Comparing electron precipitation fluxes calculated from pitch angle diffusion coefficients to LEO satellite observations

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9 Key Points:

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10	•	The simulated and measured precipitation are well correlated on the dawnside at
11		$L^* > 5$ for $> 30 \text{keV}$ electrons.
12	•	Additional diffusion is required at higher energies, >100 keV, and on the dusk-
13		side.
14	•	The total precipitating flux typically exceeds that measured by POES by a fac-
15		tor between 1 and 10.

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16 Abstract

Particle precipitation is a loss mechanism from the Radiation Belts whereby particles 17 trapped by the Earth's magnetic field are scattered into the loss cone due to wave-particle 18 interactions. Energetic electron precipitation creates ozone destroying chemicals which 19 can affect the temperatures of the polar regions, therefore it is crucial to accurately quan-20 tify this impact on the Earth's atmosphere. We use bounce-averaged pitch angle diffu-21 sion coefficients for whistler mode chorus waves, plasmaspheric hiss and atmospheric col-22 lisions to calculate magnetic local time (MLT) dependent electron precipitation inside 23 the field of view of the Polar Orbiting Environmental Satellites (POES) T0 detector, be-24 tween 26-30 March 2013. These diffusion coefficients are used in the BAS Radiation Belt 25 Model (BAS-RBM) and this paper is a first step towards testing the loss in this model 26 via comparison with real world data. We find the best agreement between the calculated 27 and measured T0 precipitation at $L^*>5$ on the dawnside for the >30keV electron chan-28 nel, consistent with precipitation driven by lower band chorus. Additional diffusion is 29 required to explain the flux at higher energies and on the dusk side. The POES T0 de-30 tector underestimates electron precipitation as its field of view does not measure the en-31 tire loss cone. We demonstrate the potential for utilizing diffusion coefficients to recon-32 struct precipitating flux over the entire loss cone. Our results show that the total pre-33 cipitation can exceed that measured by the POES >30 keV electron channel by a fac-34 tor that typically varies from 1 to 10 for $L^* = 6, 6.5$ and 7. 35

1 Introduction

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The Van Allen radiation belts are highly dynamic regions of trapped particles in 37 the Earth's magnetosphere which can pose a threat to satellites (e.g. Baker et al. (1987)). 38 Radiation belt particles also have an impact on our atmosphere when they are lost by 39 precipitation and collide with atmospheric particles, creating ozone-destroying chemi-40 cal species such as odd nitrogen (NO_x) and odd hydrogen (HO_x) (Thorne, 1977). Both 41 of these species are capable of effecting the atmospheric chemistry in their own right, but 42 ozone concentration plays a significant role in controlling the temperature and dynam-43 ics of the atmosphere (Andersson et al., 2014). The full extent of the impact of radia-44 tion belt particles on our atmosphere is an outstanding question associated with solar 45 forcing of the climate system (Matthes et al., 2017). Changes in the surface tempera-46 tures of the polar regions have been linked with enhanced geomagnetic activity (e.g. Seppälä 47

et al. (2009); Baumgaertner et al. (2011)) and it has been shown that particle precip-

⁴⁹ itation can impact regional climate patterns (Rozanov et al., 2005).

There have been several attempts at quantifying the input of electron precipita-50 tion into our atmosphere (Andersson et al., 2018; Orsolini et al., 2018), and it is now in-51 cluded as part of the Climate Modelling Intercomparison Project Phase 6 (CMIP6, Matthes 52 et al. (2017)). Van de Kamp et al. (2016, 2018) obtained data from low-Earth orbiting 53 Polar Orbiting Environmental Satellites (POES) between 2002–2012 to create the Ap-54 Energetic Electron Precipitation (APEEP) model for the CMIP6 dataset. The model 55 is focused on the energy range 0.3-1 MeV and runs at a resolution of either 3 hours or 56 1 day. However, this model relies on a POES instrument which does not account for the 57 entire loss cone (e.g. Rodger et al. (2013)). Nesse Tyssøy et al. (2016) used wave-particle 58 theory to try and correct for the POES field of view issue and construct a more com-59 plete picture of the electron precipitation fluxes across the whole bounce loss cone. 60

Trapped radiation belt particles can be pitch angle scattered into the loss cone by 61 resonant wave-particle interactions. Particle precipitation is known to increase with ge-62 omagnetic activity (e.g. Horne et al. (2009)). Meredith et al. (2011) found electron pre-63 cipitation to increase during the passage of high-speed solar streams; these increases in 64 precipitation were mostly seen on the dawnside, making chorus waves a likely candidate 65 for their scattering. Chorus waves can resonate with electrons of energies from a few hun-66 dred eV up to several MeV (Horne et al., 2005) and are predominately observed outside 67 the plasmasphere on the dawnside of the magnetosphere (e.g. Meredith et al. (2003)). 68 Lam et al. (2010) found that lower-band chorus plays a dominant role in scattering >30 keV 69 electrons. Plasmaspheric hiss has also been shown to scatter electrons between 20 keV -70 2 MeV (Meredith et al., 2004). Plasmaspheric hiss is typically observed in high density 71 regions such as the plasmasphere and plasmaspheric plumes. The wave intensities tend 72 to be strongest during active conditions on the dayside in the region $2 < L^* < 4$. How-73 ever, during quiet conditions and on the dusk-side, weaker hiss intensities have been ob-74 served at higher L^{*} values (e.g., (Meredith et al., 2018)). Other sources of precipitation 75 include electromagnetic ion cyclotron (EMIC) waves which generally resonate with elec-76 trons >500 keV (Summers & Thorne, 2003; Hendry et al., 2017). Magnetosonic waves 77 have been observed in all MLT sectors outside the plasmasphere but are restricted to the 78 duskside inside the plasmasphere (Meredith et al., 2008); these waves are capable of ac-79 celerating trapped electrons to high energies, similar to chorus waves, but they are not 80

thought to contribute to precipitation in their own right as they do not scatter particles directly into the loss cone (Horne et al., 2007). However, magnetosonic waves may contribute to electron loss rates by scattering particles at higher pitch angles which can then be diffused by other plasma waves (e.g. Meredith et al. (2009)).

Wave-particle interactions are represented in some radiation belt models (such as 85 those described in Albert et al. (2009); Subbotin et al. (2010); Glauert et al. (2014)) by 86 diffusion coefficients. In this paper we are using bounce-averaged versions of the pitch 87 angle diffusion coefficients used in the BAS Radiation Belt Model (BAS-RBM) to cal-88 culate electron precipitation. The BAS-RBM solves a 3-D Fokker-Planck diffusion equa-89 tion for the electron flux taking into account radial diffusion, acceleration and losses due 90 to wave-particle interactions, magnetopause shadowing and losses due to atmospheric 91 collisions (Glauert et al., 2014). This model has been extensively used to simulate the 92 trapped radiation belt population, for example, Glauert et al. (2018) recently employed 93 the code to run over a 30 year period and found good agreement with GIOVE-B data. 94 However, the diffusion coefficients used in the BAS-RBM have yet to be utilized to sim-95 ulate electron precipitation or to calculate the electron flux inside the loss cone. Inves-96 tigating electron precipitation in a model such as this is important, not only because elec-97 tron precipitation plays a role in atmospheric chemistry (as discussed above), but also 98 to validate the losses when simulating the trapped population. Very few attempts have 99 been made to quantify loss from radiation belt models. Ferradas et al. (2019) indirectly 100 looked by testing three different loss mechanisms in a radiation belt model but only com-101 pared to trapped flux measurements from the Van Allen Probes (VAP). Jordanova et 102 al. (2016) investigated mechanisms for short lived particle injections and their subsequent 103 trapping or loss in a radiation belt model, finding good agreement with observations of 104 both trapped and precipitating flux measured by VAP and POES satellites respectively. 105 In this paper, we will compare precipitating flux calculated using diffusion coefficients 106 with precipitation measurements from POES between 26-30 March 2013. The March 2013 107 period has been studied by several authors, for example Xiao et al. (2014), Li et al. (2014), 108 Shprits et al. (2015), Ripoll et al. (2017), Ripoll et al. (2019) and references therein. The 109 analysis presented in this paper is a direct test of the how well the diffusion coefficients 110 used in the BAS-RBM are able to quantify the precipitating flux and therefore a first 111 step towards testing the loss within the BAS-RBM without actually running the BAS-112 RBM code itself, which is left for a future study. 113

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The pitch angle diffusion coefficients evaluated in this analysis are described in Section 2.1 and the POES electron instruments are outlined in Section 2.2. The theory and method of how we calculate the electron precipitation is given in Section 3. Our results are presented in Section 4, where we give a comparison to the POES data in Section 4.1 followed by a demonstration of how our analysis may one day be implemented to reconstruct the entire loss cone (currently missed by POES) in Section 4.2. The results are discussed and the conclusions presented in Sections 5 and 6 respectively.

121 2 Data sets

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2.1 Diffusion coefficients

We have combined bounce-averaged pitch angle diffusion coefficients ($< D_{\alpha\alpha} >$) 123 from whistler mode chorus waves, plasmaspheric hiss and atmospheric Coulomb colli-124 sions The contributions from EMIC waves are also included but are negligible at the en-125 ergies we are looking at and therefore not discussed further in this paper. The hiss and 126 chorus $D_{\alpha\alpha}$ used in the BAS-RBM are calculated from the PADIE code (Glauert & Horne, 127 2005) which requires the wave power spectrum, wave-normal angle and the ratio of f_{pe}/f_{ce} . 128 The wave power spectra and f_{pe}/f_{ce} are determined by averaging observations from mul-129 tiple spacecraft which have been binned by frequency, L*, MLT, magnetic latitude and 130 geomagnetic activity level. Therefore, the diffusion coefficients used in this study are av-131 eraged diffusion coefficients and not event-specific as in, for example, Ripoll et al. (2019). 132

For the chorus waves, we are using pitch angle diffusion coefficients derived from 133 a new wave database using data from seven satellites presented in Meredith et al. (2020). 134 The calculations for $\langle D_{\alpha\alpha} \rangle$ are done in nearly the same way as Horne et al. (2013) 135 with a few differences: a data driven version of PADIE that takes a frequency spectrum 136 rather than Gaussian parameters has been used, there is no interpolation in L^* and the 137 f_{pe}/f_{ce} has a 1 hour MLT grid rather than 3 hours. As in Horne et al. (2013), the sta-138 tistical wave power maps used in calculating the average chorus wave diffusion coefficients 139 exclude wave observations that are thought to be inside the plasmapause; this is inferred 140 from a combination of observations of plasmapause crossings (where available) and a plasma 141 density model (Carpenter & Anderson, 1992). A mask is also applied to the wave power 142 map whereby anything inside a modelled plasmapause is set to zero (Meredith et al., 2018). 143

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The wave-normal angle spectrum was assumed to be a Gaussian in the tangent of the wave-normal angle (as in Horne et al. (2013); Glauert and Horne (2005)).

The diffusion coefficients for the hiss waves were derived as described in Glauert et al. (2014) using an updated wave model based on data from eight satellites described in Meredith et al. (2018). These $\langle D_{\alpha\alpha} \rangle$ were calculated using a variable wave-normal angle, where the peak wave-normal angle is field aligned at the equator and then increases with increasing latitude (Glauert et al., 2014). Similar to the chorus wave data, the wave power outside the plasmapause is excluded by a mask (Meredith et al., 2018).

The top three rows of Figure 1 show global maps of the chorus and hiss $\langle D_{\alpha\alpha} \rangle$ 152 for low, moderate, and high geomagnetic activity levels, as specified by Kp, for the elec-153 tron energies at 30 keV, 100 keV, and 300 keV. The values of $\langle D_{\alpha\alpha} \rangle$ used in this study, 154 and shown in Figure 1, have been averaged over the loss cone at each L-shell (the loss 155 cone angle has been calculated assuming a dipole magnetic field and an atmospheric al-156 titude of 100 km, as is done in the PADIE calculations). The yellow line in the figures 157 marks the modelled location of the plasmapause (Lpp); this line is shown dashed between 158 14-22 MLT as more work is needed to determine the average location of the plasmapause 159 in this region. As mentioned above, this modelled Lpp was used as a mask to separate 160 the wave power inside and outside the plasmapause when calculating the diffusion co-161 efficients and therefore the yellow line in the figures separates the hiss and chorus $\langle D_{\alpha\alpha} \rangle$. 162 For reference, the bottom row of Figure 1 shows the values of the f_{pe}/f_{ce} used in the cal-163 culations of the hiss and chorus $\langle D_{\alpha\alpha} \rangle$, again separated by the Lpp. 164

Figure 1 demonstrates that the chorus $\langle D_{\alpha\alpha} \rangle$ have a strong MLT dependence 165 which peaks on the dawnside, consistent with enhanced chorus power and low values of 166 f_{pe}/f_{ce} in this region during active conditions (e.g., Meredith et al. (2003)). The $\langle D_{\alpha\alpha} \rangle$ 167 outside the plasmapause are strongest for 30 keV electrons, suggesting that chorus waves 168 are better at scattering electrons at lower energies. During active conditions the region 169 of strongest diffusion for 30 keV electrons moves to higher L shells in the pre-noon sec-170 tor. This is consistent with the behaviour of the peak in the chorus wave power which 171 also shows a similar dependence on MLT in the equatorial region (Meredith et al., 2020). 172

As discussed above, the $\langle D_{\alpha\alpha} \rangle$ for chorus and hiss waves have pitch angle, energy, L-shell, MLT and geomagnetic activity dependence. The top two panels of Figure 2 show the chorus and hiss diffusion coefficients $\langle D_{\alpha\alpha} \rangle$ as a function of pitch angle



Figure 1. Top three rows showing the global distribution of the bounce-averaged diffusion coefficients for chorus waves and hiss waves at electron energies of 30 keV, 100 keV and 300 keV for low, moderate and high geomagnetic activity levels averaged over the dipolar loss cone. The yellow line shows the Lpp which marks the boundary between the hiss and chorus $\langle D_{\alpha\alpha} \rangle$. The bottom row shows the f_{pe}/f_{ce} used to calculate the . Noon is at the top and dawn is to the right.

for 30 keV electrons at $L^* = 5.5$ during high geomagnetic activity levels (4 < Kp < 7) 176 for different MLT sectors (shown in different colours). The loss cone angle is shown by 177 a vertical dashed line. Over this limited pitch angle range close to the loss cone, the dif-178 fusion coefficients for both chorus and hiss are fairly flat. Both waves show strong MLT 179 dependence with the hiss $\langle D_{\alpha\alpha} \rangle$ only contributing on the duskside (and inside the plas-180 masphere) and the $\langle D_{\alpha\alpha} \rangle$'s for chorus are strongest on the dawnside (as can be seen 181 in Figure 1). The strong diffusion limit at $L^* = 6$ and E = 30 keV is 3.7×10^{-3} s⁻¹ (cal-182 culated following Summers and Thorne (2003) and indicated by a dotted line in Figure 2), 183 showing that the diffusion driven by chorus approaches the strong diffusion limit on the 184 dawnside at this energy, L-shell and geomagnetic activity level. 185

The bottom panel of Figure 2 shows the $D_{\alpha\alpha}$ for the coulomb collisions, these $D_{\alpha\alpha}$ 186 are calculated as a function of energy and L-shell, as outlined in Abel and Thorne (1998). 187 The neutral and plasma densities are taken from the NRLMSISE-00 (Picone et al., 2002) 188 model and the GCPM (Gallagher et al., 2000) respectively. In these calculations, the edge 189 of the loss cone is defined to be where the energy of the electrons has dropped by 1/e190 of its original value due to collisions with atmospheric particles. The loss timescales (τ_C) 191 is set to be a quarter of the bounce time in the loss cone and infinite elsewhere. Figure 2 192 demonstrates that the collision $D_{\alpha\alpha}$ only contribute inside or near to the 100 km loss 193 cone and fall off rapidly outside. We neglect energy diffusion of coulomb collisions in this 194 study but note it could be important at larger pitch angles as shown by Selesnick (2012) 195 and Cunningham et al. (2018). 196

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2.2 The Polar Orbiting Environmental Satellites (POES)

The POES constellation of spacecraft are in Sun-synchronous orbits at a low al-198 titude of 800-850 km altitude. We have obtained data from the Space Environment Mon-199 itor (SEM-2) package on board POES spacecraft NOAA15 to 19. The SEM-2 package 200 includes the Medium Energy Proton and Electron Detectors (MEPED), which has two 201 electron solid state detectors capable of measuring electrons between 30-2500 keV in three 202 integral channels (>30 keV, >100 keV and >300 keV) (Evans & Greer, 2004). Each chan-203 nel is known to suffer from proton contamination (e.g. Yando et al. (2011)), we are eval-204 uating data which have been corrected for this using the bow tie method described in 205 Lam et al. (2010). Both detectors are $\pm 15^{\circ}$ wide, one centered 9° from local zenith (the 206 0° detector, T0) and the other mounted perpendicular to this (the 90° detector, T90 anti-207



Figure 2. Bounce-average pitch angle diffusion coefficients ($\langle D_{\alpha\alpha} \rangle$) from the BAS-RBM at $L^* = 5.5$ and $4 \langle Kp \langle 7$, shown for chorus and hiss waves (top two panels) and coulomb collisions (bottom panel). The $\langle D_{\alpha\alpha} \rangle$ for chorus and hiss are shown for MLT sectors, indicated on the right hand side on the plot. The angle of the loss cone is shown by a vertical dashed line and the strong diffusive limit is shown by a dotted line in the top panel.

parallel to the spacecraft velocity). The 0° detector predominately measures electrons in the bounce loss cone for L >1.4 (Rodger, Clilverd, et al., 2010). The 90° detector measures a mixture of electrons in drift and bounce loss cones and those that are trapped (Rodger, Carson, et al., 2010).

To make sure we are only evaluating data from T0 when its measuring precipitating flux and T90 when its measuring flux outside the loss cone in our analysis, we make sure the equatorial loss cone angle (α_0) is greater than the field of view of the T0 detector and less than the field of view of the T90 detector. We calculate α_0 at each time using

$$\alpha_0 = \sin^{-1} \left(\sqrt{\frac{B_{eq}}{B_{POES_FOFL}}} \right),\tag{1}$$

where B_{eq} is the magnetic field strength at the equator (given by Olson-Pfitzer quiet time model (Olson & Pfitzer, 1977)) and B_{POES_FOFL} is the field strength at the foot of the field line at the location of POES (assumed to be 100 km, from the IGRF). The T0 and T90 fields of view are projected to the equator using

$$\alpha_{eq} = \sin^{-1} \left(\sqrt{\frac{B_{eq}}{B_{POES}}} \sin(\theta_{T90/0} \pm 15^{\circ}) \right), \tag{2}$$

where $\theta_{T90/0}$ are the central pitch angles of each detector (of which we take $\pm 15^{\circ}$ to take into account for the entire field of view) and B_{POES} is the magnetic field strength at the height POES (from the IGRF). We note that this does not guarantee T90 is measuring trapped flux as it could be measuring flux in the drift loss cone.

²²⁵ 3 Calculation of POES precipitating flux

To calculate the precipitating flux measured by POES, we are using a steady state solution to a Fokker Planck equation for pitch angle diffusion from Kennel and Petschek (1966), given by:

$$J_{eq}(E, \alpha_{eq}) = N \ S(E) \ D_{\alpha\alpha}(\alpha_0)^{-1} \left[h(\alpha_0) + \ln\left(\frac{\sin\alpha_{eq}}{\sin\alpha_0}\right) \right],\tag{3}$$

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outside the loss cone $(\alpha_0 \leq \alpha_{eq} \leq \frac{\pi}{2})$, and

$$J_{eq}(E, \alpha_{eq}) = N \ S(E) \ D_{\alpha\alpha}(\alpha_0)^{-1} \ h(\alpha_{eq}), \tag{4}$$

inside the loss cone $(\alpha_{eq} \leq \alpha_0)$, where

$$h(\alpha_{eq}) \equiv \frac{\sqrt{D_{\alpha\alpha}(\alpha_0)\tau}}{\alpha_0} \left[\frac{I_0\left(\frac{\alpha_{eq}}{\sqrt{D_{\alpha\alpha}(\alpha_0)\tau}}\right)}{I_1\left(\frac{\alpha_0}{\sqrt{D_{\alpha\alpha}(\alpha_0)\tau}}\right)} \right].$$
 (5)

 $J_{eq}(E, \alpha_{eq})$ is the equatorial flux distribution for electrons, E is the energy, α_{eq} are 231 the equatorial pitch angles, τ the bounce loss time (assumed to be a quarter of a bounce 232 period), N is a normalisation factor, S(E) is the source of particles (N and S(E) will 233 be defined in Section 3.1), I_0 and I_1 are modified Bessel functions and $D_{\alpha\alpha}(\alpha_0)$ are the 234 combined bounce-averaged pitch angle diffusion coefficients from the BAS-RBM (described 235 in Section 2.1) evaluated at the loss cone. The value of $D_{\alpha\alpha}(\alpha_0)$ is determined at each 236 time depending on the L^*/MLT location of the spacecraft and the current geomagnetic 237 activity level. 238

Despite being a solution for a steady state, this application has been validated in several studies by comparison to different data sets (for example, the POES electron observations in Li et al. (2013) and Nesse Tyssøy et al. (2016)). Furthermore, this steady state solution is independent of the scattering mechanism for pitch angle diffusion (Theodoridis & Paolini, 1967) and therefore we can use the combined diffusion coefficients from the BAS-RBM (described in Section 1.2).

Figure 3 demonstrates the differential flux (J_{eq}) calculated from Equations 3 and 245 4 for a range of diffusion coefficients (indicated in the bottom right corner of Figure 3d) 246 at $L^* = 4, 5, 6, 7$ and for 30 keV (solid lines) and 100 keV (dashed lines) electrons. Here 247 we have adopted a common source term of $S(E) = 10^5 \text{ cm}^{-2} \text{ sr}^{-1} \text{ s}^{-1} \text{ keV}^{-1}$ at $\alpha_{eq} = \frac{\pi}{2}$ 248 as an example of a reasonable source term and assumed at dipolar loss cone (shown by 249 the vertical dotted black line). The strong diffusion limit has been calculated following 250 Summers and Thorne (2003) for 30 keV (red) and 100 keV (yellow) at each L^* and is 251 shown at the top of each figure; these figures show at the strong diffusion limit, we have 252 a near isotropic distribution between the trapped and the precipitating flux. As the dif-253 fusion coefficients decrease, the flux in the loss cone drops off exponentially. The median 254 field of view (FOV) of the POES T90 and T0 (which have been projected to the equa-255 tor using Equation 2) during the event investigated in this paper (26-30 March 2013) are 256 indicated by grey shaded regions for each L^{*}. This demonstrates that the FOV of the 257 T0 detector is not measuring the entire loss cone and therefore any precipitating flux mea-258 surements from this channel will be an underestimate unless the loss cone is full, as pre-259

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Figure 3. Each panel shows the differential flux calculated from Equations 3 and 4 at for 30 keV (solid) and 100 keV (dashed) electrons for a range of diffusion coefficients (given in the bottom right figure) at (a) $L^* = 4$, (b) $L^* = 5$, (c) $L^* = 6$ and (d) $L^* = 7$. The red and yellow lines show the flux calculated during the strong diffusion limit (values for which are given at the top of each figure). Median values for the T90 and T0 field of view each L^* are indicated by grey shaded regions.

viously shown by Rodger et al. (2013). Furthermore, the T90 FOV is very close to the
loss cone and therefore when selecting our data points for analysis we always make sure
the T90 FOV is outside the bounce loss cone as discussed above. We also note that the
trapped flux drops significantly just outside the loss cone, this is taken into account as
discussed below.

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3.1 Energy spectrum and source term

To get the source term and normalisation factor, N S(E), in equations 3 and 4, we convert the T90 measurement of the trapped integral flux to differential flux by assuming a kappa-type function (Xiao et al., 2008; Whittaker et al., 2013) for the energy spectrum of the source flux $(J_S(E))$. By adopting similar notation to Equation 10 in Glauert et al. (2018) this gives

$$J_S(E) = m_0 \frac{E(E+2E_0)}{E_0} P_1 \left(1 + \left(\frac{E}{P_2}\right)^2\right)^{-(\kappa+1)} dE,$$
(6)

where E_0 is the particle rest energy, given by m_0c^2 (m_0 is the rest mass and c is 271 the speed of light). We adopt $\kappa = 5$, as in Li et al. (2013), and solve for P_1 and P_2 . For 272 P_2 , we use an iterative method, whereby we take the difference of the ratio between the 273 POES T90 >30 keV and >100 keV detector measurements and the ratio of Equation 6 274 integrated between 30 keV to 2.5 MeV and 100 keV to 2.5 MeV (to simulate the POES 275 detectors) until the difference is less than 1×10^{-3} . We then take this value of P₂ and 276 the >30 keV T90 measurement to solve for P_1 and obtain an overall kappa-type fit for 277 the differential flux. Figure 4 demonstrates the differential flux estimated from this method 278 for one of the L*/MLT sectors in our analysis (L* = 6, 09-12 MLT), where the P_1 and 279 P_2 solutions are indicated for each spectra at each time step. 280

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We use this distribution to solve for N S(E) by rearranging Equation 3 as follows:

$$N S(E) = \frac{J_S(E)}{D_{\alpha\alpha}(\alpha_0)^{-1} \left[h(\alpha_0) + \ln \frac{\sin(\alpha_{eq})}{\sin(\alpha_0)}\right]}.$$
(7)

Here we take the central pitch angle of the T90 detector (θ_{T90}) as α_{eq} , which has been transformed to the equator using Equation 2.



Figure 4. Differential electron flux spectra fitted to a kappa-type distribution using Equation 6. The values of P1 and P2 are shown for each spectra at each time step (indicated by the color). This spectra is evaluated at θ_{T90} , which corresponds to the pitch angle location of the T90 detector.

Note that the calculation of N S(E) is for the equatorial pitch angle corresponding to that observed by the POES T90 detector and not that at $\alpha_{eq} = \frac{\pi}{2}$. This therefore takes into account the change in flux for different diffusion rates just outside the loss cone in the steady state solution.

By employing this method to obtain the source term, we are not using the flux output calculated by the BAS model but instead our best assessment of what the actual flux was from the POES T90 experimental measurements. Therefore the analysis presented in this paper is a test of the BAS wave diffusion matrix and not the model itself.

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3.2 Comparing to POES T0 measurement

We calculate the theoretical flux measured by the POES T0 detector by integrating the differential flux $(J_{eq}(E, \alpha_{eq})$ from Equations 3-4) inside the FOV of the POES detectors based on an equation from Walt (1994) given by

$$J_{calc}(E > E_{th}) = \frac{\int_{E_{th}}^{E_{max}} \int_0^{2\pi} \int_0^\beta J_{eq}(E, \alpha_{eq}) A \sin \eta \, \mathrm{d}\eta \, \mathrm{d}\psi \, \mathrm{d}E}{\int_0^{2\pi} \int_0^\beta A \sin \eta \, \mathrm{d}\eta \, \mathrm{d}\psi},\tag{8}$$

where A is the detector area (stated to be 25 mm² for the solid-state detector in the POES electron detector telescope in Evans and Greer (2004)) and E_{th} and E_{max} are the thresholds of the POES electron detectors (30, 100 and 300 keV) and maximum energy (taken to be 2.5 MeV as a representative nominal value) respectively. A similar approach was adopted for comparison with POES data in Li et al. (2013). The value of J_{calc} will be directly compared with POES measurements later in this paper.

The pitch angle of the detector is given by

$$\cos \alpha = \cos \theta \cos \eta + \sin \theta \sin \eta \cos \psi, \tag{9}$$

where α is the local pitch angle at the POES detectors, θ is the central pitch angle of the POES detector (provided with the data), β is the half-angle of detector acceptance (15° for the POES T0 detector) and η and ψ are integrated over the field of view of the POES detector (as demonstrated by Figure 1b of Li et al. (2013)). We transform α to the equator (by Equation 2) before using in Equations 3 and 4 to calculate the equatorial flux.

In Equation 8, we are effectively dividing a count rate by a geometric factor (GF). 309 The POES documentation states that the count rate should be divided by GF = 0.01310 to get the integral flux (Evans & Greer, 2004) (updated modelling of the MEPED in-311 strumentation and the electron telescope geometric factors shows this is reasonable for 312 most energies (Yando et al., 2011)). However, the GF was calculated for an isotropic elec-313 tron flux (Evans & Greer, 2004) whereas the flux in the loss cone can be highly anisotropic 314 (as demonstrated in Figure 3). Furthermore, the GF takes into account the sensitivity 315 of the detector which we do not need to do as we are calculating true theoretical count 316 rates from Equation 8 and not count rates as measured by an instrument. In the anisotropic 317 case here we compute the flux that would be measured numerically and use an effective 318 geometric factor (GF*), where $GF^* = \int_0^{2\pi} \int_0^{\beta} A \sin \eta \, \mathrm{d}\eta \, \mathrm{d}\psi = 2\pi \cdot \mathbf{A} \cdot (1 - \cos \beta).$ 319

320 4 Results

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4.1 POES Comparison

We present precipitation flux observations from NOAA15, 16, 17, 18 and 19 between 322 26-30 March 2013, shown in Figure 5. The data from each spacecraft have been com-323 bined by taking the mean of the measurements over 0.5 L^{*}, for example at a quoted $L^* = 6$ 324 we have averaged the flux data between $6-6.5 \text{ L}^*$ from each spacecraft in both hemispheres; 325 this is done to match the L^{*} bins of the $\langle D_{\alpha\alpha} \rangle$ used in the analysis. The L^{*} associ-326 ated with the POES data in this paper were calculated using the International Geomag-327 netic Reference Field and the T96 external field (Tsyganenko, 1995), as in Allison et al. 328 (2018). This event captures minor geomagnetic storms, with low/moderate Dst level and 329 moderate/high Kp level (high for 12 hours on March 27) as shown in the bottom panel 330 of Figure 5, and avoids a solar proton event seen earlier in the month. To minimise the 331 chance of proton contamination, we have omitted times where the POES satellites were 332 within the longitude of the South Atlantic anomaly as in that area protons overwhelm 333 the electron observation from both telescopes (e.g. Figure 4 of Rodger et al. (2013)). The 334 top three panels of Figure 5 give an overview of the POES T0 measurements at $L^* =$ 335 4, 5, 6 for the three electron channels; it can be seen that the precipitating fluxes are great-336 est at $L^* = 6$ for the >30 keV channel during periods when the geomagnetic activity is 337 highest. 338

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Figure 5. The top three panels show the POES flux for the >30 keV (black), >100 keV (blue) and >300 keV (red) electron channels at $L^* = 4$, 5 and 6 respectively. The dotted horizon-tal line shows the noise threshold. The bottom panel gives the geomagnetic Kp (black) and Dst (blue) indices during this event.

For our analysis, we adopt a strict noise threshold of $1000 \text{ cm}^{-2} \text{ sr}^{-1} \text{ s}^{-1}$ for each electron channel, indicated by a horizontal dotted line in the top three panels. It can be seen that during this event, the precipitating flux measured by the >300 keV channel (red) is predominately below this line and will therefore not be considered for the remainder of this paper.

Figures 6a and b show the agreement between our calculated T0 precipitation $(J_{calc},$ 344 from Equations 3-8) and the POES T0 (blue line) and T90 measurements (red line) at 345 $L^* = 7$ between 09-12 MLT and $L^* = 5$ between 21-24 MLT respectively. The calculated 346 T0 flux, shown by black crosses, remains below the flux measured by T90 as required. 347 The bottom panel in each figure shows the Kp and the selected diffusion coefficients for 348 30 keV (crosses) and 100 keV (triangles) used at each time for our calculation; these are 349 representative values for each energy channel, >30 keV (top panel) and >100 keV (mid-350 dle panel), as the flux is highest for these energies and therefore these diffusion coeffi-351 cients dominate our flux calculation. The $\langle D_{\alpha\alpha} \rangle$ are selected at each energy depend-352 ing on the location of POES in terms of L^{*} and MLT at each time step (the $\langle D_{\alpha\alpha} \rangle$ 353 have 0.5 L^{*} and 1 hour MLT resolution, however we do our analysis over 3 hours of MLT 354 to increase the number of data points in each L*/MLT sector). The activity level of the 355 $< D_{\alpha\alpha} >$ is chosen depending on either the current Kp or the Kp averaged over the last 356 12 hours, which ever is highest, to take into account the time history of the system (re-357 ferred to as Kp^{*} in later plots). We have also averaged the $\langle D_{\alpha\alpha} \rangle$ over all pitch an-358 gles within the loss cone (see Figure 2). 359

The top panel of Figure 6a shows good agreement between the measured and cal-360 culated T0 precipitation for the >30 keV integral flux channel. We note, at this L-shell 361 and MLT location that these results are consistent with chorus wave driven diffusion, 362 this is will be discussed more below. For the >100 keV channel (middle panel), our cal-363 culations are underestimating the precipitation. Figure 6b, on the other hand, shows us 364 an example where our calculated flux is much lower than that measured by POES T0, 365 with much of the calculated T0 precipitation below the y-range on the plot axis (all for 366 the >100 keV channel). We can see from the bottom panel Figure 6b that, at this MLT 367 and L-shell, the BAS wave model predicts a large number of the $\langle D_{\alpha\alpha} \rangle$'s to be be-368 tween 10^{-5} and 10^{-6} s⁻¹ (particularly for 100 keV). Figure 3b (blue and cyan lines) shows 369 these values for the $D_{\alpha\alpha}$ correspond to an exponential drop off in the flux in the loss cone 370 which is outside the median FOV of the T0 detector during this event; this will there-371

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Figure 6. Figure showing the flux measured by the POES electron detector for the >30 keV (top) and >100 keV (middle) channels for the 0° (blue) and 90° (red) telescopes and the Kp index during the event (bottom) for (a). L* = 7, 09-12 MLT and (b). L* = 5, 21-24 MLT. The black crosses in the top two panels show the calculated precipitation from the BAS-RBM. The blue crosses and triangles in the third panel show the diffusion coefficients selected at each time for 30 and 100 keV respectively. The red and yellow dashed lines represent the strong diffusion limit for the 30 keV and 100 keV electrons respectively. In (b) for >100 keV, the simulated T0 flux falls below the y-axis (cf. Figure 9)



Figure 7. Figures demonstrating the correlation between the measured and calculated T0 precipitation for a. $L^* = 6$, 09-12 MLT and b. $L^* = 5$, 21-24 MLT as black crosses and blue triangles for the >30 keV and >100 keV channels respectively. The horizontal dashed line shows the noise threshold from our criteria.

fore result in our method (Equations 3-8) predicting low precipitating fluxes at these times. 372 Conversely, the bottom panel of Figure 6a shows, at times, the BAS diffusion coefficients 373 are approaching the strong diffusive limit from (Summers & Thorne, 2003) (shown by 374 red and yellow lines dashed lines for the 30 keV and 100 keV electrons respectively) for 375 $L^* = 7$, between 09-12 MLT. At these times, the T0 measurements are reaching the T90 376 measurements, suggesting the trapped and precipitating fluxes are comparable, as ex-377 pected during strong diffusion and demonstrated in Figure 3d by the yellow and red lines. 378 These results suggests we are getting better agreement between the calculated and mea-379 sured T0 precipitation during periods of strong diffusion, i.e when there is more flux in 380 the loss cone. 381



Figure 8. Figure showing the linear correlation between the precipitation calculated from the BAS-RBM diffusion coefficients and the precipitation measured by POES. The correlation is only shown where the confidence level is above 95%.

Figure 7a and b show scatter plots of the calculated and measured T0 precipita-382 tion for the two L*/MLT sectors presented in Figure 6. Figure 7a demonstrates our method 383 simulates the T0 measurements well in this L*/MLT sector, with most of the points ly-384 ing on or close to the x = y line for the >30 keV channel. For the >100 keV channel we 385 predominately underestimate the precipitating flux. Figure 7b shows we are consistently 386 underestimating the precipitation in the 21-24 MLT sector for both energy channels, with 387 a large spread in the calculated values. As discussed above, this is likely due to the low 388 values of the $\langle D_{\alpha\alpha} \rangle$ from the BAS model in this MLT sector which are causing an ex-389 ponential drop off in flux in the loss cone (see Figure 3b). Each plot gives the Pearson 390 Linear correlation coefficient (r) for the measured and calculated T0 precipitation and 391 also notes the number of data points (N) in each L*/MLT sector that meet our crite-392 ria for analysis. The correlation is higher in the 09-12 MLT sector compared to the 21-393 24 MLT sector for each energy channel and in both MLT sectors the correlation is higher 394 for the >30 keV channel than the >100 keV channel. 395

Figure 8 shows the global linear correlation (given by the colour) between the cal-396 culated T0 precipitation and that measured by the POES T0 >30 keV channel during 397 the event at three hour MLT and $0.5 L^*$ resolution between $L^* = 4$ -8. This is calculated 398 as demonstrated in Figures 6 and 7 but is only shown where the confidence level is above 399 95% (less than 0.05 significance). Overall, the results show higher correlation between 400 the measured and calculated precipitation on the dawnside than the duskside, although 401 we note that there are less statistically significant results on the duskside (this is due to 402 smaller correlations needing more data points to be statistically significant). We do not 403 show the results from the >100 kev channel as there are not enough data to make the 404 results statistically significant, however we see a similar pattern with higher correlations 405 on the dawnside at $L^* > 5$. Figure 8, demonstrates that we find the best agreement for 406 the >30 keV electrons between 06-12 MLT for $L^* > 5$ and between 03-06 MLT for L^* 407 from 4.5-6; this pattern is very similar to that seen for the chorus $\langle D_{\alpha\alpha} \rangle$ at 30 keV 408 shown in Figure 1. 409

Figure 9 shows the ratio of the calculated and measured T0 precipitation flux for 410 a range of MLT sectors and L-shells as a function of Kp^{*} (larger of the current Kp or 411 the Kp averaged over the last 12 hours). The best agreement between the measured and 412 calculated T0 flux occurs between 06-12 MLT at $L^*=5$ and 6 for the >30 keV channel. 413 There is a tendency for better agreement for higher Kp (particularly at $L^* = 5, 06-12$ MLT, 414 for both >30 keV and >100 keV), but it is not very strong. The measured flux is con-415 sistently higher than the calculated flux on the duskside (12-18 and 18-24 MLT sectors) 416 and at all MLT's at $L^* = 4$. The calculations also underestimate the precipitation at most 417 MLT's for the >100 keV channel. These underestimates are fairly consistent over all ge-418 omagnetic activity levels and the possible reasons are discussed in Section 5. 419

420

4.2 Loss cone reconstruction

As demonstrated by Figure 3, the steady state solutions from Kennel and Petschek (1966) (Equations 3 and 4) can be used to simulate the flux over the entire loss cone for different levels of pitch angle diffusion. In the above analysis we calculated the theoretical flux that would be measured inside the field of view of the POES T0 detector but as we can see from Figure 3, the T0 FOV does not cover the entire loss cone. Below we repeat our calculation shown in Equation 8 but now integrate over the entire loss cone,



Figure 9. Plot showing the ratio between the calculated and measured T0 precipitation as a function of Kp^{*} for a range of L^{*} and MLT sectors in black and blue for >30 keV and >100 keV channels. A dashed line is shown at y = 1 indicate perfect agreement between the model and the measurements and where the model is under (below the line) and over estimating the precipitation measured by POES (above the line).

$$J_{LC}(E > E_{th}) = \frac{2\pi \int_{E_{th}}^{E_{max}} \int_{0}^{\alpha_0} J_{eq}(E, \alpha_{eq}) \sin \alpha \, \mathrm{d}\alpha \, \mathrm{d}E}{2\pi \int_{0}^{\alpha_0} \sin \alpha \, \mathrm{d}\alpha},\tag{10}$$

427

where $J_{eq}(E, \alpha_{eq})$ is the flux calculated from Equation 4.

Figure 10 shows the ratio of the calculated flux measured by POES T0 (J_{calc} , from 428 Equations 3-8) and the total flux in the loss cone (J_{LC}) for the >30 keV electron chan-429 nel as a function of Kp^{*} at $L^* = 6, 6.5$ and 7 for 06-09 MLT (where we get good agree-430 ment between our analysis and the POES measurements, as demonstrated by Figure 8). 431 Figure 10 shows the ratio predominately varies between 1-10, with some higher ratio val-432 ues during low Kp^{*}; the second panel of Figure 10, for $L^* = 6.5$, there is one instance where 433 the ratio is almost 60 at $Kp^* = 1$. This suggests that the calculated T0 flux misses a higher 434 percentage of the precipitating flux during lower geomagnetic activity. Lines of best fit 435 are included on each panel showing that the ratio is decreasing with increasing Kp^{*}. This 436 relation is in agreement with previous studies who have tried to correct for the T0 FOV, 437 for example, Rodger et al. (2013). 438

439 5 Discussion

Bounce-averaged pitch angle diffusion coefficients from the BAS-RBM have been 440 used to calculate electron precipitation and compared to POES data. The results show 441 better agreement between the calculated and measured T0 flux for $L^* > 5$ between 06-442 12 MLT and $L^* = 4.5-6$ between 03-06 MLT for >30 keV electron precipitation (see Fig-443 ure 8). Indeed, the global distribution of the best correlation (Figure 8) closely resem-444 bles the global chorus $\langle D_{\alpha\alpha} \rangle$ at 30 keV shown in Figure 1, suggesting that chorus wave 445 are responsible for the bulk of the precipitation in these regions. We find better agree-446 ment between the calculated precipitating flux at >30 keV than at >100 keV for all lev-447 els of activity which suggests we may be missing a process which more efficiently scat-448 ters higher energy electrons. 449

We demonstrated a novel method to reconstruct the precipitation over the entire loss cone from the BAS-RBM diffusion coefficients, as demonstrated in Section 4.2. We found that the difference between the total calculated flux in the loss cone and the calculated flux in the T0 FOV varied predominately between 1-10 (see Figure 10); there are cases where the ratio is higher during low Kp. However we note that the largest disagreements between our calculated and the measured T0 flux are when geomagnetic con-

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Figure 10. Figure showing the ratio of the calculated precipitation over the entire loss cone and the calculated precipitation inside the T0 FOV at $L^* = 6$. 6.5, 7 between 06-09 MLT as a function of Kp^{*}. Lines of best fit are indicated in each panel by dashed lines.

ditions are at their quietest and therefore these high ratios may be a product of our method 456 underestimating the T0 flux. Our results are in agreement with those found by Nesse Tyssøy 457 et al. (2016); in their study they evaluate similar wave-particle interaction formulations 458 to those presented in this paper to construct the entire bounce loss cone, finding the ra-459 tio to be around 1 during active conditions and up to 10 during moderate geomagnetic 460 conditions. Our results are also consistent with Rodger et al. (2013) who found, by com-461 parison with riometer data in northern Finland, that during periods of high precipita-462 tion the riometer and POES observations agreed well but during quieter times, the POES 463 instruments were underestimating the flux by 7-9 times. The fact our results are con-464 sistent with previous work is promising for adopting this analysis, after further checks, 465 to account for the electron precipitation input currently missed by the POES T0 detec-466 tor (which has been used to quantify the precipitation in the CMIP6 data set). 467

There are times where the method presented in this paper underestimates the cal-468 culated T0 precipitating flux (e.g. at higher energies and on the duskside, see Figure 9), 469 suggesting that some additional diffusion is required in the BAS wave model. This low 470 loss rate could mean that the trapped flux in simulations run with the BAS-RBM may 471 be over-estimated. However, if the lack of precipitation is due, for example, to insuffi-472 cient chorus wave power then this means that acceleration due to chorus is also under-473 estimated, and hence the trapped flux would be underestimated. At this stage it is not 474 easy to say what the net effect on the BAS-RBM model output would be as it would de-475 pend on the time history of the event. 476

There are several reasons we might expect to see differences between the measured 477 and calculated T0 fluxes, including the fact we are using averaged wave models (described 478 in Section 2.1) which are unlikely to capture all of the variations of the wave power dur-479 ing this specific period. As pointed out by one referee, Figure 2 of Ripoll et al. (2017) 480 show the RBSP hiss activity during the event studied in this paper (26-30 March 2013), 481 in which the plasma density has successive narrow falls off, making this period quite com-482 plex. Using event specific conditions, Ripoll et al. (2019) calculated drift averaged dif-483 fusion coefficients for hiss waves of the order of $3 \times 10^{-4} \text{ s}^{-1}$ for 100 keV electrons around 484 L = 4.5- 5.5 during quiet times in March 2013. This is significantly higher than those 485 used in this study for 100 keV electrons at $L^* = 5$, shown in the bottom row of Figure 6b, 486 which could suggest we are underestimating the precipitation in this region due to un-487 derestimating the effects of hiss waves. As described in Section 2.1, the BAS diffusion 488

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coefficients are calculated using a modelled plasmapause and averaged values of f_{pe}/f_{ce} . 489 Figure 4 of Ripoll et al. (2017) shows observations of f_{pe}/f_{ce} during this event which in-490 dicate the plasmapause reaches up to L = 5.5 on the 26 March 2016 (perhaps further 491 as the plot is limited to L = 5.5). The yellow line in Figure 1 represents the modelled 492 plasmapause used in the calculation of the BAS diffusion coefficients, it is dashed be-493 tween 14-22 MLT to indicate more work is needed to determine the average location in 494 this region as it is possible it could extend out to larger L, as suggested by the obser-105 vations from Ripoll et al. (2017). These observations demonstrate how variable the con-496 ditions are and hence how difficult it is to match the POES observations when using dif-497 fusion coefficients calculated from averaged wave properties. However, event-driven pitch 498 angle diffusion coefficients are yet to be validated against observed precipitation, as is 499 presented in this paper. 500

Figure 3 demonstrates that when the diffusion coefficients are small, the steady state 501 solutions from Kennel and Petschek (1966) (Equations 3 and 4) will give an exponen-502 tial drop off in flux close to the outer boundary of the bounce loss cone, likely outside 503 the FOV of POES T0. Potential candidates for this missing contribution include hiss and 504 chorus waves (as discussed above), EMIC waves (e.g. Clilverd et al. (2015); Rodger et 505 al. (2015); Hendry et al. (2017, 2019); Denton et al. (2019)) and magnetosonic waves (Horne 506 et al., 2007). The best way to further explore this is by applying our method to more 507 events, a statistical study would be a particularly good test of the average wave model 508 and allow us to determine how much precipitation is driven by chorus waves. 509

The method we are applying to calculate the precipitation could also be a source 510 of error in our analysis. We previously noted that by using the equations from Kennel 511 and Petschek (1966), we are assuming steady state diffusion. This assumption has been 512 adopted and validated by other studies (e.g. Li et al. (2013); Nesse Tyssøy et al. (2016)) 513 however, it could lead to an underestimate in the flux if there is bursty rather than con-514 tinuous precipitation i.e. if we are not in a steady state. Furthermore, we take the T90 515 measurement as our source term which is converted to differential flux assuming a kappa 516 distribution. We can see from Equations 3 and 4 that increasing the source term would 517 directly increase the flux in the loss cone and therefore a problem with our source term 518 may account for some of our underestimation. The T90 data itself could result in our 519 method underestimating the precipitation as, although we exclude times when the field 520 of view is inside the bounce loss cone and when the POES crosses the longitude asso-521

ciated with the South Atlantic Anomaly, we have not accounted for times when it is mea-522 suring the drift loss cone (Rodger, Carson, et al., 2010). This could mean T90 is under-523 estimating the trapped flux which will result in our source term (and hence our precip-524 itation) being underestimated. Lastly, the assumptions used in the kappa distribution 525 could lead to some error in our calculated precipitation. Whittaker et al. (2013) found, 526 by comparison to DEMETER data (a similar pitch angle resolution instrument to POES 527 T90 but with better energy resolution), that a kappa distribution worked well to repro-528 duce the spectra of radiation belt electron losses for $\kappa > 2$. In this study, we have as-529 sumed $\kappa = 5$ following Li et al. (2013), if we were to decrease the value of κ it would 530 make our spectrum harder and perhaps improve our agreement for higher energies. All 531 of these potential issues with our method could be investigated further with more stud-532 ies. 533

534 6 Conclusions

We have tested the bounce averaged pitch angle diffusion coefficients from in the BAS radiation belt electron model by using them to calculate electron precipitation and comparing the results to measurements from POES. Our principle results are:

- 1. The agreement between the calculated flux and the POES data is much better on 538 the dawn and dayside than in the afternoon sector for $L^* > 5$. This agreement 539 is consistent with chorus being the dominant scattering mechanism in this MLT 540 and L-shell zone, and that chorus-driven scattering is well represented in the model. 541 2. We find better agreement between the calculated precipitating flux at >30 keV 542 than at >100 for all levels of activity. This suggests we may be missing a process, 543 or underestimating hiss wave effects, which more efficiently scatters higher energy 544 electrons; we may also be underestimating the source spectrum at higher energies. 545 3. Our results show that, due to the limited field of view, the total precipitating flux 546 can exceed that measured by POES by a factor that varies from 1 to 10, which 547 is in agreement with previous work. 548 4. While there is likely to be a large uncertainty between our calculated precipita-549
- tion and that measured by POES due to, for example, averaging of the wave data
 which are used to calculate the diffusion rates and the sampling of the data during the event in question, the calculated flux is consistently lower in some regions.

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This suggests that some additional diffusion is required to explain the flux at higher energies, and the flux on the dusk side. The effect of this underestimated loss suggests that the trapped flux simulated by the BAS-RBM might be over-estimated. However, more investigations are required before the net effect on the BAS-RBM output can be quantified. As noted in the Discussion the differences could also be due to the method, i.e. either the assumption of steady state or the value of kappa.

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