduction

Electromagnetic ion cyclotron (EMIC) waves, Pc1-2 (0.1–5 Hz) pulsations in the Earth's magnetosphere, have long been known as drivers of relativistic electron scattering and loss within the Earth's radiation belts (e.g. Thorne & Kennel, 1971). Despite decades of study, however, many basic elements of the interactions between EMIC waves and radiation belt electrons remain unknown. Key among these are the precise details of the process driving the electron scattering and the energy range across which this scattering can occur.

For many years, quasi-linear diffusion theory was the preferred approach to study-56 ing EMIC-driven electron precipitation. Under this theory, electron scattering is expected 57 to be restricted to energies above roughly 1 - 2 MeV, only reaching lower energies in 58 extraordinary cases (Meredith et al., 2003). However, in recent years a growing number 59 of experimental studies have shown evidence of EMIC waves driving energetic electron 60 precipitation (EEP) at energies below 500 keV (e.g. Millan et al., 2007; Woodger et al., 61 2015; Clilverd et al., 2015; Rodger et al., 2015), with one study even suggesting that this 62 lower-energy EEP may be the dominant form of EMIC-driven electron precipitation (Hendry 63 et al., 2017). These results are largely incompatible with quasilinear theory, and other 64 possible explanations have been suggested, including non-linear theory (e.g. Omura & 65 Zhao, 2012, 2013), non-resonant theory (e.g. Chen et al., 2016), and resonant scatter-66 ing by low-amplitude waves (Denton et al., 2019), although none has emerged as the dom-67 inant theory to date. 68

This uncertainty regarding the fundamental characteristics of EMIC waves is in part simply due to a lack of observations. It was not until fairly recently that EMIC waves were able to be conclusively linked to electron precipitation (Miyoshi et al., 2008; Rodger et al., 2008), and even now we are limited to a handful of satellites for in-situ study of these waves. Such limited and sporadic coverage makes it difficult at times to properly characterise the waves associated with a given precipitation event. The use of groundbased instrumentation has proved useful for filling some of these gaps in coverage.

There have been a number of investigations into the size of EMIC source regions (e.g. Engebretson et al., 2008; Lee et al., 2013; Mann et al., 2014; Engebretson et al., 2015; Blum et al., 2017). However, these studies have tended to focus on either the *L*shell extent of the wave regions, which is typically much easier to determine, or have pro-

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vided only very rough estimates of the longitudinal extent. Part of the reason for this 80 is because it is generally not feasible to determine the longitudinal extent of an EMIC 81 source region from in-situ measurements alone. The combination of moving observation 82 platforms and a low density of satellites means that, generally speaking, the size sim-83 ply cannot be accurately calculated. Ground-based EMIC wave measurements do not 84 fare much better – ionospheric ducting makes it all but impossible to determine precisely 85 the source location of EMIC observations from ground-based wave observations alone 86 (Kim et al., 2010). This in turn makes it very difficult to determine how large the source 87 region is. Without precise knowledge of typical source-region extents, simulations and 88 studies of EMIC waves have to essentially guess how large the source region is, or sim-89 ply ignore this aspect entirely. This can lead to significant uncertainties regarding the 90 effect of EMIC waves on radiation belt particle populations as a whole – larger source 91 regions allow not only more of the radiation belts to interact with the waves in question, 92 but also for longer interaction times. 93

In this paper, we discuss a technique using sub-ionospheric VLF wave observations for determining the longitudinal extent of a subset of EMIC waves, namely those that are able to scatter energetic electrons into the loss cone. While this limitation excludes a significant proportion of the total EMIC wave population, it has the potential to provide much needed data on the wave characteristics of these EEP-driving waves.

# 99 **2** Instrumentation

In this study we utilize in-situ magnetic field observations from two sources: the 100 **RBSP** Electric and Magnetic Field Instrument Suite and Integrated Science (EMFISIS) 101 triaxial fluxgate magnetometer (MAG) (Kletzing et al., 2013) and the Arase Magnetic 102 Field Experiment (MGF), which is also a triaxial fluxgate magnetometer (Matsuoka et 103 al., 2018). These instruments sample at 64 Hz and 256 Hz respectively, making them ideal 104 for investigating EMIC activity. We complement these observations with data from the 105 100 Hz ground-based search-coil magnetometer (SCM) located in Eskdalemuir, Scotland 106  $(55.3^{\circ} \text{ N}, -3.2^{\circ} \text{ E}, L = \sim 2.8)$ , run by the British Geological Survey (Beggan & Musur, 107 2018). The ESK magnetometer consists of two coils, one arranged north-south, the other 108 east-west. 109

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For ground-based observation of electron fluxes, we use data from the Antarctic-110 Arctic Radiation-belt Dynamic Deposition VLF Atmospheric Research Konsortia (AARD-111 DVARK) network. AARDDVARK is a global network of very low frequency (VLF) ra-112 dio receivers, used to monitor the height of the ionospheric D-region through the mon-113 itoring of powerful man-made VLF radio signals. VLF waves may propagate for very long 114 distances through the Earth-Ionosphere waveguide. Changes in the height of the D-region, 115 for instance due to energetic electron precipitation into the ionosphere, change the prop-116 erties of this waveguide, resulting in changes in the characteristics (i.e., phase and am-117 plitude) of the received wave. By monitoring and investigating these changes, it is pos-118 sible to derive information about electron precipitation into the ionosphere. More infor-119 mation on the AARDDVARK network and the remote sensing of the ionosphere can be 120 found in Clilverd et al. (2009), and the sources within. 121

#### <sup>122</sup> 3 Event description

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# 3.1 Wave observations: in-situ

As shown in Figure 1(a), on 25 August 2018 from 20:46–21:05 UT, the RBSP-B 124 EMFISIS MAG instrument observed a burst of EMIC wave activity between roughly 0.4– 125 1.2 Hz, in the helium wave band ( $\Omega_{\rm He^+} < \omega < \Omega_{\rm H^+}$ ). This activity consisted of two 126 distinct wave bursts from 20:46–20:49 UT and 20:50–21:05 UT, with the peak wave am-127 plitudes of 5.5 nT and 12.7 nT respectively. A lower-amplitude burst of wave power was 128 also observed in the hydrogen band ( $\Omega_{O^+} < \omega < \Omega_{He^+}$ ) from roughly 1.2–1.6 Hz at 129 around 21:04 UT, however this was comparatively much weaker than the helium band 130 wave, peaking at roughly 1.8 nT. We see evidence of rising-tone subpacket structures (some-131 times called *fine-structure elements*, e.g. Matsuda et al. (2018)), particularly during the 132 second wave burst. Over the duration of this wave observation, the RBSP-B satellite tra-133 versed roughly L=3.9-4.3, calculated using the 2002 Tsyganenko (T02) model (Tsyganenko, 134 2002a, 2002b) magnetic field model, at 20.7–21.2 MLT. RBSP-B was located close to the 135 magnetic equator at this time, at a magnetic latitude of roughly -7.2°. 136

Figure 1(a) presents the wavelet spectrogram of the RBSP-B wave power perpendicular to the background field, calculated during the event period using the generalised Morse wavelet (Olhede & Walden, 2002) with symmetry parameter  $\gamma = 3$ . The equatorial helium and oxygen gyrofrequencies,  $\Omega_{He^+}$  and  $\Omega_{O^+}$  respectively, are over-plotted



Figure 1. (a) Wavelet spectrogram of the RBSP-B perpendicular wave power (field-aligned 137 coordinates), with the helium and oxygen gyrofrequencies plotted in white. (b) as in (a), but for 138 the data from the Arase MGF instrument. (c) Map of the event region with the RBSP-B and 139 Arase T02 footprints in red and blue respectively (with arrows indicating the direction of travel 140 and white diamonds indicating the point of closest approach), the 3 AARDDVARK VLF paths 141 in red, and the Eskdalemuir SCM (red square). T02 L-shells from 3-6 are shown as dashed black 142 lines. (d) and (e): as in (a) and (b) but plotted against MLT and normalised by the equatorial 143 helium gyrofrequency. 144

in white. The T02 footprint of the RBSP-B satellite during this period of wave observation, taken as the geographic coordinates of the magnetic field line traced down from
the satellite to an altitude of 100 km, is shown in red in Figure 1(c).

During this same time period, the Arase satellite was roughly in conjunction with 152 RBSP-B. From roughly 20:49–20:59 UT, the Arase magnetometer observed strong wave 153 power in the helium wave band. Like the RBSP-B observations, Arase saw two distinct 154 wave bursts from 20:49–20:51 UT and 20:51–20:59 UT, peaking at 6.3 nT and 9.3 nT 155 respectively. During this wave observation, Arase traversed roughly L=3.6-4.3 (T02) and 156 20.75–21.2 MLT. Arase was located much further down the field-line than RBSP-B at 157 a magnetic latitude of roughly  $-30^{\circ}$ , likely outside the EMIC source region. The wavelet 158 spectrogram of the Arase perpendicular wave power is presented in the same format as 159 the RBSP-B data in Figure 1(b). The T02 footprint of the Arase satellite during this 160 period of wave observation is shown in blue in Figure 1(c). 161

RBSP-B and Arase were not in perfect conjunction during this wave event, as is 162 evident from examination of the footprint traces presented in Figure 1(c) – at every point 163 during the wave event, the satellites were separated in either L-shell or MLT. At clos-164 est approach, the satellites were separated by  $\sim 800$  km when traced to the magnetic 165 equator (using the T02 field model). Thus, a direct comparison between the wave ob-166 servations is not necessarily the best approach to investigating the wave data. Figures 1(d) 167 and (e) show the same data as Figures 1(a) and (b), plotted against MLT instead of UT 168 and with the frequency normalised by the equatorial helium gyrofrequency for each satel-169 lite. When viewed in this fashion, it is clear that these observations are of the same wave 170 event, with very strong similarities in the MLT locations of the wave observations. 171

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#### 3.2 Wave observations: ground-based

Evidence of EMIC wave activity was observed in the ESK SCM (Figure 1(c), red 173 square) at the same time as the satellite observations, shown in Figure 2(a). This mag-174 netometer is located roughly 5° southward and 5° eastward of the satellite footprint re-175 gion – i.e., roughly the same MLT, and well within the limits of EMIC ducting (Kim et 176 al., 2010). The wave seen in the ESK magnetometer was a clear IPDP-type (intervals 177 of pulsations with diminishing periods) wave, with the average frequency of the wave grad-178 ually increasing over the observation period. We also see evidence of more rapid inter-179 nal rising tone subpacket structure. The wave activity on the ground lasts longer than 180 the satellite observations, occurring for roughly 40 minutes from 20:35 UT until 21:15 181 UT, suggesting again that the satellites were passing through an existing wave source-182 region, rather than observing the initial growth of the wave. In Figure 2(a) we have in-183

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dicated the approximate temporal extent of the wave with vertical solid white lines, estimated as the times where the instantaneous sum of the wavepower in the helium band returned to the background level.

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#### 3.3 EEP observations: ground-based

There is growing experimental evidence to suggest that strong EMIC waves, particularly those with rising-tone subpacket structures, are capable of driving significant electron scattering into the loss-cone, potentially through nonlinear interactions (e.g. Omura & Zhao, 2013; Kubota & Omura, 2017; Hendry et al., 2019). Thus we expect that this wave event, which is both strong and features rising-tone subpacket structures, should drive electron precipitation into the upper atmosphere.

To get an idea of the electron precipitation being driven by this event, we can look 194 at this event using ground-based instrumentation. The footprint region of this wave event 195 is crossed by 10-15 AARDDVARK VLF paths, depending on the signals being observed 196 at a given station. For this case study, a number of these were unusable due to poor sig-197 nal strength or lack of phase-lock. There is also overlap between some of the paths, pro-198 viding essentially redundant data. We focus on the measurements from two AARDDVARK 199 receivers located in Reykjavik, Iceland (REY) and Ny-Ålesund, Norway (NYA). For each 200 of these receivers, we examine the signal from the British VLF transmitter located in 201 Anthorn, UK (GQD). We also examine the signal from another British VLF transmit-202 ter in Skelton, UK (GVT) using data from the Ny-Ålesund, Norway (NYA) receiver. These 203 paths are shown in Figures 1(c); due to the scale of the map, the transmitter and receiver 204 locations are not shown. 205

To examine the AARDDVARK data properly, we must estimate the quiet-day curve 212 (QDC), that is, the form the signal would take in the absence of any atypical modifica-213 tion of the waveguide. For each of the paths studied, we construct an approximate QDC 214 phase curve through a combination of detrending and analysis of quiet days prior to the 215 event day. This QDC is then subtracted from the AARDDVARK signal, leaving only 216 the changes to the signal caused by the EEP-driven ionisation of the D-region. For this 217 study, we focus on the phase of the signal. The results of this are shown in Figures 2(b), 218 (c), and (d). The solid red lines indicate the period of wave activity, as determined by 219 the ESK magnetometer. 220

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Figure 2. (a) Wavelet spectrogram of the ESK North-South component with the approximate temporal limits of the wave shown in white. (b) The difference between the phase of the GQD-NYA VLF signal at the event time and the QDC. (c) as in (b) for the GVT-NYA path. (d) as in (b) for the GQD-REY path. For panels (b)-(d), the dashed red lines indicate the zero point (i.e., the QDC), and the solid red lines indicate the temporal limits of the EMIC wave as seen at Eskdalemuir.

The timing of this event is such that the terminator crosses each of the VLF paths during the event period. VLF phase and amplitude propagation is significantly complicated by the presence of the terminator, which can make detailed analysis of the VLF signal difficult. Fortunately, for our purposes, we take a less quantitative approach to this analysis, so precise knowledge of the phase and amplitude changes are not necessary.

In Figures 2(b), (c), and (d), it is clear that there is EEP occurring along each of the paths, with significant changes in the measured phase of the signal in each case. We note that there are significant differences in the timing and duration of these phase changes; in the next section, we will investigate these changes in more detail, using the different

locations of the paths to estimate the longitudinal extent of the EMIC source region.

# <sup>232</sup> 4 Source-region analysis

From a combination of our in-situ and ground-based observations, we are able to investigate the size and westward drift rate of the EMIC source region for this event. Firstly, we investigate what the wave observations tell us about the source region.

From our ground-based EMIC wave observations, we know that this EMIC wave 236 event began at roughly 20:35 UT, lasting for 40 minutes until 21:15 UT. Both the RBSP-237 B and Arase observations, from 20:46–21:05 UT and 20:49–20:59 UT respectively, oc-238 cur entirely within this time period, meaning that the limits of these in-situ wave ob-239 servations must represent spatial limits to the region occupied by the wave, rather than 240 temporal limits. In other words, the onset and disappearance of wave activity in the satel-241 lites is due to the satellites entering the source region, rather than the source region form-242 ing and decaying around the satellites. 243

Based on the analysis of the satellite traces in Figure 1(c), it is clear that the if the 244 onset of wave activity on the satellites cannot be explained by temporal changes in the 245 source region, then it must be due to the satellites passing through the western-most edge 246 of the wave region; thus, by examining the satellite locations at these times we can de-247 termine the MLT (or longitude) location of the western edge of the slowly westward-drifting 248 source region. By similar reasoning, it is clear that the disappearance of wave activity 249 on the satellites is due to them reaching the upper L-shell extent of the EEP and EMIC 250 source region. 251

The solid red and blue lines in Figure 1(c) trace T02 footprint RBSP-B and Arase 252 satellites for the periods when each sees EMIC wave activity, i.e., 20:45–21:04 UT for RBSP-253 B and 20:49–20:59 UT for Arase. From the endpoints of the interval, we can define a rough 254 upper limit on the L-shell extent of the event region at L = 4.3. From the limits of the 255 Arase observations, we know that the wave region must extend down to at least L =256 3.6, however we cannot rule out the possibility of the wave region extending lower. Other 257 studies have used observations from the Polar-orbiting Operational Environmental Satel-258 lites (POES) constellation to estimate the L-shell extent of EMIC waves (e.g. Engebret-259

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son et al., 2015), however due to extensive proton contamination of the POES electron
data, this is not possible for this case.

Using the RBSP-B and Arase data, we can also estimate the drift rate of the source 262 region relative to the Earth, from the slight differences in the satellite footprint locations 263 at the onset of wave activity in each. The RBSP-B satellite first detected wave activ-264 ity at 20:45:41, at which point the (T02) footprint of the satellite was located at a lon-265 gitude of -11.69°E (21.14 MLT). The Arase satellite detected wave activity slightly later 266 in time, starting at 20:49:23, at which point the (T02) footprint was located at a lon-267 gitude of  $-12.15^{\circ}$ E (21.14 MLT). This suggests that the westward boundary of the source 268 region had drifted 0.46° westward in longitude over a period of roughly 5 minutes, giv-269 ing a westward drift rate relative to the Earth of roughly  $6^{\circ}/hr$ . We cannot determine 270 the extent of the source region purely from this; to complete the picture, we turn to the 271 ground-based observations from AARDDVARK. 272

Starting with the REY path, shown in Figure 2(c), we compare the change in phase to the ESK spectrogram plotted in Figure 2(a). We can see that the phase change starts and ends roughly in sync with the wave seen at ESK, with the peak of the change in phase coinciding roughly with the peak wave intensity seen in the magnetometer. This suggests that the REY path overlaps with the EMIC source region for the entirety of the event period, and that electron precipitation was occurring for the entire event period.

We turn now to the two NYA paths, from the GQD and GVT transmitters. For 279 each of these paths, we note a phase change that starts in sync with the onset of the wave 280 power in the ESK magnetometer, suggesting that the paths start the event period within 281 the source region. Unlike the REY path, however, the phase change on both of these paths 282 return to zero before the wave power does. This return to zero indicates that no more 283 electron precipitation is occurring along with path, which we attribute to the westward 284 drift of the eastern boundary of the EMIC and EEP source regions, resulting in the east-285 ern most edge of the source region passing over these paths. Importantly, there is a slight 286 difference in the times at which each path returns to zero, with roughly 6 minutes sep-287 arating the them. Using this time offset together with the distance between the two paths, 288 we can calculate the drift rate of the source region, relative to the Earth. Over the L-289 shell region for which we see waves in the satellite data, these two paths are separated 290

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by roughly 0.4° longitude, suggesting a westward drift rate of roughly 4°/hr. We note that this is almost identical to that calculated from the satellite footprints.

To determine the extent of the source region, we first assume that the point in time 293 at which the phase change in the AARDDVARK paths returns to zero occurs when the 294 eastern-most edge of the source region is directly over the path. We then use the calcu-295 lated drift rates to extrapolate back in time, allowing us to determine the location of the 296 eastern-most edge of the source region at the time of wave onset in the satellite data – 297 the difference in this eastern edge and the western edge calculated from the satellite data 298 gives us the extent of the wave source region. The GQD-NYA path returns to zero roughly 200 8 minutes after wave onset in the RBSP-B satellite – if we average our two drift estimates 300 and assume a  $5^{\circ}$ /hr westward drift rate, this suggests that the source region drifts west 301 by roughly 0.67° longitude in this time. The mean longitude of the GQD-NYA path over 302 the L-shell range of the satellite observations is -1.4°E. Thus, at the time of wave onset 303 in the RBSP satellite, the eastern-most edge of the source region was located at a lon-304 gitude of roughly -0.75° E. This gives us a total source region longitudinal extent of ap-305 proximately 11°. 306

At times it may be more useful to determine the source region extent in terms of MLT, rather than geographic longitude, although we note that the drift calculations are typically simpler using longitude due to the inherent time-dependence of MLT. Redoing the above calculation in terms of MLT, we determine a source region extent of roughly 0.83 hr MLT and an approximately negligible MLT drift rate – in other words, the source region is in fact stationary in MLT.

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#### 5 Discussion and conclusions

We have demonstrated a method for determining the approximate longitudinal extent and drift rate of an EMIC source region using a combination of in situ spacecraft and ground-based measurements and the AARDDVARK network. The general process for an arbitrary event is as follows:

Determine the presence and footprint location of EMIC waves using in-situ mag netometer observations. In-situ wave observations for this step are not strictly nec essary, however we note that due to the ability of waves to duct significant dis tances upon reaching the Earth's ionosphere, the ground-based observation of waves

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- is not sufficient to determine the presence of EMIC waves across a given AARD-322 DVARK path. It may be possible to use a proxy instead of direct wave measure-323 ments, for instance the precipitation trigger described in Carson et al. (2013), for 324 this purpose. 325 2. Determine the temporal extent of the wave using ground-based magnetometers. 326 This step is important to provide context for the AARDDVARK measurements, 327 to ensure that timing of the observed VLF signal changes match with the timing 328 of the wave. 329 3. Determine the drift rate of the source region by comparing the times at which the 330 source region boundaries cross the AARDDVARK paths. In this study, we used 331 the time at which the phase change of the VLF signals (relative to the QDC cal-332 culated in Section 3.3) returned to zero, however the time of onset of phase changes 333 is equally valid, provided that this onset is due to the source region drifting over 334 the path. 335 4. Determine the eastern and western boundaries of the event by extrapolating from 336
- the path crossing times using the calculated drift rate. In this study, we were able to use the satellite data to determine the western edge of the source region, however this may not always be possible. In theory this step can be performed with only two AARDDVARK paths (a minimum of two are required to calculate the drift speed relative to the Earth), however in general more paths will allow for a more accurate determination of the source-region size. From these measurements, calculating the size of the source region is fairly trivial, as we have shown.
- We note that the above method will not be possible in all cases, as AARDDVARK coverage will not always be sufficient to calculate the require parameters.
- We can draw comparisons between our method and that of Sakaguchi et al. (2015), who investigated the spatial scale size of EMIC-associated isolated proton aurora (IPA). The authors showed that individual IPA patches were typically less than 12° longitude wide, which places our event at the upper limit of this scale. However, we note that the size reported by Sakaguchi et al. is the size of individual IPA patches rather than the EMIC regions themselves, which may contain several distinct IPA patches.
- A study by Zhang et al. (2016) used in situ and ground-based wave measurements to estimate the source region extent of a single EMIC wave event, estimating an extent

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of 2 h for the H<sup>+</sup> band and 4 h for the He<sup>+</sup> band. These are significantly larger than our
own estimates, however it must be noted that the use of ground-based wave measurements for determining source region extent is unreliable, due to the ducting issues mentioned previously. This could lead to a significant overestimation of the source region size.
We also note that the Zhang et al. (2016) event occurred on the dayside, whereas our
own event was well into the duskside – we cannot rule out an MLT-dependence of the
source region extent. Clearly further study is required to determine if this is the case.

The use of the AARDDVARK network for determining the spatial extent of EMIC 361 wave source regions has benefits over alternative methods. One of the greatest benefits 362 is that of coverage. The AARDDVARK network has the ability to remotely sense changes 363 to the ionosphere in regions impossible for other ground-based instruments to be installed, 364 including oceanic regions and the majority of the southern hemisphere. We note, how-365 ever, that this range is a double-edged sword; care must be taken to ensure that precip-366 itation observed by the AARDDVARK network is indeed due to the EMIC wave in ques-367 tion, and not due to some other precipitation source occurring elsewhere along the same 368 VLF path. Care must also be taken to ensure a valid QDC is used to remove diurnal and 369 other background variations in the signal – in this paper we used a simple method man-370 ually comparing the active period to quiet periods on surrounding days, a well established 371 method in the literature (e.g. Clilverd et al., 2006), however we note that attempts have 372 been made to automate this process (e.g. Neal et al., 2015). 373

In theory, a similar method should be possible with riometers, however these are limited by their sensitivity and scope. Riometers are most sensitive to electron precipitation with energies of hundreds of keV, and do not response strongly to relativistic electron precipitation. They can also only detect electron precipitation that occurs directly overhead the instrument, which limits their utility in such a study. With a dense enough riometer network however, for instance the Canadian GO-RIO network, similar results should be possible.

The presented method is based on the assumption that the extent of the EMIC source region is the same as the extent of the EEP region. To justify this, we need only look to the AARDDVARK data presented earlier in this paper. In Figure 2(d), we showed that the onset of the phase change in each of the paths lined up almost perfectly with the onset of EMIC wave power in the ESK magnetometer, suggesting that EMIC driven

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electron scattering begins almost immediately after wave generation. This is supported
by the literature as well; Omura and Zhao (2013) and Kubota and Omura (2017) both
showed that electron precipitation occurs within seconds of interaction with rising-tone
EMIC waves, such as the wave in this case study. We also note that the REY path, shown
in Figure 2(d), passes very close to the western edge of the event region, as defined by
the RBSP-B and Arase satellites. This suggests that any longitudinal lag between the
wave region and the precipitation region is likely very small.

Being able to determine the extent of EMIC source regions has important impli-393 cations for the study of EMIC waves. When investigating the impact that EMIC waves 394 have on radiation belt electron and ion populations, knowledge of the longitudinal ex-395 tent of the EMIC wave region is essential – clearly, larger regions will have a greater ef-396 fect on radiation belt populations. Being able to quantify this size will allow for more 397 accurate simulations of EMIC wave-particle interactions, leading to better understand-398 ing of the scattering processes involved. Knowledge of the boundaries of the wave source 399 region is also important for investigating EMIC wave generation, for instance determin-400 ing how the scale of these regions varies across different wave observations, and whether 401 this variation ties into other wave properties. 402

The clear downside of this technique is that it only works on EMIC waves that are 403 actually capable of scattering electrons into the loss-cone. In their study of EMIC-driven 404 electron precipitation, Hendry et al. (2016) showed that there was a distinct difference 405 between the spatial distribution of EEP-producing EMIC waves and EMIC waves as a 406 whole, with EEP-producing EMIC waves typically occurring around magnetic midnight, 407 well away from the typical peak in EMIC occurrence (e.g. Saikin et al., 2015). Thus, while 408 this technique provides an invaluable insight into these EEP-producing waves, we must 409 devise other techniques for determining the extent of other active EMIC waves. 410

There is an interesting aspect of the EMIC source-region examined in this study that bears further investigation. One of the prevailing theories of IPDP-type wave generation suggests that the wave growth is driven by substorm-related ion injections at magnetic midnight, which drift clockwise (i.e., in a negative MLT direction) around the Earth (e.g. Yahnin et al., 2009). However, in Section 4, we observed that the source region was in fact static with respect to MLT. This suggests that for this particular case study, ion injections are not the driving process of the wave generation. This is not without prece-

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dent; other studies of EMIC waves have seen source regions that do not drift in MLT (e.g. Hendry et al., 2016). At present it is unclear what the true driving process might be; we hope to answer this in a future study.

As a proof of concept, this study shows that not only is it feasible, but that it is a relatively simple process to calculate the extent of an EEP-driving EMIC source region from the EEP signature in ground-based VLF measurements. We hope to expand this method into a broader study of EEP-driving EMIC waves, to derive statistics on the size of these wave regions. We hope that this will lead to a better understanding of the generation of EEP-driving EMIC waves, as well as the wave-particle interaction processes themselves.

#### 428 Acknowledgments

The authors would like to thank the personnel who developed, maintain, and operate each of the satellites and instruments used in this study. Processing and analysis of EM-FISIS data was performed under the support of JHU/APL contract no. 921647 under NASA Prime contract No. NAS5-01072. EMFISIS data may be obtained from http://emfisis.physics.uiowa.edu/data/index. The search coil magnetometer data

used in this study are available from BGS on request. Science data of the ERG (Arase)
satellite used in this study were obtained from the ERG Science Center operated by ISAS/JAXA
and ISEE/Nagoya University (https://ergsc.isee.nagoya-u.ac.jp/index.shtml.en) (Miyoshi
et al., 2018). The present study analyzed the MGF v01.00 data and the MEP-i v01\_00
data. AARDDVARK data availability is described at

http://www.physics.otago.ac.nz/space/AARDDVARK\_homepage.htm. This work
has been supported by the postdoctoral program of the Czech Academy of Sciences and
by its Praemium Academiae award and JSPS-19-05 project. OS also acknowledges support from grants LTAUSA17070 and GACR 18-05285S. This study is supported by Grantsin-Aid for Scientific Research (15H05815, 16H06286,17H00728) of Japan Society for the
Promotion of Science (JSPS). This study was supported by JSPS Bilateral Open Partnership Joint Research Projects.

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Figure 1.



Figure 2.

