

**1 Characteristics of precipitating energetic electron
2 fluxes relative to the plasmopause during
3 geomagnetic storms**

Ian C. Whittaker,¹ Mark A. Clilverd,² Craig J. Rodger¹

Corresponding author: I. Whittaker, Department of Physics, University of Otago, PO Box 56,
Dunedin 9054, New Zealand. (ian.whittaker@otago.ac.nz)

¹Department of Physics, University of
Otago, Dunedin, New Zealand.

²British Antarctic Survey (NERC),
Cambridge, UK.

4 **Abstract.** In this study we investigate the link between precipitating electrons
5 from the Van Allen radiation belts and the dynamical plasmopause. We consider
6 electron precipitation observations from the POES satellite constellation during
7 geomagnetic storms. Superposed epoch analysis is performed on precipitating
8 electron observations for the 13 year period of 1999 to 2012 in two MLT sectors,
9 morning and afternoon. We assume the precipitation is due to wave particle
10 interactions and our two MLT sectors focus on chorus (outside the plasmopause)
11 and plasmapheric hiss (inside the plasmopause) waves. We generate simple
12 expressions based on the geomagnetic index, Dst, which reproduce the chorus-
13 driven observations for the >30 keV precipitating electron flux magnitudes.
14 Additionally, we find expressions for the fitted spectral index to describe the
15 flux variation with energy, allowing a full energy reproduction as a function
16 of distance from the plasmopause. The hiss-driven precipitating flux occurs
17 inside the plasmopause, but is independent of distance from the plasmopause.
18 In the POES observations the hiss induced electron precipitation is only detectable
19 above the instrument noise in the >300 keV and P6 (>800 keV) channels
20 of the flux detection instrument. We have derived expressions for the storm-
21 time variation in flux inside the plasmopause using Dst as a proxy. The observations
22 show there is little evidence for >800 keV electron precipitation occurring
23 outside of the plasmopause, in the MLT sectors studied.

1. Introduction

24 Energetic electron precipitation (EEP), which is strongest during geomagnetic storms,
25 is of great interest to radiation belt and atmospheric scientists. The particle energy
26 determines the altitude in the atmosphere at which the majority of its energy is deposited
27 [e.g., *Turunen et al.*, 2009, Fig.3]. Electrons with energies ~ 100 keV cause peak ionization
28 changes at ~ 80 km altitude while ~ 1 MeV electron energy peaks at ~ 62 km altitude.
29 This has major implications for atmospheric chemistry as precipitating charged particles
30 produce odd nitrogen (NO_x [*Newnham et al.*, 2011]) and odd hydrogen (HO_x [*Verronen*
31 *et al.*, 2011]) in the Earth's atmosphere. These odd particles can then catalytically destroy
32 ozone due to their longer lifetime at these altitudes [*Thorne*, 1977, 1980; *Solomon, Crutzen*
33 *and Roble*, 1982; *Brasseur and Solomon*, 2005; *Verronen et al.*, 2013] and have been linked
34 to variability in surface climate [*Seppälä et al.*, 2013]. In particular, *Andersson et al.*
35 [2012] reported experimental evidence of electron precipitation producing odd hydrogen
36 changes, during geomagnetic storms, stretching over the altitude range of ~ 52 to 82 km,
37 corresponding to electrons from ~ 100 keV to ~ 3 MeV. These authors recently showed that
38 atmospheric HO_x increases during geomagnetic storms at atmospheric locations under the
39 radiation belts [*Andersson et al.*, 2014].

40

41 In the radiation belts wave-particle interactions can cause pitch angle [*Lakhina et al.*,
42 2010] and energy [*Meredith et al.*, 2002] diffusion. For a recent review on wave-particle
43 interaction, see *Thorne* [2010]. In the VLF range one important type of wave is whistler-
44 mode chorus, while in the ULF range attention tends to focus on EMIC (ElectroMagnetic

45 Ion Cyclotron) waves [*Horne and Thorne, 1998*]. Chorus is observed in the frequency
46 range of a few hundred Hz to several kHz [*Helliwell, 1969*] and occurs in the morning
47 MLT region outside the plasmopause [*Summers, Thorne and Xiao, 1998*]. There have been
48 many studies which have linked chorus waves to intense energetic electron precipitation
49 [e.g. *Hikishima, Omura and Summers, 2010; Lam et al., 2010; Meredith et al., 2011*],
50 as expected from the strong wave amplitudes. Plasmaspheric hiss occurs in the inner
51 magnetosphere over a band between 100 Hz and 2 kHz [*Summers, et al., 2008*]. Hiss
52 induced electron precipitation has been shown to be responsible for the formation of
53 the slot region between the inner and outer radiation belts [*Lyons and Thorne, 1973*].
54 Long-lasting plasmaspheric hiss-driven precipitation has been monitored from the ground
55 [*Rodger et al., 2007*], and shown to be able to produce significant ozone depletions [*Rodger*
56 *et al., 2010a*].

57

58 It has long been recognized that there is a link between the dynamical plasmopause
59 location and the trapped fluxes in the outer radiation belt. Observations of relativistic
60 electrons from SAMPEX showed that over time periods of weeks to months the
61 plasmopause location was a good indication of the inner edge of the outer radiation
62 belt [*Li et al., 2006*]. This correlation demonstrates how differing wave activity inside and
63 outside the plasmopause strongly determines the long term variation in the trapped flux
64 magnitudes and location. The same study, however, demonstrated that this relationship
65 breaks down on shorter time periods. This is clearest for events where the plasmopause
66 moves inwards, allowing chorus to accelerate electrons to higher energies at comparatively
67 low L-shells, and then outwards, “stranding” this high energy population inside the

68 plasmopause. A particularly dramatic example of this is the recent reports of the “third
69 radiation belt” observed by the Van Allen probes [*Baker et al.*, 2013], and subsequently
70 successfully modeled [e.g. *Thorne et al.*, 2013a]. One should note this sort of dynamical
71 behavior is not uncommon, and can also lead to electron flux enhancements inside the
72 plasmopause at non-relativistic energies [*Lichtenberger et al.*, 2013]. There have also
73 been previous studies reporting links between the plasmopause location and relativistic
74 electron precipitation caused by chorus [e.g. *Johnston and Anderson*, 2010] and EMIC
75 waves [*Carson, Rodger and Clilverd*, 2013].

76
77 *Lam et al.* [2010] observed using the POES (Polar Orbiting Environmental Satellite)
78 >30 keV electron flux that the distribution of precipitating flux in this energy range was
79 well correlated with the global distribution of lower band chorus observed by CRRES
80 (Combined Release and Radiation Effects Satellite). More recent modeling showing the
81 high efficiency of chorus wave particle acceleration *Li et al.* [2013] agrees with this result
82 and was further confirmed with high resolution electron flux measurements from NASA’s
83 Van Allen probes [*Thorne et al.*, 2013b]. These observations showed that chorus waves
84 could explain all the observed energy and angular distribution of relativistic electron fluxes
85 in a particular case study.

86
87 The POES (Polar Orbiting Environmental Satellite) network of polar orbiting satellites
88 (formerly known as TIROS - Television and InfraRed Observation Satellite) are operated
89 by NOAA (National Oceanic and Atmospheric Administration). These satellites have
90 been running from NOAA-05 in 1978 up to the present in Sun-synchronous orbits at

91 varying Equatorial Crossing Times (ECT). EUMETSAT added the MetOp-02 satellite to
92 the POES network with the same particle instrumentation in May 2007. The MEPED
93 (Medium Energy Proton and Electron Detector) instrument is the focus of our study and
94 the data have been widely used in previous research on electron precipitation [e.g *Callis*,
95 1997; *Millan et al.*, 2010; *Carson, Rodger and Clilverd*, 2013]. The MEPED instrument is
96 an electron flux detector, which takes measurements at both 0° and 90° pitch angles for
97 3 integral energy ranges. A full description of the instrument is included in Section 2.1.
98 The main advantage of using this instrument for magnetospheric research comes from
99 the large datasets, which span more than two solar cycles with almost continuous data
100 coverage.

101

102 The goal of our study is undertake a superposed epoch analysis of precipitating electron
103 flux so that we can perform fitting techniques to provide an accurate empirical EEP model
104 during geomagnetic storm time. This model can then be used to give an approximate
105 precipitating electron flux inside and outside of the plasmopause due to chorus and
106 plasmaspheric hiss.

2. Data acquisition

107 To get an average of the electron fluxes around the plasmopause at different geomagnetic
108 conditions we use data collected from the long running POES satellite constellation.

2.1. POES electron flux instrument

109 The NOAA/POES MEPED sensor provides two kinds of particle count rate
110 measurements including two directional measurements of protons (0.03 to >6.9 MeV,

111 with 6 energy steps labeled P1 to P6) and electrons (0.03-2.5 MeV, in 3 energy ranges,
112 labeled E1 (>30 keV), E2 (>100 keV) and E3 (>300 keV)). There are two telescopes
113 sampling both protons and electrons pointing in different directions, each with a viewing
114 width of $\pm 15^\circ$. The 0° detector is directed along the Earth-spacecraft radial direction,
115 and the axis of the 90° detector is perpendicular to this (anti-parallel to the spacecraft
116 velocity vector). Modeling work has established that the 0° telescope monitors particles
117 in the atmospheric bounce loss cone that will enter the Earth's atmosphere below the
118 satellite when the spacecraft is poleward of $L \approx 1.5-1.6$, while the 90° telescope monitors
119 trapped fluxes or those in the drift loss cone, depending primarily upon the L shell [*Rodger*
120 *et al.*, 2010b, Appendix A].

121

122 The MEPED instrument has been updated as part of the SEM-2 subsystem and these
123 changes have been implemented from NOAA-15 to NOAA-19 and the MetOp-2 satellite.
124 For our study we consider only observations made using SEM-2, and hence only the
125 satellites listed above are considered. We use the equations given in *Lam et al.* [2010] to
126 convert from instrument counts to integral electron flux values with units of $\text{cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$.
127 The *Lam et al.* [2010] equations also remove proton contamination for periods observed
128 outside of the South Atlantic Magnetic Anomaly (SAMA) and solar proton events. A full
129 description of the SEM-2 system which includes the MEPED instrument can be found in
130 *Evans and Greer* [2004].

2.2. MLT and L shell data binning

131 The aim of this paper is to characterize energetic electron fluxes both inside and outside
132 of the plasmopause and to do this we sort our data by Magnetic Local Time (MLT).

133 Figure 1 is taken from *Summers, Ni and Meredith* [Figure 21, 2007], showing a schematic
134 of the plasmopause location including a drainage plume. The main areas of chorus wave
135 and plasmaspheric hiss activity are also shown, separated by the plasmopause. In this
136 study we have selected two MLT sectors to determine the effects of each wave type, and
137 to characterize the resultant electron precipitation occurring inside and outside of the
138 plasmopause. We identify the regions which are chorus-dominated as spanning 01:00-
139 08:00 MLT (morning) and hiss-dominated as spanning 11:00-16:00 MLT (afternoon).
140 These two regions are shaded in Figure 1 with the grey region showing the morning sector
141 (chorus wave dominated) and the purple region shows the afternoon sector (plasmaspheric
142 hiss dominated). We note that both chorus and hiss regions are more extensive than
143 investigated here, but we use focused regions to identify the main characteristics of the
144 whole region driven by each wave type.

145

146 The precipitating electron fluxes measured by the POES 0° pointing telescope between
147 1999 and 2012 are binned by both IGRF L shell and time with respective resolutions of
148 $0.2 L$ and 20 minutes for each MLT sector and integral energy range. Observations from
149 inside and around the SAMA are excluded before the measurements are combined. There
150 are 42 bins in L shell ranging from $L = 1.8$ to $L = 10.2$, when discussed in this study each
151 bin will be referred to by its central L shell value (e.g. the first bin is at $L = 1.9$). It should
152 be noted that the lowest L shell considered, $L = 1.8$, is larger than the minimum L shell
153 required to ensure that the 0° MEPED instrument is observing precipitating electrons
154 (Section 2.1). To maximize the quality and MLT range of the electron flux data, results

155 from all available POES satellites are combined and the median taken from the available
156 fluxes in each bin.

3. Determination of storm epochs

157 To create an average dataset of how electron precipitation varies during geomagnetic
158 storms and the gradual recovery to quiescent conditions, we undertake a superposed
159 epoch analysis for each MEPED energy channel and MLT sector around an identified
160 geomagnetic storm. To begin our investigation we create a superposed epoch dataset
161 ranging from 5 days before to 15 days after a geomagnetic storm allowing both quiet (pre
162 and post storm) and active (storm time) geomagnetic activity to be compared.

163

164 While Kp is commonly used in energetic electron studies [e.g., *Meredith et al.*, 2006;
165 *Whittaker et al.*, 2013], Dst is chosen as the geomagnetic index for this study as it is
166 continuous, rather than Kp which has specific discrete values (e.g. 0, 0.3, 0.7, etc),
167 *Simon-Wedlund et al.* [2014] also showed that Dst was a good proxy for EEP flux. Dst is
168 a measure of the energy density of the ring current measured at several equatorial stations
169 around the globe by determining differences in the horizontal component of the Earth's
170 magnetic field [*Sugiura*, 1964] and describes the magnetospheric response to the solar wind
171 *Gonzalez et al.* [1994]. These values are generally negative and we take a value of Dst
172 ≤ -50 nT as describing geomagnetic stormtime [*Borovsky and Denton*, 2006] with the local
173 minimum used as the epoch point [*Loewe and Prölss*, 1997]. To ensure that a storm only
174 counts once, an extra condition is applied to the Dst detection algorithm. We make sure
175 that each geomagnetic storm begins in a quiet magnetosphere by producing a “clean” list
176 of storms as described by *Katus et al.* [2013]. These authors require a 48 hour period with

177 Dst > -50 nT before any Dst minimum to ensure a list of well defined, isolated geomagnetic
178 storms. Previous work using DEMETER has shown that geomagnetic storms can affect
179 electron fluxes for longer time periods than this [Whittaker *et al.*, 2013] and so we extend
180 this pre-storm quiet period to 5 days. The total number of acceptable Dst storm epochs
181 identified during the 13 year time period was 164. The POES/MEPED proton data
182 were then checked during each storm event in order to remove any which include Solar
183 Proton Events (SPE). The POES/MEPED electron telescopes are sensitive to proton
184 contamination [Yando *et al.*, 2011] and while a previous study [Whittaker *et al.*, 2014] has
185 shown that the Lam *et al.* [2010] proton removal equations give a good approximation of
186 the true electron flux, the approach fails during solar proton events and inside the SAMA.
187 Hence, we remove any events which MEPED reports as having a differential proton flux
188 $>10 \text{ cm}^{-2}\text{sr}^{-1}\text{s}^{-1}\text{keV}^{-1}$ in the P5 channel (at an energy of 2.63 MeV) during any time
189 in the epoch. This SPE detection process removed 61 storms. The remaining 103 events
190 were then combined by taking the median flux within each 12 hour time bin and 0.2 L
191 shell bin. The superposed epoch analysis covers 20 days, beginning 5 days before Dst
192 minimum and giving 41 time bins, and is performed for 42 L bins, ranging from $L = 1.8$
193 to $L = 10.2$.

194
195 The left panel of Figure 2 shows the median Dst value taken from these 103 epochs at 12
196 hour intervals. There is a smooth variation in the Dst values which take approximately 7
197 days to return to quiet levels (-11 nT) after the storm peaks at zero epoch (median of -61
198 nT). We use the model Dst equation for the plasmopause location (L_{pp}) given in O'Brien
199 and Moldwin [2003]. We note from Table 1 of the O'Brien and Moldwin paper that using

200 the minimum of the 12 or 24 hour Dst value works equally well for the models, so we take
201 the minimum of the Dst in 12 hour resolution. The MLT dependent equation was initially
202 trialed with our dataset, producing L_{pp} values which were higher in L during the morning
203 MLT than during the afternoon MLT sector (consistent with moderate disturbance in
204 Figure 2 of *O'Brien and Moldwin* [2003]). This difference in L is opposite to what would
205 be expected as the model is unable to reproduce either plume structure or the dusk-side
206 bulge that would be expected from such a plume. To recreate the disturbed Dst L_{pp}
207 O'Brien and Moldwin use a Dst of \sim -300 nT, which is an unrealistic index for averaged
208 Dst values to reach. We therefore use the non-MLT plasmopause location equation for
209 this study. The right panels of Figure 2 show the E3 response for the morning and
210 afternoon MLT sectors. The main features of these panels are the precipitation due to
211 chorus (outside the plasmopause from Figure 1) at the epoch time ($t = 0$) and also
212 the precipitation due to plasmaspheric hiss (inside the plasmopause from Figure 1, t
213 = 2 to 7 days). The solid line in panels b) and c) is the O'Brien and Moldwin model
214 plasmopause for the Dst shown in panel a). This model plasmopause appears to bisect the
215 hiss precipitation leaving a significant amount outside the plasmopause. To compensate
216 for this we provide a constant addition to the model plasmopause within the error limits
217 defined by O'Brien and Moldwin ($\pm 1 L$). In panel b) we find that an addition of $0.5 L$
218 (dashed line) to the O'Brien and Moldwin L_{pp} values better enclose the hiss precipitation
219 and still leaves the chorus induced precipitation outside of the plasmopause. When we
220 perform the same shift for the afternoon MLT in panel c) we find that a constant addition
221 of $0.75 L$ performs better at separating the chorus and hiss induced precipitation. This
222 difference is consistent with the schematic shown in Figure 1 and illustrates the problem

223 with the MLT dependent plasmopause equations. We use the +0.5 L addition to the
224 O'Brien and Moldwin L_{pp} plasmopause model for our morning MLT analysis. As we
225 find no plasmopause relation for the hiss precipitation (only averaged Dst) the afternoon
226 plasmopause shift of +0.75 L is only shown for completeness.

4. EEP characteristics outside of the plasmopause

227 To determine electron precipitation occurring outside the plasmopause we investigate
228 the chorus dominated morning MLT sector of Figure 1 (01:00 - 08:00). Figure 3 shows
229 the variation in EEP fluxes around the storm epoch for all three channels of the MEPED
230 instrument in the morning MLT sector, >30 keV (top left panel), >100 keV (top right
231 panel) and >300 keV (lower left panel). A power law fit, previously shown to be the
232 best type of electron spectral fit to apply [*Whittaker et al.*, 2013], is applied to each L
233 shell and time bin across the three energies. The spectral index of this fit is shown in
234 the lower right panel of Figure 3. The chorus induced electron flux is observed outside
235 the plasmopause with the enhancement in flux lasting approximately 7 days. The hiss
236 induced precipitation can be seen clearly in the >300 keV channel inside the plasmopause.

237

238 The fitting of the flux in the three integral electron channels is performed by applying a
239 linear fit to the \log_{10} of the energy and flux values (Equation (1)), giving a power law fit
240 on linear axes (Equation (2)) as shown below. The fit spectral index is always negative
241 as we are fitting integral energy ranges (i.e., >100 keV channel has to have lower fluxes

242 than the >30 keV channel).

$$\log_{10}j = \gamma\log_{10}E + \log_{10}\alpha \quad (1)$$

$$j = \alpha E^\gamma \quad (2)$$

243 Where:

$$j = \text{integral flux at energy } E \text{ (cm}^{-2}\text{sr}^{-1}\text{s}^{-1}\text{)}$$

244

245 The previously described plasmopause location fits extremely well to the fluxes of all three
 246 energies, describing the boundary between high and low precipitating fluxes. To provide
 247 information on precipitating fluxes outside the plasmopause we provide two simulations;
 248 > 30 keV and the power law fit spectral index. The ability to reproduce both of these
 249 parameters will allow precipitating electron fluxes of any energy to be calculated relative
 250 to the plasmopause location as a geomagnetic storm progresses.

4.1. >30 keV simulation process

251 We begin by investigating the >30 keV superposed epoch (top left panel of Figure 3).
 252 The data shows that the highest precipitating fluxes are in the 12 hour bin around storm
 253 time, meaning that no delay between Dst and flux needs to be incorporated. This matching
 254 of peak electron flux to the Dst minimum indicates that the precipitation due to chorus
 255 wave interaction occurs within 6 hours of the main phase of the storm.

256

257 At each 12 hour time frame of the >30 keV data we plot the precipitating electron
 258 flux as a function of the distance from the plasmopause (S_{pp}) and apply a Gaussian fit in
 259 the form of $\text{Flux} = a.e^{-\left(\frac{S_{pp}-c}{w}\right)^2}$. These fits produced an average adjusted r^2 (r_{adj}^2) value

260 of 0.87 with the lowest correlations (~ 0.81) occurring at the maximum Dst plateau before
 261 the storm. The variables (a , c and w), which were different at each time frame, were then
 262 compared to the corresponding absolute Dst value and fitted with simple functions. The
 263 final equation for simulating the >30 keV is shown in Equation (3) providing flux with
 264 units of $\text{e}^- \text{cm}^{-2} \text{sr}^{-1} \text{s}^{-1}$.

$$\text{Flux}_{chorus} = a(|Dst|).e^{-\left(\frac{S_{pp}-c(|Dst|)}{w(|Dst|)}\right)^2} \quad (3)$$

265 where:

$$a(|Dst|) = 4.53|Dst|^{2.475}$$

$$c(|Dst|) = 3.11|Dst|^{-0.14}$$

$$w(|Dst|) = 1.59.e^{-0.061|Dst|} + 0.95$$

$$S_{pp} = \text{distance from the plasmopause (in } L)$$

266 The blue solid lines in the left panels of Figure 4 show time varying plots of the superposed
 267 epoch analyzed precipitating flux at 4 different distances from the plasmopause. These
 268 distances start at the plasmopause location and increase to $3 L$ outside the plasmopause.
 269 The black dashed lines in this figure show the average precipitating flux before the storm at
 270 each distance from the plasmopause, and it can be seen that the fluxes take approximately
 271 7 days to recover, on a similar timescale to Dst. Equation (3) was then tested by simulating
 272 the flux seen at each distance from the plasmopause and has been included as the red
 273 dashed line in the left panels of Figure 4, the simulation also has a minimum flux condition
 274 applied (to match the instrument noise) which is described in Section 4.3 and only affects
 275 the value at 12 hours before the storm. These model fluxes match very well to the lines
 276 representing observed flux outside the plasmopause (linear correlation coefficient > 0.95)

277 but less well at the plasmopause (linear correlation coefficient of 0.87), with root mean
 278 squared error (RMSE) values of 391 (L_{pp}), 2600 ($L_{pp} + 1$), 2589 ($L_{pp} + 2$) and 1180
 279 $\text{cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$ ($L_{pp} + 3$). A full simulation of Equation 4 is discussed in Section 4.3. We
 280 conclude that this equation performs adequately in modeling the >30 keV precipitating
 281 electron fluxes outside the plasmopause.

4.2. Flux spectral index simulation

282 We now investigate the electron flux spectral index (γ) for the varying geomagnetic
 283 conditions shown in the lower right panel of Figure 3. This is performed in a similar way
 284 to the >30 keV flux simulation in Section 4.1.

285
 286 The spectral index is compared to the distance from the plasmopause for each of the
 287 12 hour time bins. Unlike the >30 keV fitting, a single Gaussian fits poorly. This poor
 288 fit arises from a sharp change in spectral index at low L shells (e.g., $L = 3.1$ (-0.29) to L
 289 $= 4.3$ (-2.25)), at higher L the increase from minimum takes place over a larger L space
 290 (e.g., $L = 5.5$ (-2.89) to $L = 6.7$ (-2.13) over the same distance in L). Hence, a double
 291 Gaussian was required to accurately simulate the high L response. To be able to fit the
 292 coefficients of the double Gaussian as a function of Dst we had to include restrictions to
 293 the spectral index vs plasmopause distance fit. The first condition was to lock the centre
 294 of the first Gaussian to the minimum index value and the second condition was to make
 295 sure the centre of the second Gaussian was at a higher L value than the first centre. These
 296 conditions ensured a smooth shape and the ability to sensibly fit the coefficients to the
 297 absolute Dst value. The full equation is shown in Equation 4.

$$\gamma_{chorus} = a_1(|Dst|).e^{-\left(\frac{S_{pp}-c_1(|Dst|)}{w_1(|Dst|)}\right)^2} + a_2(|Dst|).e^{-\left(\frac{S_{pp}-c_2(|Dst|)}{w_2(|Dst|)}\right)^2} \quad (4)$$

298 where:

$$a_1(|Dst|) = -3.8 \times 10^4 |Dst|^2 - 0.0142 |Dst| - 0.12 \quad a_2(|Dst|) = 1.14.e^{-0.092|Dst|} - 1.4$$

$$w_1(|Dst|) = 6.123|Dst|^{-0.34} \quad w_2(|Dst|) = 3.66$$

$$c_1(|Dst|) = -0.0126|Dst| + 2.074 \quad c_2(|Dst|) = 0.03|Dst| + 2.6$$

S_{pp} = distance from the plasmopause (in L)

299 The right panels of Figure 4 show the observed (solid blue) and simulated (dashed
 300 red) spectral index for 4 distances from the plasmopause in a similar style to the left
 301 hand panels. The thin dashed black line indicates the average spectral index before the
 302 storm. The minimum in spectral index again occurs in the 12 hours around the Dst
 303 minimum, with a similar 7 day recovery time. The spectral indices calculated from
 304 Equation (4) again show an excellent fit outside the plasmopause with +1 and +2 L from
 305 the plasmopause having linear correlation coefficients > 0.9 (RMSE values are 0.231 and
 306 0.129 respectively). The simulation of the spectral index at +3 L slightly overestimates
 307 the data with a linear correlation coefficient of 0.87 (RMSE = 0.254). The simulation at
 308 the plasmopause again overestimates the data with the day before the storm particularly
 309 different from the data. The linear correlation coefficient for this plot is 0.64 (RMSE
 310 = 0.346). A full simulation of Equation (4) is discussed in Section 4.3. We conclude
 311 this equation performs adequately in modeling the spectral index of precipitating electron
 312 fluxes outside the plasmopause.

4.3. Model confidence

313 Examination of Figure 4 shows very clearly that the equations do an excellent job of
 314 reproducing the fluxes and spectral index outside the plasmopause. Taking 1 L outside

315 the plasmopause as an example, the average >30 keV flux difference between the model
316 and observations is $2600 \text{ cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$ with an interquartile range of 691, giving a range of
317 between 2×10^3 and 3×10^3 (this average value is 2.3% of the storm time flux). This range
318 is approximately equal to the average flux during quiet geomagnetic conditions (shown by
319 the dashed black line). Performing a similar analysis for the spectral index at 1 L outside
320 the plasmopause gives a mean absolute difference of 0.23 with an interquartile range of 0.2,
321 resulting in an error up to a maximum of 0.43, which is small compared to the data values.

322

323 As a more complete test of these equations, the >30 keV and spectral index epoch panels
324 from Figure 3 are recreated using Equations (3) and (4). These are shown in Figure 5
325 with the >30 keV flux variation shown in the left panels, and the spectral index variation
326 shown in the right panels. When we consider the >30 keV flux epoch, the simulation
327 (middle left panel) looks very similar to the data (top left panel). The biggest source of
328 difference exists in the quiet period before the storm, where the simulation reports fluxes
329 close to zero and the data gives a maximum flux around $10^3 \text{ cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$. There is a
330 background flux in the data which appears to be L shell dependent and we can replicate
331 this by determining the minimum flux value at each L shell and fitting a function to it
332 (shown below in Equation 5). This extra background is unlikely to be representative of
333 the true precipitating flux and is more likely to be the result of instrument noise and is
334 only used when comparing to the MEPED instrument fluxes. The simulation with this
335 minimum flux condition applied is shown in the bottom left panel of Figure 5 and looks
336 extremely similar to the data in the top left panel. An analysis of the difference in data
337 points shows that on average the data is higher than the simulation by less than a factor

338 of 2 (1.73). It should be noted that the biggest errors are at the very high L shell values
 339 ($L > 8$).

$$\text{Minimum Flux} = 789.e^{-\left(\frac{L-7.7}{1.9}\right)^2} + 100 \quad (5)$$

340 When we apply the same analysis of Figure 5 to the spectral index simulation (middle
 341 right panel) and data (upper right panel) we again see strong similarities between the
 342 two. The largest difference between data and simulation is again the day before the
 343 storm and at high L values ($L > 9$). A similar maximum spectral index as a function
 344 of L shell is calculated and applied (shown in the lower right panel of Figure 5). The
 345 difference between the plots is negligible and the only effect is at the 24 hour period
 346 before the storm. We therefore base our comparison between simulation and data using
 347 Equation (4) only. The spectral index simulation overestimates the data by a factor of 1.4
 348 on average, this is mostly due to the high L values and the 24 hours on the eve of the storm.

349
 350 The simulations in Figure 5 also show that at the highest L shells, the simulations do not
 351 seem to represent the epoch very well. We therefore advise that the model equations are
 352 not used beyond $L = 8.5$, corresponding to approximately 3 L outside the geomagnetically
 353 quiet plasmopause.

5. EEP characteristics inside the plasmopause

354 To determine electron precipitation occurring inside the plasmopause we investigate the
 355 plasmaspheric hiss dominated MLT sector (11:00 - 16:00). Figure 6 shows the electron
 356 precipitation variation after a superposed epoch analysis for all three channels of the
 357 MEPED instrument, >30 keV (top left panel), >100 keV (top right panel) and >300 keV
 358 (lower left panel) in a similar manner to Figure 3 and using the same color scales. In

359 comparison to Figure 3 the fluxes outside the plasmopause in the afternoon MLT sector
360 are lower in magnitude. This weaker chorus is a result of insufficient electron flux and
361 anisotropy to drive chorus generation past 15:00 MLT [*Bortnik, Thorne and Meredith,*
362 2007], with a significant weakening of the chorus past noon as seen in Figure 1. The >300
363 keV electron fluxes inside the plasmopause are higher than observed in the morning MLT
364 sector, this indicates that our chosen MLT sectors are behaving as expected.

5.1. Energetic distribution of hiss induced precipitation

365 In Figure 3 the energy spectra of the chorus induced electron precipitation is easily
366 observed. However, this is more difficult inside the plasmopause for the afternoon MLT
367 sector. Examination of Figure 6 shows that the center of the >300 keV channel flux
368 distribution occurs in the bin 84 hours (± 6 hours) after the main phase of the storm
369 at $L = 4.1$. This flux enhancement is very difficult to see in the other integral energy
370 channels even with a narrow color table range indicating there is a lack of any obvious
371 flux enhancement inside the plasmopause in the >30 keV and >100 keV energy channels
372 at this specific time. The >100 keV channel shows some small precipitation enhancement
373 approximately 36 to 72 hours from the main phase of the storm peaking at an L shell
374 of 4.5. There is no visible effect in the >30 keV channel. This is consistent with the
375 results from *Summers, et al.* [2008] stating that electron loss due to pitch angle scattering
376 from plasmaspheric hiss is energy dependent. The typical precipitation time given by
377 these authors states that 100 to 200 keV electrons are lost in approximately one day.
378 For the >30 keV channel this suggests the losses happen much faster and are probably
379 hidden in our observations by the 12 hour time resolution, with the main hiss induced loss
380 happening at the epoch time and visually lost amongst the chorus induced precipitation.

381

382 As a further test of these results we investigate the P6 proton channel on the MEPED
383 instrument. The geometric factor related to this high energy proton telescope (>6.9 MeV
384 protons) indicates that it functions very well as a relativistic electron detector when such
385 protons are not present [Yando *et al.*, 2011]. It should be noted that there are no high
386 energy protons present in our analysis as we have removed such epochs as part of our SPE
387 removal. The superposed epoch analysis of this telescope in the afternoon MLT sector is
388 shown in the lower right panel of Figure 6 with the same \log_{10} color scale as the >300 keV
389 channel. The main precipitating flux can be seen at approximately 120 hours from the
390 main phase of the storm with a narrower L shell profile and centered at a lower L shell (L
391 $= 4.2$) than the >300 keV precipitation. The energy of this channel has been determined
392 in previous studies as approximately >800 keV [e.g. Carson, Rodger and Clilverd, 2013;
393 Rodger *et al.*, 2010b], as this is when the geometric factor for the electrons in this channel
394 is greater than 10^{-3} cm^2 sr. We can also make an estimate of the upper energy limit.
395 From the geometric factors given in Yando *et al.* [2011], the P6 channel would respond
396 more strongly than the >300 keV for electrons above 1.4 MeV. Thus, as the fluxes in the
397 P6 channel are lower than the >300 keV channel from Figure 6, we can assume the energy
398 of a high proportion of precipitating electrons detected in the P6 channel are between 0.8
399 and 1.4 MeV.

400

401 An interesting point of note is that there is no evidence of chorus induced precipitation in
402 the P6 observations. The morning MLT superposed epoch analysis was also investigated
403 and showed the same lack of precipitating flux outside the plasmopause. Horne, Lam

404 *and Green* [2009] showed that electrons with energies >1 MeV are not precipitated but
 405 scattered into the drift loss cone and lost around the SAMA. As we have removed the
 406 SAMA geographical location from our superposed epoch analysis then it is consistent that
 407 we see no precipitating flux with energy greater than 800 keV outside the plasmopause.

5.2. Hiss induced EEP simulation (>300 keV)

408 We now proceed to simulate the fluxes inside the plasmopause. From our observations
 409 we can only simulate the >300 and >800 keV (P6) channels and we begin with the >300
 410 keV observations.

411
 412 The method used to characterize the chorus induced >30 keV precipitation and spectral
 413 index can not be used in this case as it is clear that the flux inside the plasmopause does
 414 not follow the Dst value directly, (i.e., there is no sharp cut off between pre and post
 415 storm). Providing a delay in the Dst does not assist the analysis due to the rapid change
 416 in plasmopause location and gradual change in >300 keV flux. However, by taking an
 417 average of $|\text{Dst}|$ over the previous 84 hours provides an index that gradually increases to
 418 maximum and then gradually returns to background levels, in a similar manner to the
 419 >300 keV flux inside the plasmopause. We also observed that the distribution of flux does
 420 not appear to change in L shell. Our method of simulation is then to take rows of the
 421 data array corresponding to L shell, fitting them to the averaged $|\text{Dst}|$ value described
 422 above. The fit appears to follow a power law with a constant gradient value of 0.055.
 423 The amplitude is fitted to L with a Gaussian and the full equation providing >300 keV
 424 electron flux with units of $\text{cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$, is shown below in Equation (6).

$$\text{Flux}_{\text{hiss}>300} = a(L)|\overline{\text{Dst}}_{-84:0}|^{0.055} \quad (6)$$

425 where:

$$a(L) = 128e^{-\left(\frac{L-4.5}{3.2}\right)^2}$$

426 A selection of the >300 keV flux lines can be seen in panels a) to d) of Figure 7 as the solid
 427 blue line. The fluxes are taken at $L = 3.9$ (panel a), $L = 4.5$ (panel b), $L = 4.9$ (panel c)
 428 and $L = 5.3$ (panel d). The dashed red line on each panel is the simulation calculated from
 429 Equation (6) at each L . It should be noted that panels b) to d) strongly underestimate
 430 the observations at the zero epoch. This is intentional as these L shells have precipitation
 431 induced from chorus waves at this time which we do not wish to include. If we ignore the
 432 zero epoch time, the largest difference between the simulation and data in these panels
 433 is $\sim 10 \text{ cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$, this occurs at the minimum flux value ($L = 4.9$, $t = +12$ days) and
 434 contributes 8% of this flux.

435
 436 Panel e) of Figure 7 shows the >300 keV epoch from Figure 6 on a linear color scale,
 437 with the plasmopause shown as the black dashed line. We then use Equation (6) to
 438 attempt to replicate panel e). The simulation is shown in panel f) utilizing the same
 439 color scale. Using the 84 hour averaged Dst gives a simulation which appears to agree
 440 well by eye. We compare the simulation and the observed data between $2.5 \leq L \leq 5.9$
 441 and between $-1.5 \text{ days} \leq t \leq +15 \text{ days}$ with the 12 hour zero epoch removed. The mean
 442 absolute difference between these arrays is $6.2 \text{ cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$ which is 4% of the average
 443 flux in this region ($137 \text{ cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$) and 16% of the range between the minimum (120
 444 $\text{cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$) and maximum ($158 \text{ cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$) flux.

5.3. Hiss induced EEP simulation (>800 keV)

445 As we have simulated the >300 keV channel we now move onto a simulation of the >800
 446 keV (P6) channel. The superposed epoch of the >800 keV channel in Figure 6 (lower right
 447 panel) is visually very similar to the >300 keV superposed epoch (lower left panel). The
 448 main differences between them are the L shell range of precipitating electrons and the
 449 time lag with respect to average Dst, as previously mentioned. We therefore apply the
 450 same simulation technique as used for the >300 keV electron channel (Section 5.2) to the
 451 P6 observations.

452

453 The superposed epoch of the >800 keV precipitating electrons is reproduced in panel
 454 (g) of Figure 7 shown using a linear color scale. The superposed epoch analysis flux value
 455 at each 0.2 L shell between $L = 3.3$ and $L = 5.5$ is taken and compared to the mean Dst
 456 value from 5 days to 1 day previously. The data was tested using the 5 day Dst mean
 457 and the fitting did not perform as well as the 4 day average Dst with a 24 hour delay.
 458 The fitting equation produced is in the same form as Equation (6), with the same power
 459 index value of 0.055 used. The amplitude of the power fit is then calculated with a fitted
 460 Gaussian and the coefficients are given below in Equation (7).

$$\text{Flux}_{\text{hiss}>800} = a(L) |\overline{\text{Dst}}_{-120:-24}|^{0.055} \quad (7)$$

461 where:

$$f(L) = 114e^{-\left(\frac{L-4.2}{2.8}\right)^2}$$

462 The simulation of the time variation of the P6 fluxes is shown in panel h) of Figure 7 and
 463 on the same color scale as the superposed epoch analysis observations in panel g). When
 464 we compare the differences between the observations and the simulation ($2.9 \leq L \leq 5.5$,

465 $t \geq 0$), we find that the mean difference (using absolute values) is $3.3 \text{ cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$ which
 466 is 2.8% of the average flux in this region ($122 \text{ cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$) and 8% of the range between
 467 the minimum ($100 \text{ cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$) and maximum ($143 \text{ cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$) flux.

6. Discussion

468 We now have a complete model description of the POES observed electron fluxes outside
 469 and inside the plasmopause due to chorus and plasmaspheric hiss. As a confirmation
 470 of our results we investigate the DEMETER (Detection of Electro-Magnetic Emissions
 471 Transmitted from Earthquake Regions) ICE (Instrument Champ Electrique) instrument
 472 observations to determine the wave activity in the lower chorus band using our superposed
 473 epoch analysis. The ICE instrument performs a continuous survey of a wide range of DC
 474 and AC electric fields with a high sensitivity and a 1 second temporal resolution. A
 475 full description of the instrument can be found in *Berthelier et al.* [2006]. A previous
 476 study [*Hayosh et al.*, 2013] has linked electron precipitation to chorus wave activity using
 477 ICE and POES data in two case studies. Panel a) of Figure 8 shows a superposed
 478 epoch analysis using the same epochs as we used for the POES analysis, but limited to
 479 those which occurred in the DEMETER satellite lifetime of 2006-2011. The limitation of
 480 requiring an isolated storm means that the epochs within this time period (around solar
 481 minimum) are limited to 16 events. The model plasmopause, as calculated in Section 3
 482 for the morning MLT, is included as the dashed line on this plot. The color scale indicates
 483 the variation in the power of lower band chorus waves. This plot shows that the chorus
 484 wave activity peaks at storm time and is largely contained outside of the plasmopause.
 485 This confirms that strong chorus wave activity is present during the main period when the
 486 electron precipitation is enhanced. Note also that there is enhanced wave power inside the

487 plasmopause for some days after the storm time zero epoch. This is likely to be caused
488 by plasmaspheric hiss, which can overlap the frequency band of lower-band chorus in that
489 L shell range. The modeling study of *Chen et al.* [2012] showed that this hiss response
490 is likely formed by chorus emissions originating at low L during the inward movement of
491 plasmopause location.

492

493 To visually show the difference in electron flux enhancement effects between chorus and
494 hiss we plot both observations together with the Dst value. Panel b) of Figure 8 shows
495 the peak electron flux for each wave type (>30 keV for chorus and >300 keV for hiss).
496 The chorus precipitating flux is shown as the blue solid line with circles, occurs at $L = 5.5$
497 and has a peak electron flux of $1.24 \times 10^5 \text{ cm}^{-2} \text{sr}^{-1} \text{s}^{-1}$. The peak hiss precipitating flux
498 occurs at $L = 4.5$ and is shown by the green solid line with x markers, the maximum flux
499 at this L shell is $158 \text{ cm}^{-2} \text{sr}^{-1} \text{s}^{-1}$. The Dst value is also shown as the black dashed line for
500 comparison. The relative difference in precipitating electron enhancements is very clear
501 in this figure with the chorus having an effect over three orders of magnitude larger than
502 hiss. This is an expected result as the average population of >30 keV electrons is much
503 larger than the average population of >300 keV electrons. A comparison of the strength
504 of the effects of chorus and hiss can be found by comparing the peak >300 keV flux
505 inside and outside of the plasmopause. The peak flux outside of the plasmopause for the
506 >300 keV morning MLT precipitating electrons is $187 \text{ cm}^{-2} \text{sr}^{-1} \text{s}^{-1}$ and the peak inside the
507 plasmopause is $158 \text{ cm}^{-2} \text{sr}^{-1} \text{s}^{-1}$. When we consider these fluxes as enhancements from the
508 background flux value ($100 \text{ cm}^{-2} \text{sr}^{-1} \text{s}^{-1}$) we find that the chorus induced enhancement has
509 an effect approximately 1.5 times stronger than the hiss induced enhancement. Evidently

510 this is only true for high energy electrons, as fluxes that are a factor of $\frac{2}{3}$ of the peak
511 chorus induced flux inside the plasmasphere would be clearly visible in Figures 3 and 6 at
512 lower energies. Panel c) of Figure 8 shows just the hiss peak flux on a much reduced and
513 linear y-axis range. The Dst delay effect can be clearly seen as well as the small chorus
514 contamination effect at the time of the storm. The purple dashed line with + markers in
515 this plot represents the previous 3.5 day mean Dst, to show the similarity between this
516 index and the flux.

517

518 The P6 channel (>800 keV) in the afternoon MLT epoch shows a flux drop out at storm
519 onset. This is commonly seen in high energy electron fluxes during geomagnetic activity
520 and is a result of radial outward transport of electrons through the magnetopause [*Turner*
521 *et al.*, 2012]. The flux then returns strongly around L shells of 3.5 to 5.5, this matches
522 well with the observations seen in *Horne et al.* [2005]. However, the work by these
523 authors attributed the high energy relativistic flux to chorus acceleration just outside the
524 plasmapause, increasing the flux by an order of magnitude approximately 24 hours later.
525 We attribute our observed precipitation (with an approximate 10% increase from quiet
526 time) to plasmaspheric hiss which peaks in wave power at $L = 4.4$ [*Li et al.*, 2014].

527

528 Our epochs have been created using the 1 hour median Dst value from each event in
529 the statistical model we have created, this means that our equations have not included
530 any positive Dst values. When used for comparison in case studies this is important as
531 the effects of $Dst > 0$ on the model are unknown. This is especially true in the case of

532 the >30 keV flux which uses the absolute value of Dst and hence a positive Dst would
533 increase the model precipitation level, rather than reduce it as would be expected.

7. Conclusions

534 We have performed a superposed epoch analysis of precipitating electron flux taken from
535 the POES/MEPED instrument. The epoch has been based on the minimum value of Dst
536 during a geomagnetic storm, taken when Dst drops below -50 nT with a previous 5 day
537 quiet period. Our results have been split into two MLT regions to focus upon the different
538 enhancement effects of chorus and plasmaspheric hiss waves on the electron precipitation.
539 From our superposed epoch analysis we have shown that for the morning MLT sector, the
540 precipitating electron fluxes outside the plasmopause are greatly enhanced during storm
541 time with this flux correlating strongly with the Dst value and distance from the modeled
542 plasmopause location. In contrast, the noon/afternoon MLT sector shows time varying
543 precipitating electron flux inside the plasmopause dependent upon electron energy. The
544 >300 keV channel precipitation peak occurs 84 hours after the minimum Dst value, while
545 the relativistic electron (>800 keV) precipitation peak occurs 120 hours after the main
546 phase of the storm. Neither hiss induced precipitation profile is dependent upon the
547 plasmopause position.

548
549 By taking electron flux values as a function of distance from the modeled plasmopause,
550 we have produced a model description of the enhancements in flux for the morning MLT
551 sector associated with chorus wave interaction. The >30 keV electron flux model is given
552 in Equation 3, along with the modeled power law fit spectral index response in Equation 4.
553 The combination of these two equations allows us to model the full precipitating electron

554 energy response during a geomagnetic storm outside the plasmopause, valid up to $L = 8.5$.
555 We have also observed that electrons >800 keV are very unlikely to precipitate outside
556 the plasmopause within our MLT sectors and L shell ranges.

557

558 The electron flux enhancements inside the plasmopause in the afternoon MLT sector,
559 associated with plasmaspheric hiss, have been modeled for electrons with energies above
560 300 keV. The >300 keV model, shown in Equation 6, depends on the L shell and operates
561 on a mean of the Dst values over the previous 3.5 days (inclusive of the current time
562 bin). The simulation of the P6 channel fluxes (Equation (7)) also depend on L shell and
563 relies on a mean 96 hour Dst value with a 1 day lag, both consistent with the results of
564 *Summers, et al.* [2008].

565

566 The models we have produced can be used to estimate precipitating electron
567 fluxes based on real time estimates of Dst and plasmopause location. The
568 European Union FP7 funded project PLASMON, intends to assimilate near real time
569 measurements of plasmaspheric densities into a dynamic plasmasphere model using
570 whistler waves detected by a VLF ground network (e.g. <http://plasmon.elte.hu/>,
571 *Collier et al.* [2011], *Lichtenberger et al.* [2013]). This project complements our
572 EEP precipitation model equations providing values which can be compared both to
573 satellite measurements (POES, DEMETER and the more recent Radiation Belt Storm
574 Probes missions) and ground based VLF perturbations (e.g. AARDDVARK network,
575 http://www.physics.otago.ac.nz/space/AARDDVARK_homepage.htm). The combination

576 of the plasmapheric results from PLASMON and our model will allow a near real-time
577 estimate to be made of precipitating energetic electron fluxes.

578 **Acknowledgments.** The research leading to these results has received funding from
579 the European Community's Seventh Framework Programme ([FP7/2007-2013]) under
580 grant agreement number 263218. The authors wish to thank the NOAA personnel who
581 developed, maintain, and operate the NOAA/POES spacecraft. The data used in this
582 paper are available at NOAA's National Geophysical Data Center (NGDC - NOAA 15-19
583 and MetOp-02 MEPED data).

References

- 584 Andersson, M., P. T. Verronen, S. Wang, C. J. Rodger, M. A. Clilverd, and B. R. Carson
585 (2012), Precipitating radiation belt electrons and enhancements of mesospheric hydroxyl
586 during 20042009., *J. Geophys. Res.*, *117*(D09304), doi:10.1029/2011JD017246.
- 587 Andersson, M., P. T. Verronen, C. J. Rodger, M. A. Clilverd, and S. Wang (2014),
588 Longitudinal hot-spots in the mesospheric OH variations due to energetic electron
589 precipitation, *Atmos. Chem. Phys.*, *4*, doi:10.5194/acp-14-1095-2014.
- 590 Baker D. N., S. G. Kanekal, V. C. Hoxie, M. G. Henderson, X. Li, H. E. Spence,
591 S. R. Elkington, R. H. W. Friedel, J. Goldstein, M. K. Hudson, G. D. Reeves, R.
592 M. Thorne, C. A. Kletzing, S. G. Claudepierre (2013), A Long-Lived Relativistic
593 Electron Storage Ring Embedded in Earths Outer Van Allen Belt, *Science*, *340*(6129),
594 doi:10.1016/science.1233518.
- 595 Berthelier, J. J., M. Godefroy, F. Leblanc, M. Malingre, M. Menvielle, D. Lagoutte, J.Y.
596 Brochot, F. Colin, F. Elie, C. Legendre, P. Zamora, D. Benoist, Y. Chapuis, J. Artru,

- 597 and R. Pfaff (2006), ICE, the electric field experiment on DEMETER, *PSS*, 54(5),
598 doi:10.1016/j.pss.2005.10.016.
- 599 Borovsky, J. E., and M. H. Denton (2006), Differences between CME driven storms and
600 CIR driven storms, *J. Geophys. Res.*, 111, A07S08, doi:10.1029/2005JA011447.
- 601 Bortnik, J., R. M. Thorne, and N. P. Meredith (2007), Modeling the propagation
602 characteristics of chorus using CRRES suprathermal electron fluxes, *J. Geophys. Res.*,
603 112, doi:10.1029/2006JA012237.
- 604 Brasseur, G., and S. Solomon (2005), *Aeronomy of the Middle Atmosphere, third ed.*, D.
605 Reidel Publishing Company, Dordrecht.
- 606 Callis, L. B. (1997), Odd nitrogen formed by energetic electron precipitation as calculated
607 from TIROS data, *Geophys. Res. Lett.*, 24(24), doi:10.1029/97GL03276
- 608 Carson, B., C. J. Rodger and M. A. Clilverd (2013), POES satellite observations of EMIC-
609 wave driven relativistic electron precipitation during 1998-2010, *J. Geophys. Res.*, 118,
610 doi:10.1029/2012JA017998.
- 611 Chen, L., J. Bortnik, W. Li, R. M. Thorne and R. B. Horne (2012), Modeling the properties
612 of plasmaspheric hiss: 1. Dependence on chorus wave emission, *J. Geophys. Res.*, 117,
613 doi:10.1029/2011JA017201.
- 614 Collier, A. B., J. Lichtenberger, M. Clilverd, B. Heilig, M. Vellante, J. Manninen, C. J.
615 Rodger, A. Jorgensen, J. Reda, R. Holzworth, R. Friedel, (2011), PLASMON: Data
616 assimilation of the Earth's plasmasphere, *General Assembly and Scientific Symposium*,
617 2011 XXXth URSI, 13-20 Aug. 2011, doi:10.1109/URSIGASS.2011.6051134.
- 618 Evans, D. S., and M. S. Greer (2004), Polar orbit environmental space satellite space
619 environment monitor 2: Instrument description and archived data documentation v1.3,

620 *NOAA Technical Memorandum, Space Environ. Lab., Boulder, Colorado*

621 Gonzalez, W. D., J. A. Joselyn, Y. Kamide, H. W. Kroehl, G. Rostoker, B. T. Tsurutani
622 and V. M. Vasyliunas (1994), What is a Geomagnetic Storm?, *J. Geophys. Res.*, *99*,
623 doi:10.1029/93JA02867.

624 Hayosh M., D. L. Pasmanik, A. G. Demekhov, O. Santolik, M. Parrot and E. E. Titova
625 (2013), Simultaneous observations of quasi-periodic ELF/VLF wave emissions and
626 electron precipitation by DEMETER satellite: A case study, *J. Geophys. Res.*, *118*,
627 doi:10.1029/jgra.50179.

628 Helliwell R. A. (1969), Low-frequency waves in the magnetosphere, *Rev. Geophys.*, *7*,
629 doi:10.1029/RG007i001p00281.

630 Hikishima, M., Y. Omura and D. Summers (2010), Microburst precipitation of
631 energetic electrons associated with chorus wave generation, *Geophys. Res. Lett.*, *37*,
632 doi:10.1029/2010GL042678.

633 Horne, R. B., and R. M. Thorne (1998), Potential waves for relativistic electron
634 scattering and stochastic acceleration during magnetic storms, *Geophys. Res. Lett.*, *25*,
635 doi:10.1029/98GL01002.

636 Horne, R. B., R. M. Thorne, S. A. Glauert, J. M. Albert, N. P. Meridith, and R. R.
637 Anderson (2005), Timescales for radiation belt electron acceleration by whistler mode
638 chorus waves, *J. Geophys. Res.*, *110*, doi:10.1029/2004JA010811.

639 Horne, R. B., M. M. Lam and J. C. Green (2009), Energetic electron precipitation
640 from the outer radiation belt during geomagnetic storms, *Geophys. Res. Lett.*, *36*,
641 doi:10.1029/2009GL040236.

- 642 Johnston, W. R. and P. C. Anderson (2010), Storm time occurrence of relativistic
643 electron microbursts in relation to the plasmopause, *J. Geophys. Res.*, *115*(A02205),
644 doi:10.1029/2009JA014328.
- 645 Katus, R., M. W. Liemohn, D. L. Gallagher, A. Ridley, and S. Zou (2013), Evidence for
646 potential and inductive convection during intense geomagnetic events using normalized
647 superposed epoch analysis., *J. Geophys. Res.*, *118*, doi:10.1029/2012JA017915.
- 648 Lam M. M., R. B. Horne, N. P. Meredith, S. A. Glauert, T. Moffat-Griffin and J. C.
649 Green (2010), Origin of energetic electron precipitation >30 keV into the atmosphere.,
650 *J. Geophys. Res.*, *115*(A00F08), doi:10.1029/2009JA014619.
- 651 Lakhina G. S., B. T. Tsurutani, O. P. Verkhoglyadova and J. S. Pickett (2010), Pitch
652 angle transport of electrons due to cyclotron interactions with the coherent chorus
653 subelements, *J. Geophys. Res.*, *115*(A00F15), doi:10.1029/2009JA014885.
- 654 Li, X., D. N. Baker, T. P. O'Brien, L. Xie, and Q. G. Zong (2006), Correlation between
655 the inner edge of outer radiation belt electrons and the innermost plasmopause location,
656 *Geophys. Res. Lett.*, *33*(L14107), doi:10.1029/2006GL026294.
- 657 Li, W., B. Ni, R. M. Thorne, J. Bortnik, J. C. Green, C. A. Kletzing, W. S. Kurth and G.
658 B. Hospodarsky (2013), Constructing the global distribution of chorus wave intensity
659 using measurements of electrons by the POES satellites and waves by the Van Allen
660 Probes, *Geophys. Res. Lett.*, *40*(17), doi:10.1002/grl.50920.
- 661 Li, W., B. Ni, R. M. Thorne, J. Bortnik, Y. Nishimura, J. C. Green, C. A. Kletzing,
662 W. S. Kurth, G. B. Hospodarsky, H. E. Spence, G. D. Reeves, J. B. Blake, J.
663 F. Fennell, S. G. Claudepierre and X. Gu (2014), Quantifying hiss-driven energetic
664 electron precipitation: A detailed conjunction event analysis, *Geophys. Res. Lett.*, *41*(4),

doi:10.1002/2013GL059132.

- Lichtenberger, L., M. A. Clilverd, B. Heilig, M. Vellante, J. Manninen, C. J. Rodger, A. B. Collier, A. M. Jørgensen, J. Reda, R. H. Holzworth, R. Friedel and M. Simon-Wedlund (2013), The plasmasphere during a space weather event: first results from the PLASMON project, *J. Space Weather Space Clim*, 3(A23), doi:10.1051/swsc/2013045.
- Loewe, C. A., and G. W. Prölss (1997), Classification and mean behavior of magnetic storms, *J. Geophys. Res.*, 102(A7), doi:10.1029/96JA04020.
- Lyons, L. R., and R. M. Thorne (1973), Equilibrium structure of radiation belt electrons, *J. Geophys. Res.*, 78(13), doi:10.1029/JA078i013p02142
- Meredith, N. P., R. B. Horne, D. Summers, R. M. Thorne, R. H. Iles, D. Heynderickx and R. R. Anderson (2002), Evidence for acceleration of outer zone electrons to relativistic energies by whistler mode chorus, *Annales Geophysicae*, 20, doi:10.5194/angeo-20-967-2002.
- Meredith, N. P., R. B. Horne, S. A. Glauert, R. M. Thorne, D. Summers, J. M. Albert, and R. R. Anderson (2006), Energetic outer zone electron loss timescales during low geomagnetic activity, *J. Geophys. Res.*, 111, A05212, doi:10.1029/2005JA011516.
- Meredith, N. P., R. B. Horne, M. M. Lam, M. H. Denton, J. E. Borovsky and J. C. Green (2011), Energetic electron precipitation during high-speed solar wind stream driven storms, *J. Geophys. Res.*, 116, A05223, doi:10.1029/2010JA016293.
- Millan, R. M, K. B. Yando, J. C. Green, and A. Y. Ukhorskiy (2010), Spatial distribution of relativistic electron precipitation during a radiation belt depletion event., *Geophys. Res. Lett.*, 37(L20103), doi:10.1029/2010GL044919.

- 687 Newnham, D. A., P. J. Espy, M. A. Clilverd, C. J. Rodger, A. Seppälä, D. J. Maxfield,
688 P. Hartogh, K. Holmén, and R. B. Horne (2011), Direct observations of nitric oxide
689 produced by energetic electron precipitation in the antarctic middle atmosphere,
690 *Geophys. Res. Lett.*, *38*(20), L20,104, doi:10.1029/2011GL049199.
- 691 O'Brien, T. P., and M. B. Moldwin (2003), Empirical plasmopause models from magnetic
692 indices, *Geophys. Res. Lett.*, *30*, 1152, doi:10.1029/2002GL016007.
- 693 Rodger, C. J., M. A. Clilverd, N. R. Thomson, R. J. Gamble, A. Seppälä, E. Turunen, N.
694 P. Meredith, M. Parrot, J-A. Sauvaud and J-J Berthelier (2010), Radiation belt electron
695 precipitation into the atmosphere: recovery from a geomagnetic storm, *J. Geophys. Res.*,
696 *112*, A11307, doi:10.1029/2007JA012383.
- 697 Rodger, C. J., M. A. Clilverd, A. Seppälä, N. R. Thomson, R. J. Gamble, M. Parrot, J-A.
698 Sauvaud and T. Ulich (2010), Radiation belt electron precipitation due to geomagnetic
699 storms: significance to middle atmosphere ozone chemistry, *J. Geophys. Res.*, *115*,
700 A11320, doi:10.1029/2010JA015599.
- 701 Rodger, C. J., M. A. Clilverd, J. Green, and M. Lam (2010), Use of POES SEM2
702 observations to examine radiation belt dynamics and energetic electron precipitation
703 in to the atmosphere, *J. Geophys. Res.*, *115*, doi:10.1029/2008JA014023.
- 704 Seppälä, A., H. Lu, M. A. Clilverd, and C. J. Rodger (2013), Geomagnetic activity
705 signatures in wintertime stratosphere wind, temperature and wave response, *J. Geophys.*
706 *Res.*, *118*, doi:10.1002/jgrd50236.
- 707 Solomon, S., P. J. Crutzen, and R. G. Roble (1982), Photochemical coupling between
708 the thermosphere and the lower atmosphere: 1. Odd nitrogen from 50 to 120 km, *J.*
709 *Geophys. Res.*, *87*, doi:10.1029/JC087iC09p07206.

- 710 Sugiura, M. (1964), Hourly values of the equatorial Dst for IGY, *Annals of the*
711 *International Geophysical Year*, 35(pp945-948), Pergamon Press.
- 712 Summers, D., R. M. Thorne, and F. Xiao (1998), Relativistic theory of wave-particle
713 resonant diffusion with application to electron acceleration in the magnetosphere, *J.*
714 *Geophys. Res.*, 103, A9, doi:10.1029/98JA01740.
- 715 Summers, D., B. Ni, and N. P. Meredith (2007), Timescales for radiation belt electron
716 acceleration and loss due to resonant wave-particle interactions: 2. Evaluation for VLF
717 chorus, ELF hiss, and electromagnetic ion cyclotron waves, *J. Geophys. Res.*, 113,
718 A04219, doi:10.1029/2007JA012678.
- 719 Summers, D., B. Ni, N. P. Meredith, R. B. Horne, R. M. Thorne, M. B. Moldwin and R.
720 R. Anderson (2008), Electron scattering by whistler-mode ELF hiss in plasmaspheric
721 plumes, *J. Geophys. Res.*, 112, A04207, doi:10.1029/2006JA011993.
- 722 Thorne, R. M. (1977), Energetic radiation belt electron precipitation: a natural depletion
723 mechanism for stratospheric ozone, *Science*, 195(4275):287-9.
- 724 Thorne, R. M. (1980), The importance of energetic particle precipitation on the chemical
725 composition of the middle atmosphere, *Pure and Appl. Geophys.*, 118(1).
- 726 Thorne, R. M. (2010), Radiation belt dynamics: The importance of wave-particle
727 interactions, *Geophys. Res. Lett.*, 37(22), doi:10.1029/2010GL044990.
- 728 Thorne, R. M., W. Li, B. Ni, Q. Ma, J. Bortnik, D. N. Baker, H. E. Spence, G. D. Reeves,
729 M. G. Henderson, C. A. Kletzing, W. S. Kurth, G. B. Hospodarsky, D. Turner and V.
730 Angelopoulos (2013), Evolution and slow decay of an unusual narrow ring of relativistic
731 electrons near L \sim 3.2 following the September 2012 magnetic storm, *Geophys. Res. Lett.*,
732 40(14), doi:10.1002/grl.50627.

733 Thorne, R. M., W. Li, B. Ni, Q. Ma, J. Bortnik, D. N. Baker, H. E. Spence, G. D. Reeves,
734 M. G. Henderson, C. A. Kletzing, W. S. Kurth, G. B. Hospodarsky, J. B. Blake, J.
735 F. Fennell, S. G. Claudepierre and S. G. Kanekal (2013), Van Allen probe evidence of
736 relativistic radiation belt electron acceleration by magnetospheric chorus, *Nature*, *504*,
737 doi:10.1038/nature12889.

738 Turner, D. L., Y. Shprits, M. Hartinger, and V. Angelopoulos (2013), Explaining sudden
739 losses of outer radiation belt electrons during geomagnetic storms, *Nature Phys.*, *8*,
740 doi:10.1038/nphys2185.

741 Turunen, E., P. T. Verronen, A. Seppälä, C. J. Rodger, M. A. Clilverd, J. Tamminen,
742 C. F. Enell, and T. Ulich (2009), Impact of different energies of precipitating particles
743 on nox generation in the middle and upper atmosphere during geomagnetic storms, *J.*
744 *Atmos. Sol. Terr. Phys.*, *71*, 1176–1189, doi:10.1029/2002GL016513.

745 Verronen, P. T., C. J. Rodger, M. A. Clilverd, and S. Wang (2011), First evidence of
746 mesospheric hydroxyl response to electron precipitation from the radiation belts, *J.*
747 *Geophys. Res.*, *116*(D07307), doi:10.1029/2010JD014965.

748 Verronen, P. T., M. Andersson, C. J. Rodger, M. A. Clilverd, S. Wang and
749 E. Turunen (2013), omparison of modeled and observed effects of radiation belt
750 electron precipitation on mesospheric hydroxyl and ozone, *J. Geophys. Res.*, *118*,
751 doi:10.1002/jgrd.50845.

752 Simon Wedlund, M., M. A. Clilverd, C. J. Rodger, K. Cresswell-Moorcock, N. Cobbett,
753 P. Breen, D. Danskin, E. Spanswick, and J. V. Rodriguez (2014), A statistical approach
754 to determining energetic outer radiation belt electron precipitation fluxes, *J. Geophys.*
755 *Res.*, *119*, doi:10.1002/2013JA019715

- 756 Whittaker, I. C., R. J. Gamble, C. J. Rodger, M. A. Clilverd and J.-A. Sauvaud (2013),
757 Determining the spectra of radiation belt electron losses: Fitting DEMETER IDP
758 observations for typical and storm-times, *J. Geophys. Res.*, doi:10.1002/2013JA019228
- 759 Whittaker, I. C., C. J. Rodger, M. A. Clilverd and J.-A. Sauvaud (2014), The effects and
760 correction of the geometric factor for the POES/MEPED electron flux instrument using
761 a multi-satellite comparison, *J. Geophys. Res.*, under review.
- 762 Yando, K., R. M. Millan, J. C. Green, and D. S. Evans (2011), A Monte Carlo simulation
763 of the NOAA POES Medium Energy Proton and Electron Detector instrument, *J.*
764 *Geophys. Res.*, 118, doi:10.1002/jgra.50584

Figure 1: *A schematic of the of the wave activity in the radiation belts and plasmasphere adapted from Summers, Ni and Meredith [2007, Figure 21]. The angle from the vertical shows the magnetic local time while the radial distance gives the L shell value. The grey shaded area shows the morning MLT sector that we use in this study to determine the chorus affected zone outside the plasmopause, ranging from 01:00 to 08:00. The purple shaded area shows the afternoon MLT sector which we investigate to determine the plasmaspsheric hiss induced fluxes inside the plasmopause, with an MLT range of 11:00 to 16:00.*

Figure 2: a) *The median Dst values associated with the 103 geomagnetic storms identified for our superposed epoch analysis, after SPE removal.* b) *The >300 keV morning MLT epoch plot using a \log_{10} colour scale, showing peak precipitation from chorus ($t = 0$) and hiss ($t = 3$ to 7 days). The solid line represents the non-MLT dependent plasmopause location and the dashed line shows a $+0.5$ L offset which separates the chorus and hiss induced precipitating flux.* c) *The >300 keV afternoon MLT epoch on the same scale and format as panel b). The dashed line represents a $+0.75$ L offset from the O'Brien and Moldwin model.*

Figure 3: *The electron flux variation shown during our superposed epoch analysis for the morning MLT sector 01:00 to 08:00. All precipitating flux panels are shown with units of $\text{cm}^{-2}\text{sr}^{-1}\text{s}^{-1}$. The top left panel shows the median >30 keV electron flux, the top right panel shows the >100 keV electron flux and the lower left panel shows the >300 keV electron flux, all are shown on a \log_{10} color scale. The lower right panel shows the spectral index from a power law fitting of the three energy ranges. The modeled plasmopause location from Figure 2 has been included on all panels as the dashed black line (O'Brien and Moldwin non MLT-dependent Dst model + 0.5 L).*

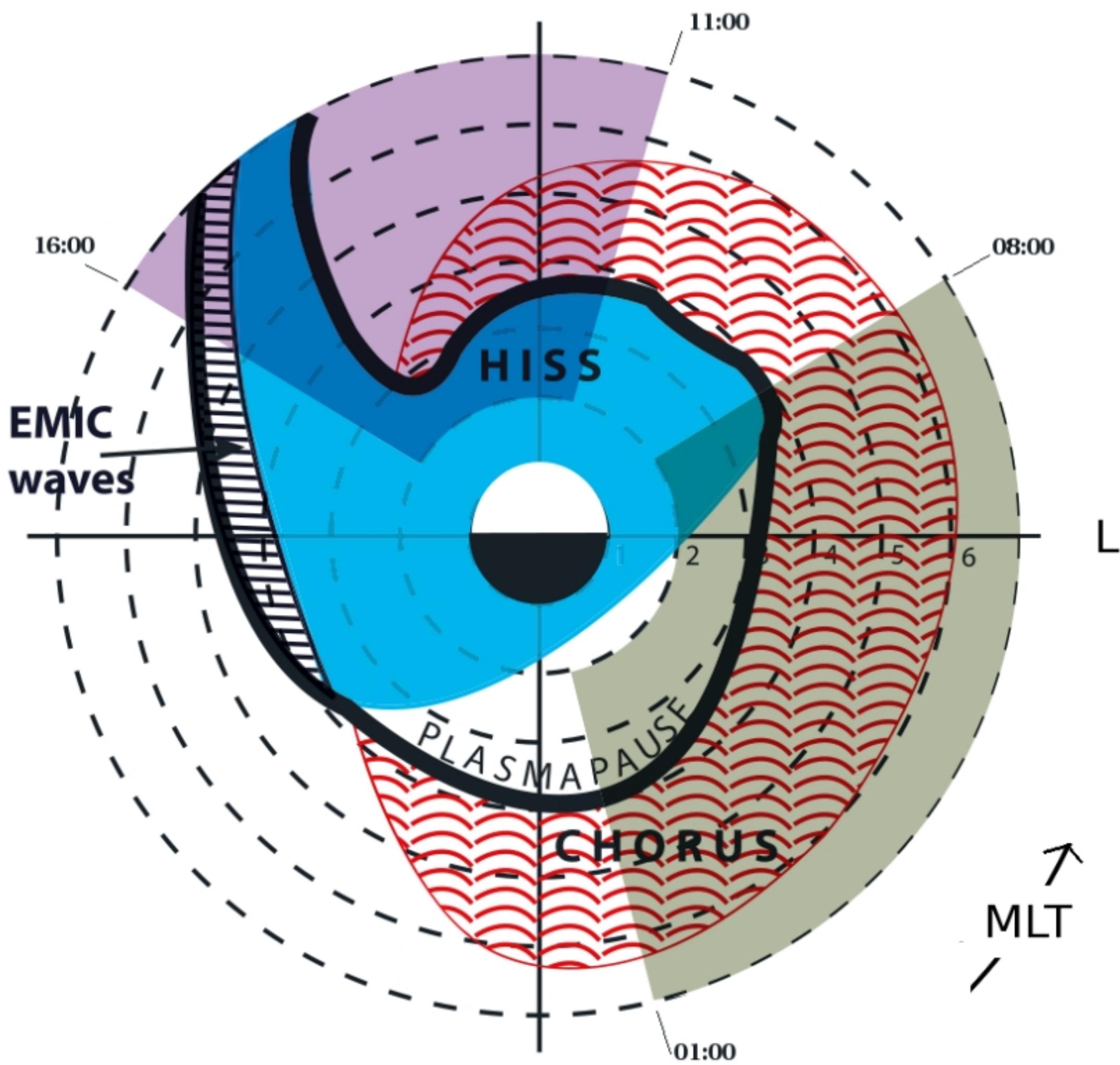
Figure 4: (Left) the >30 keV precipitating electron flux at different distances from the plasmopause (L_{pp}) are plotted, ranging from the plasmopause (top left panel) to 3 L outside the plasmopause (lower left panel). The dark blue solid line shows the observed flux after superposed epoch analysis and the red dashed line shows the model flux from Equation (3). (Right) The spectral index from the power law fit of the three MEPED electron energy channels at the same distances from the plasmopause as the left panels. The blue solid line shows the spectral index observed and the red dashed line shows the simulation from Equation (4).

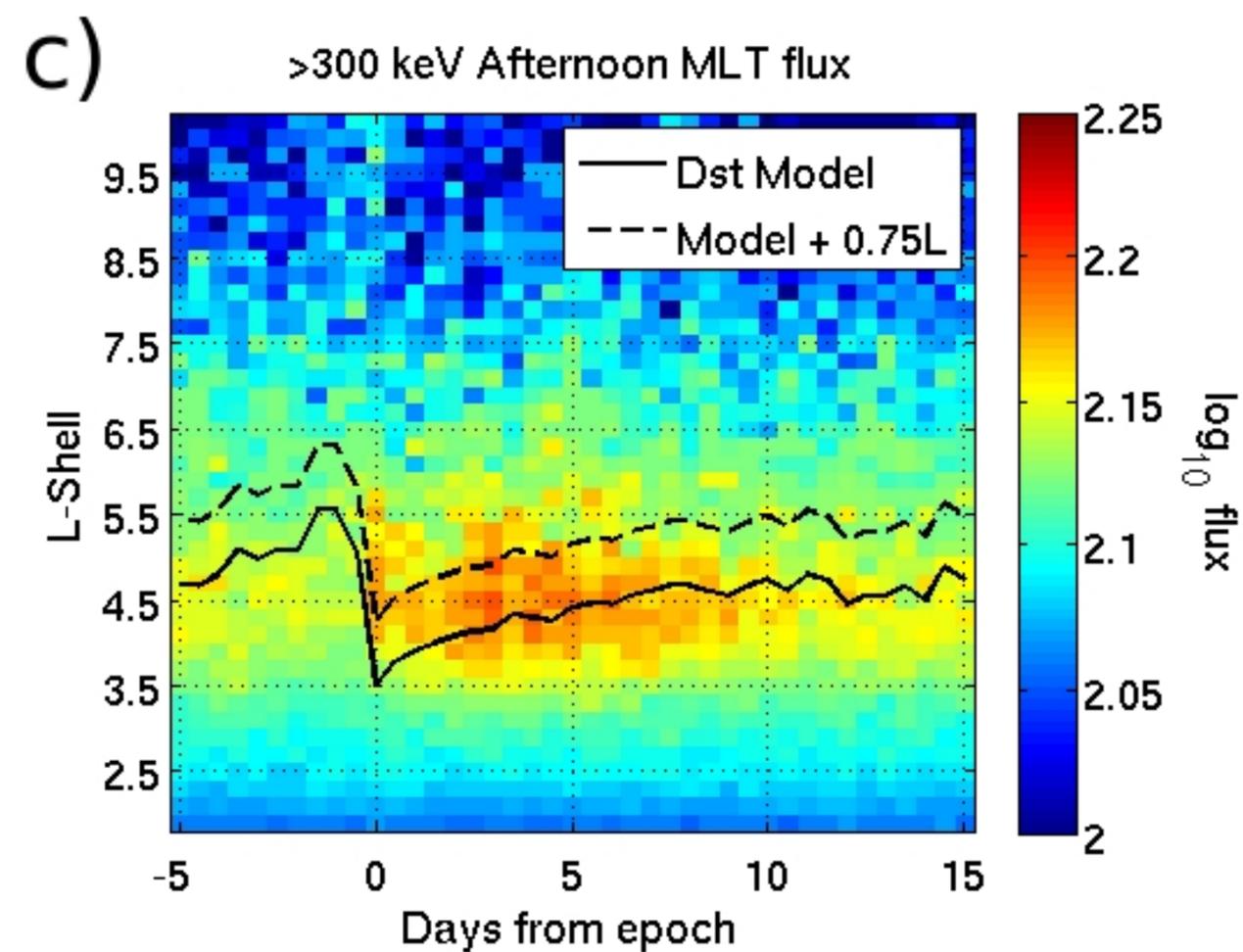
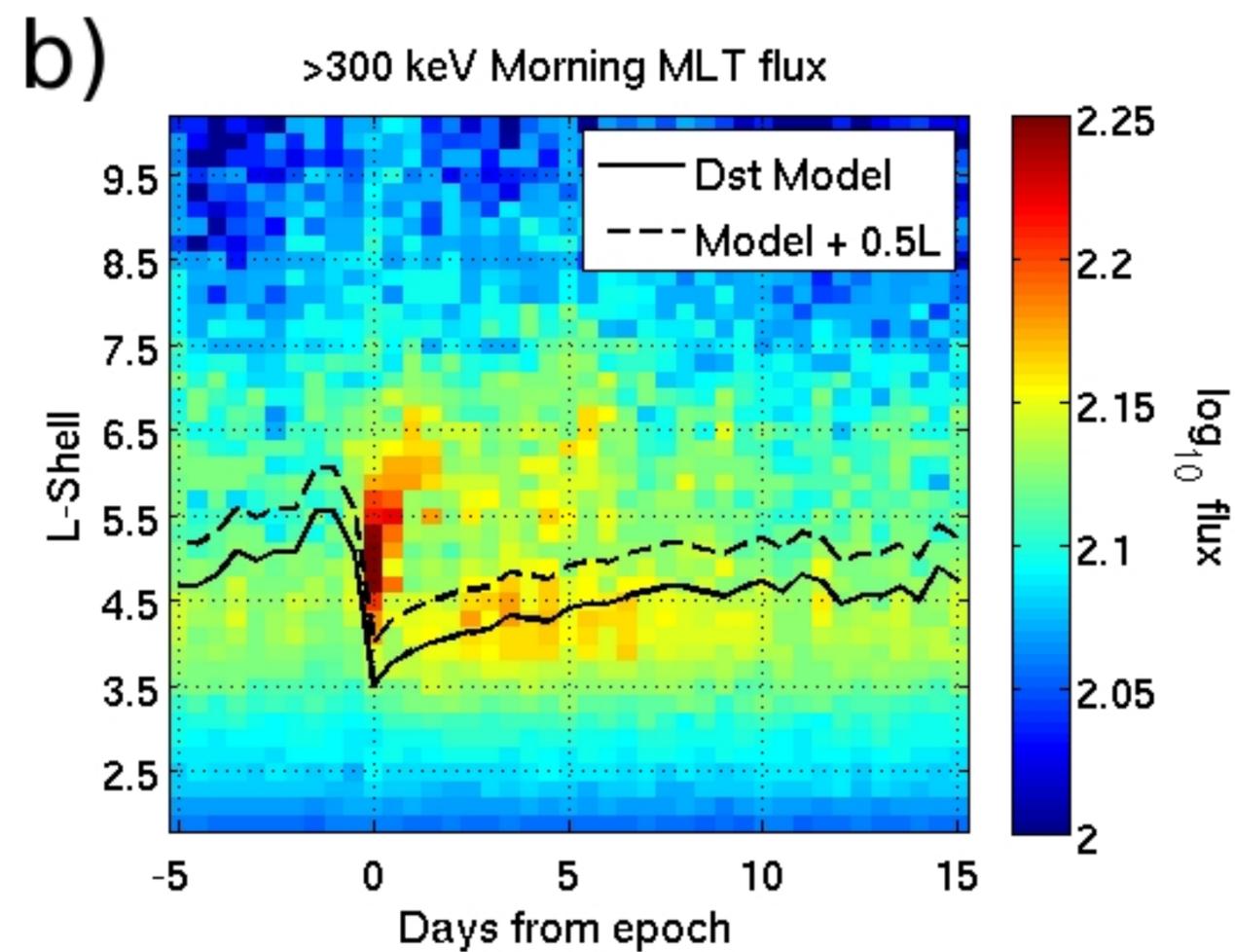
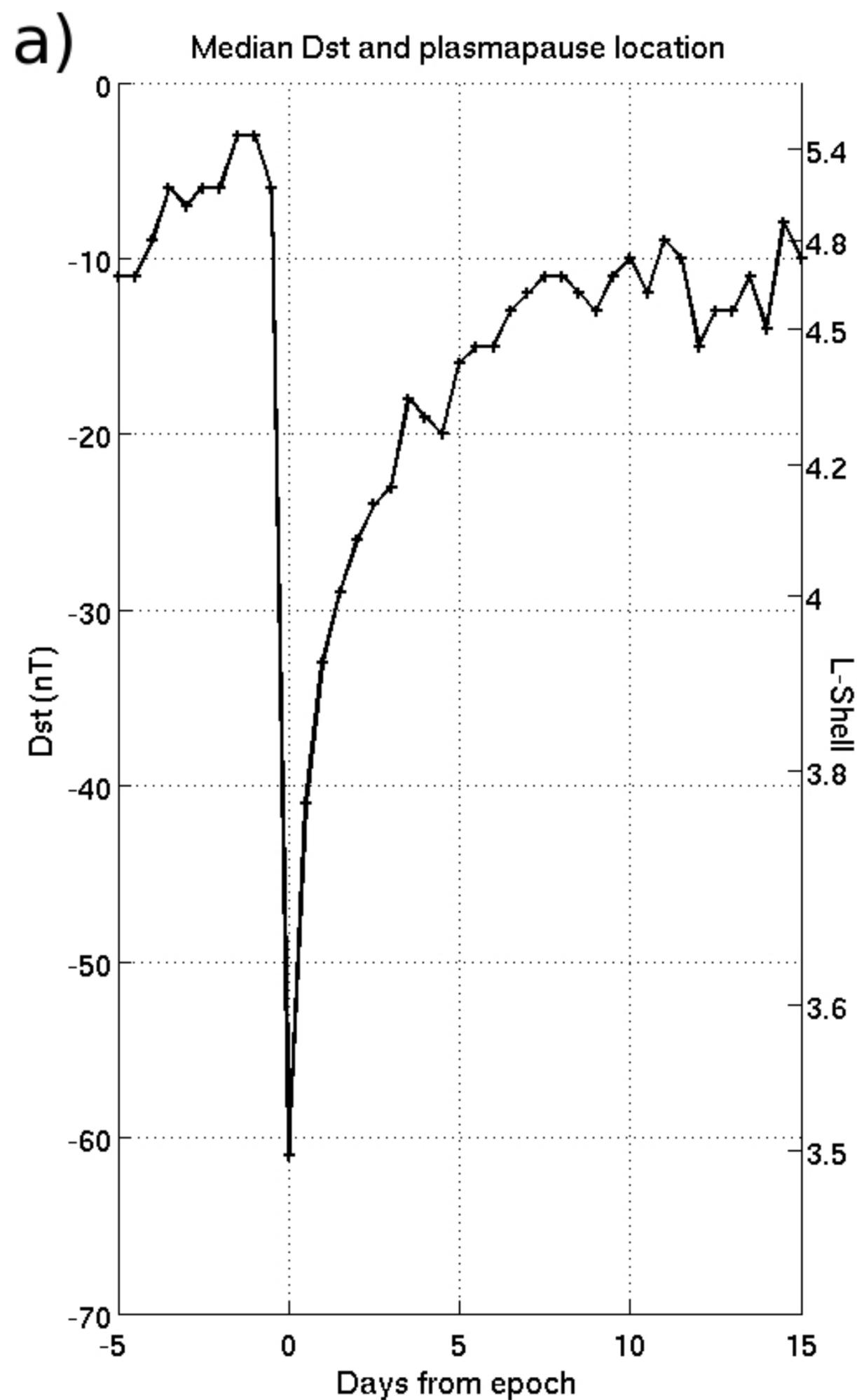
Figure 5: *Simulations of the superposed epoch analysis using Equations (3) and (4). The left panels show the >30 keV flux and the right panels show the spectral index. The top row contains the observed data, the middle row shows the simulation from Equation (3) and (4) respectively and the lower panels show the same simulation with a minimum flux (lower left, Equation (5)) and maximum spectral index (lower right) filter applied. The black dashed line shows the morning MLT plasmopause position.*

Figure 6: *The electron flux epochs for the afternoon MLT sector (11:00 to 16:00). The top left panel shows the median >30 keV electron flux, the top right panel shows the >100 keV electron flux and the lower left panel shows the >300 keV electron flux, all are shown on a \log_{10} color scale. The lower right panel shows the P6 MEPED telescope superposed epoch analysis, this telescope includes relativistic electrons with energies >800 keV. The modeled afternoon MLT plasmopause location from Figure 2 has been included on all panels as the dashed black line (O'Brien and Moldwin non MLT-dependent Dst model + 0.75 L).*

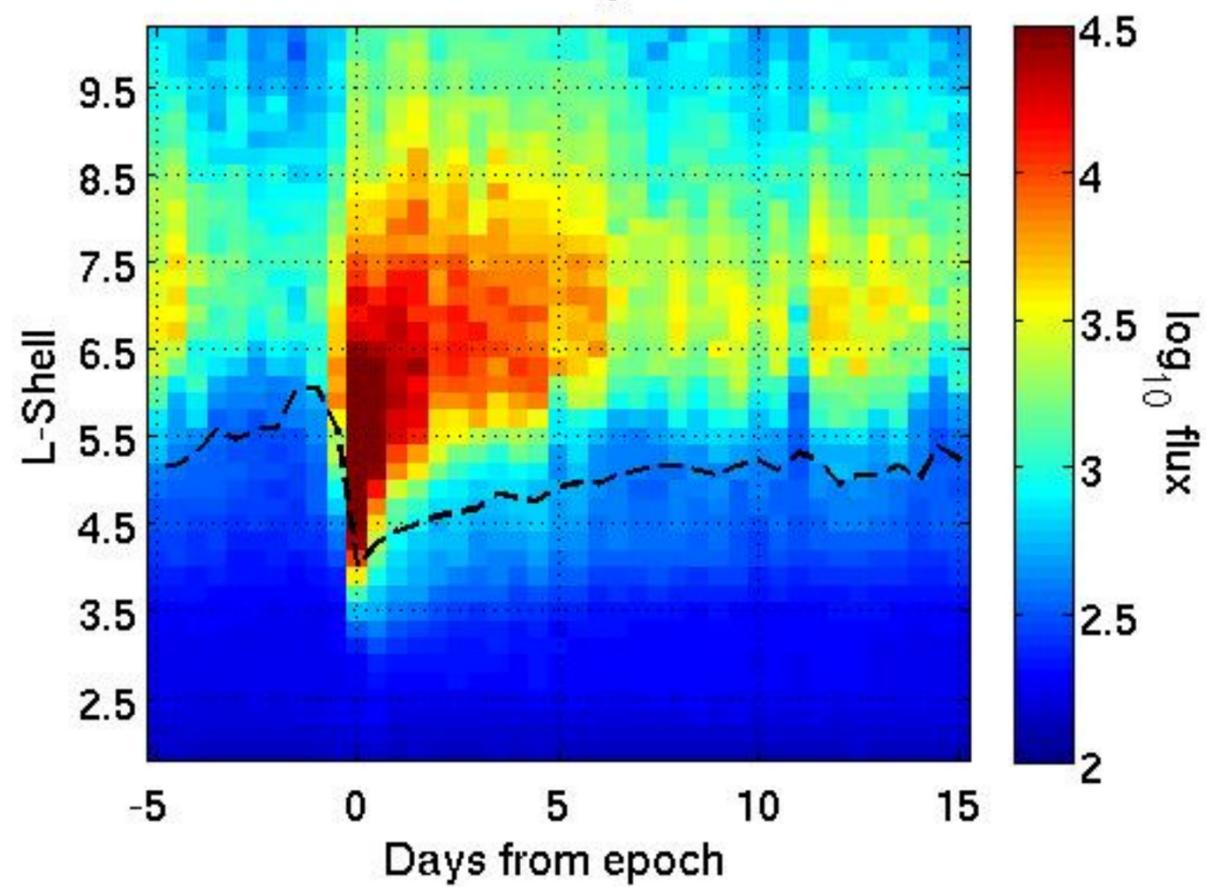
Figure 7: **a) to d)** The afternoon MLT sector (11:00-16:00) >300 keV electron flux observations at L shells of 3.3, 3.7, 4.1 and 4.5. The solid blue line shows the instrument flux and the red dashed line shows the simulation of the flux at each L shell as calculated by Equation (6). **e)** The >300 keV storm epoch from the lower left panel of Figure 6 on a linear color scale emphasising the variation in flux inside the plasmopause by reducing the color range scale. **f)** The full simulation of the >300 keV flux inside the plasmopause created using Equation (6), on the same color scale as panel e) and using a 84 hour mean Dst . **g)** shows the P6 observations from the lower right panel of Figure 6 on a linear color scale. **h)** The P6 simulation generated from Equation (7), on the same linear color scale as panel g) working on a 96 hour mean Dst with a 1 day delay. The black dashed line in the epoch plots is the modeled plasmopause from Figure 2.

Figure 8: a) A DEMETER ICE superposed epoch analysis of lowerband chorus wave power around geomagnetic storms within the operating period of the satellite. The plasmopause model used for the POES data is also shown on this plot. b) A comparison

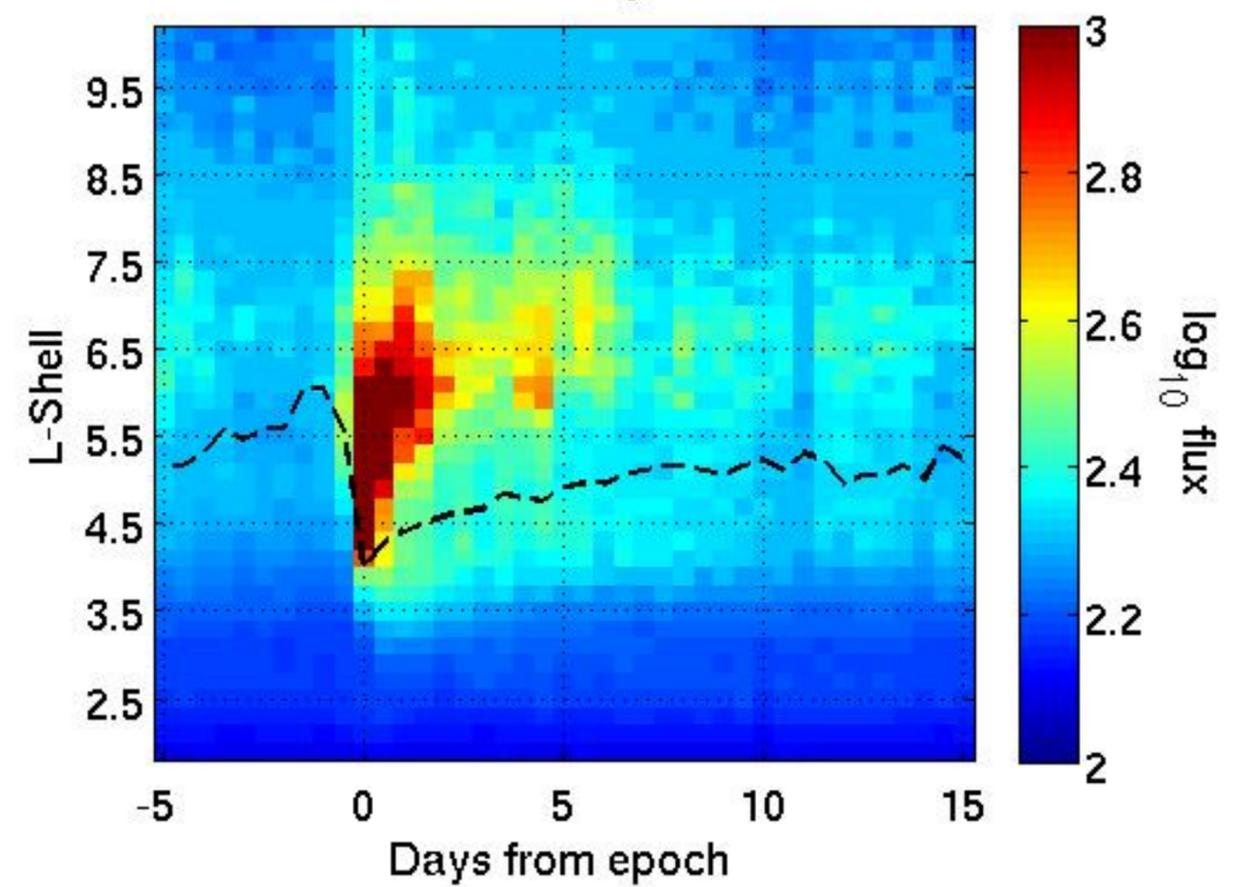




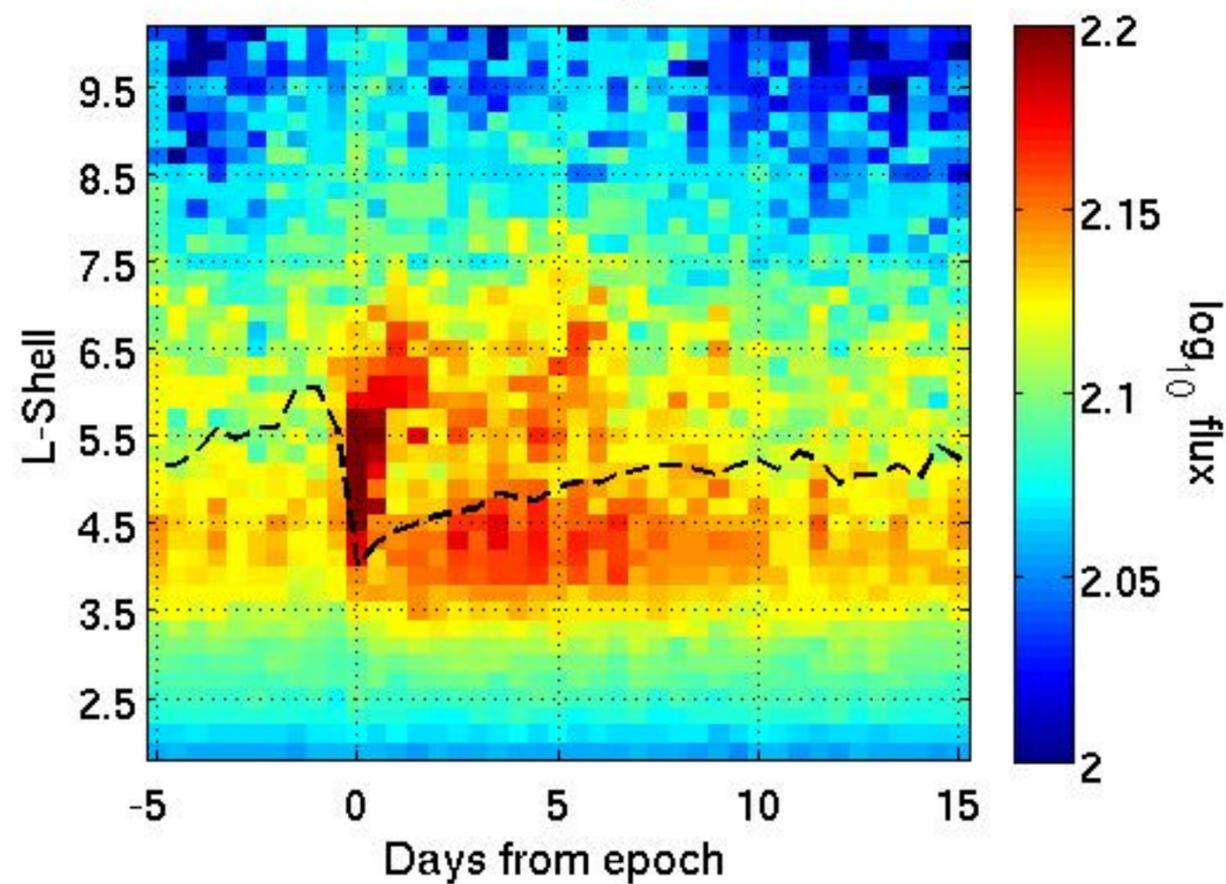
>30 keV Morning MLT flux



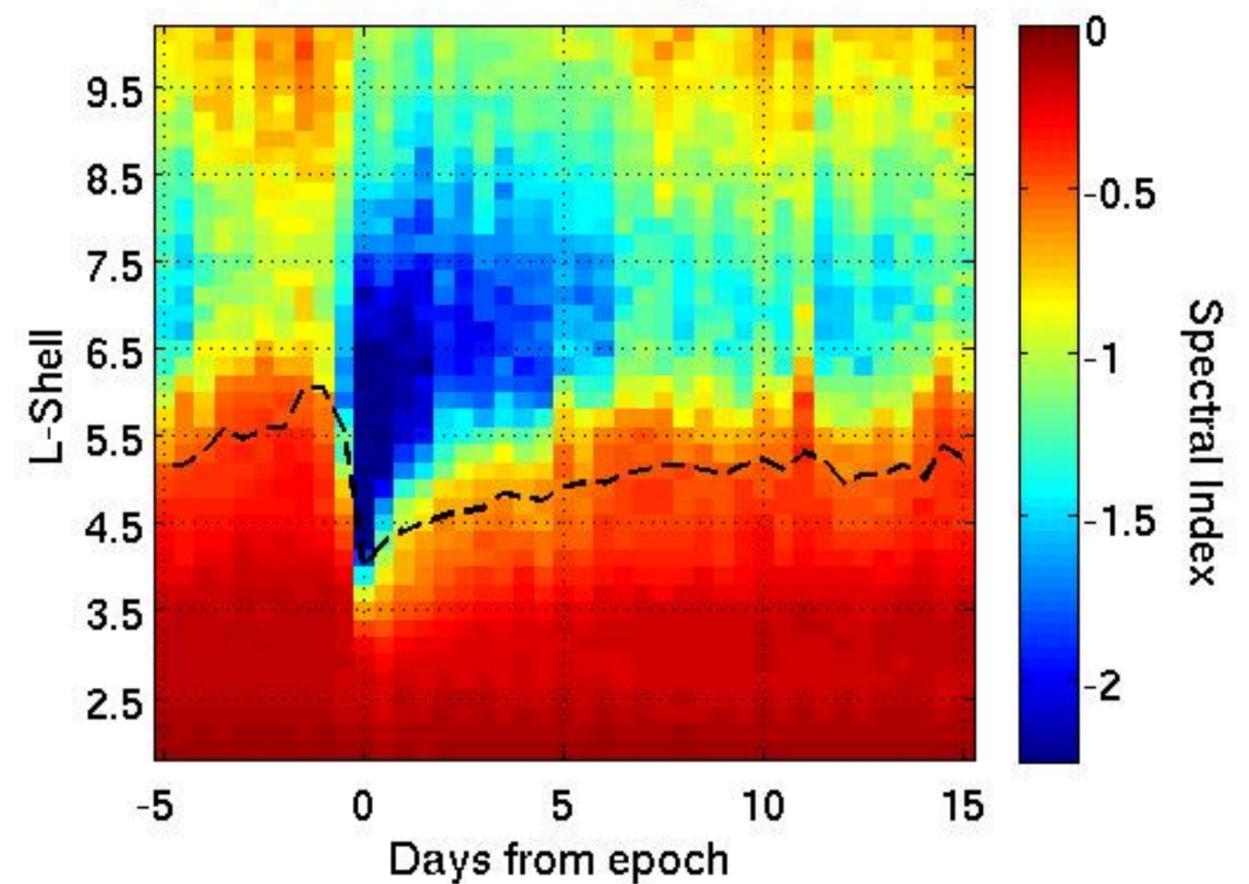
>100 keV Morning MLT flux

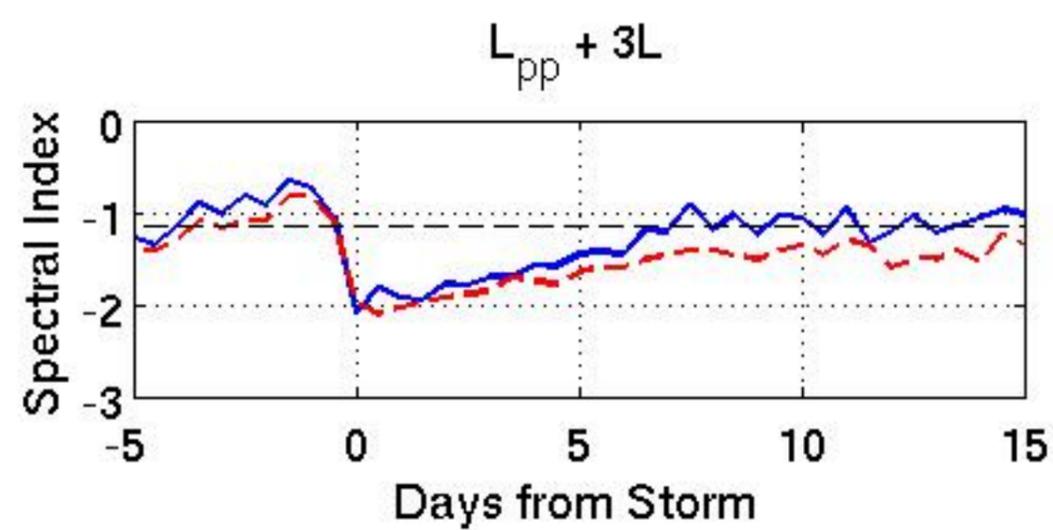
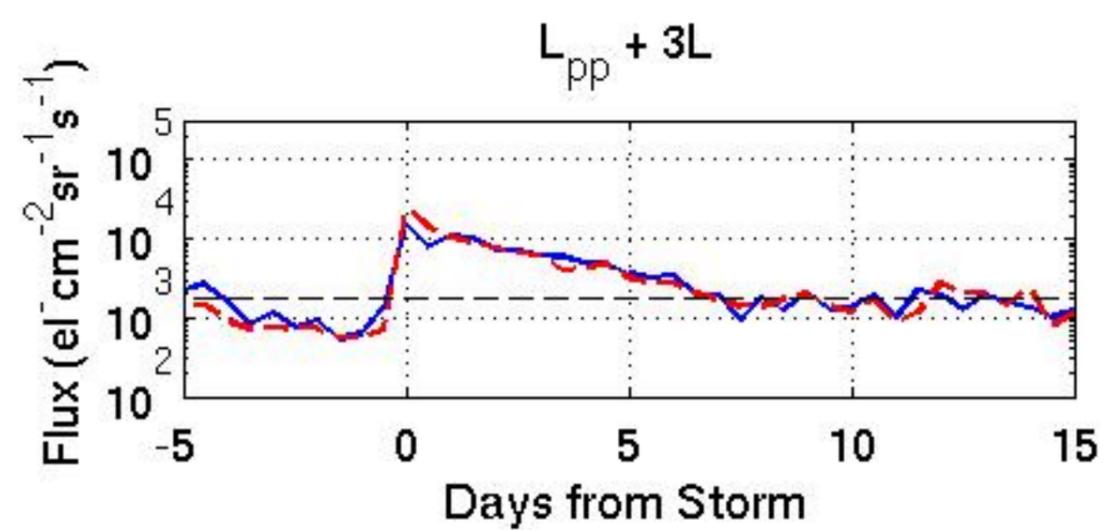
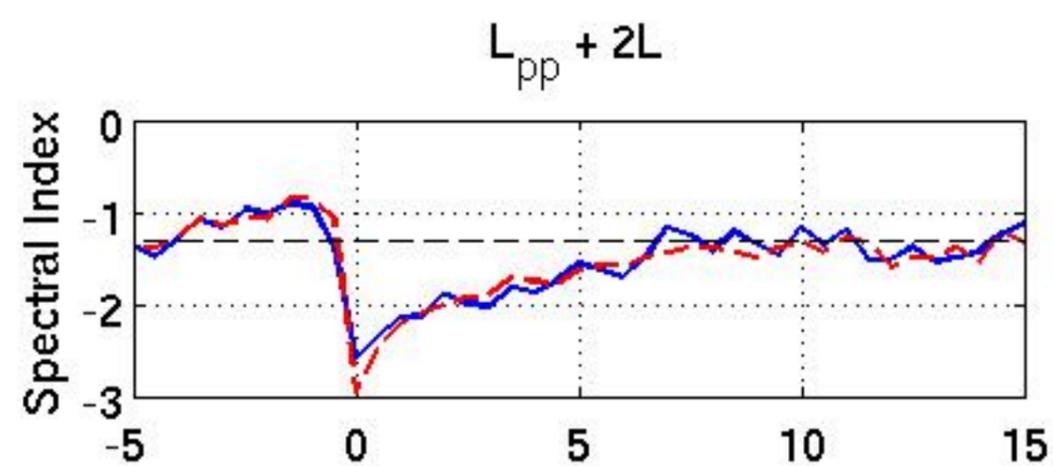
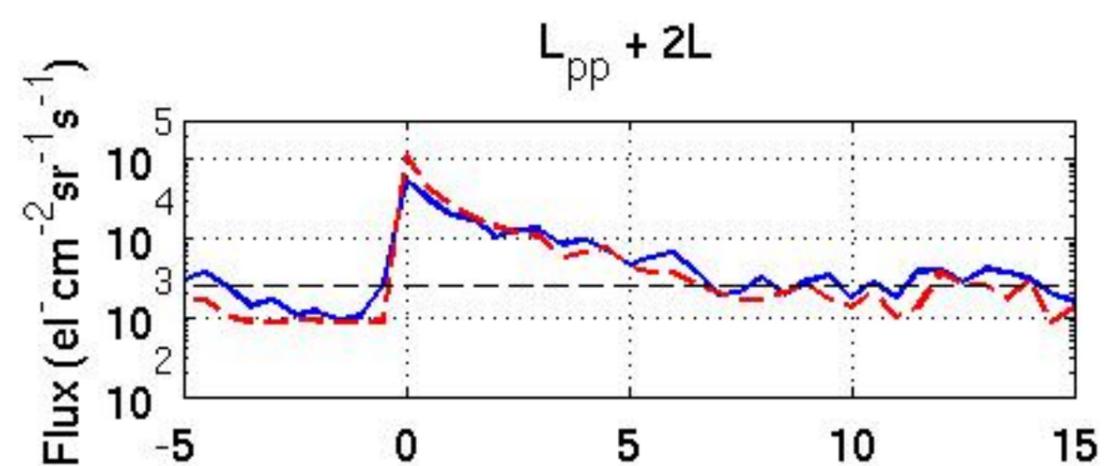
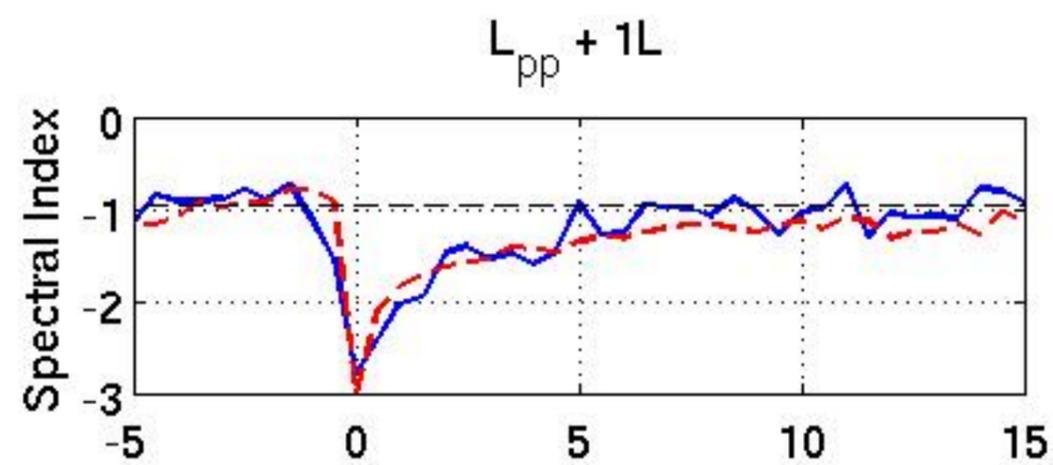
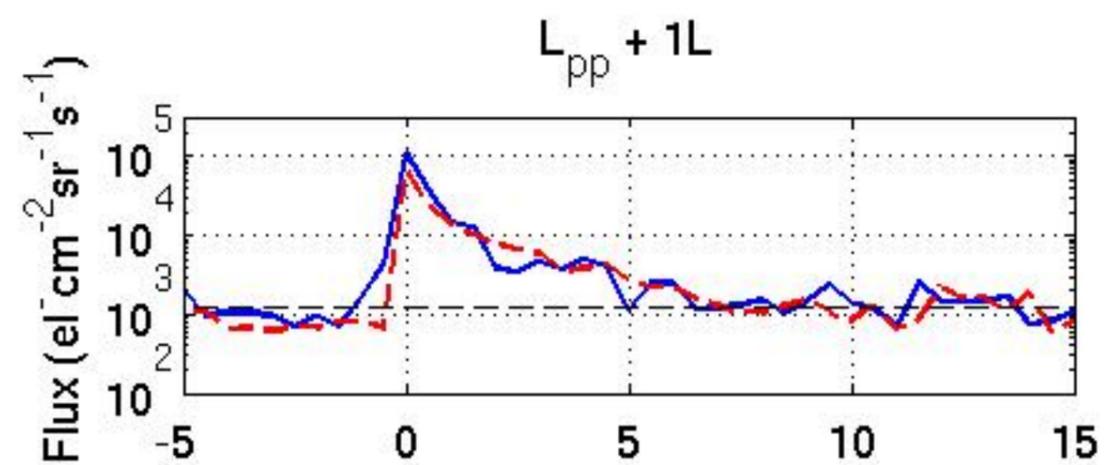
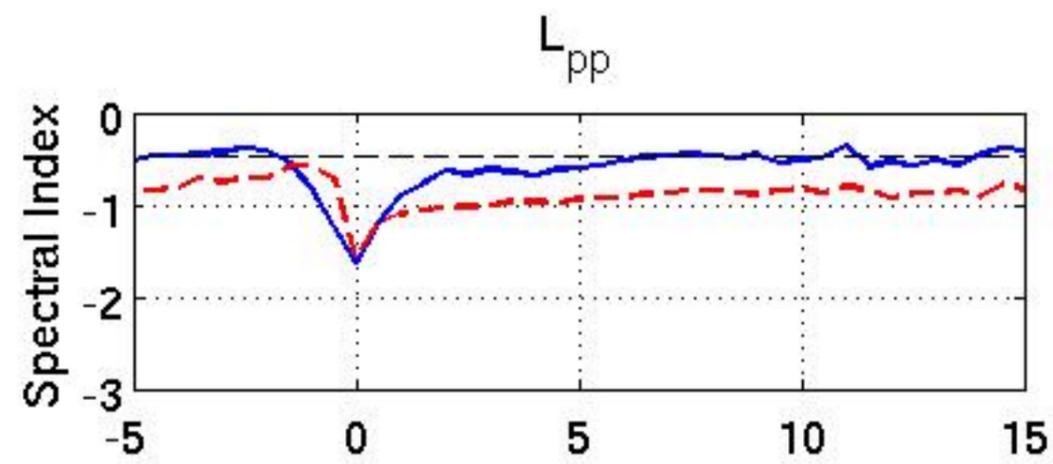
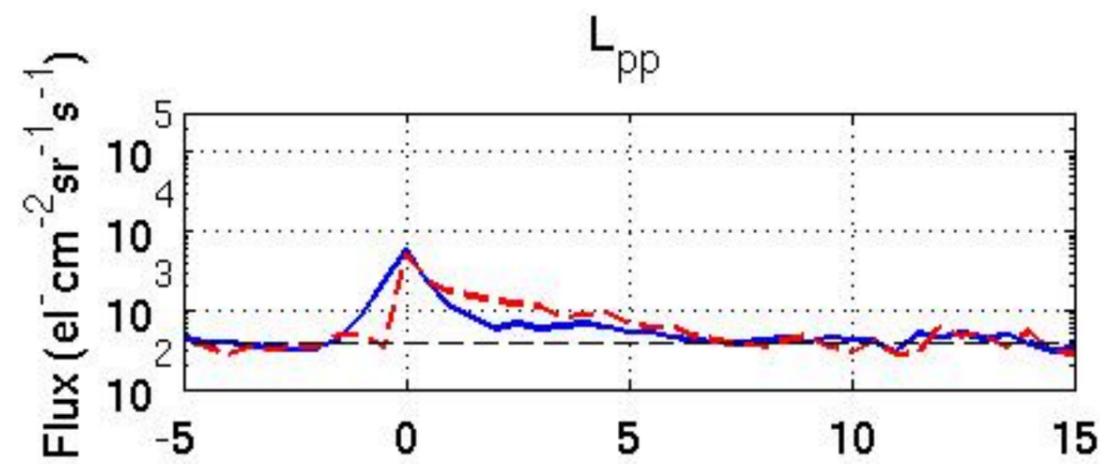


>300 keV Morning MLT flux

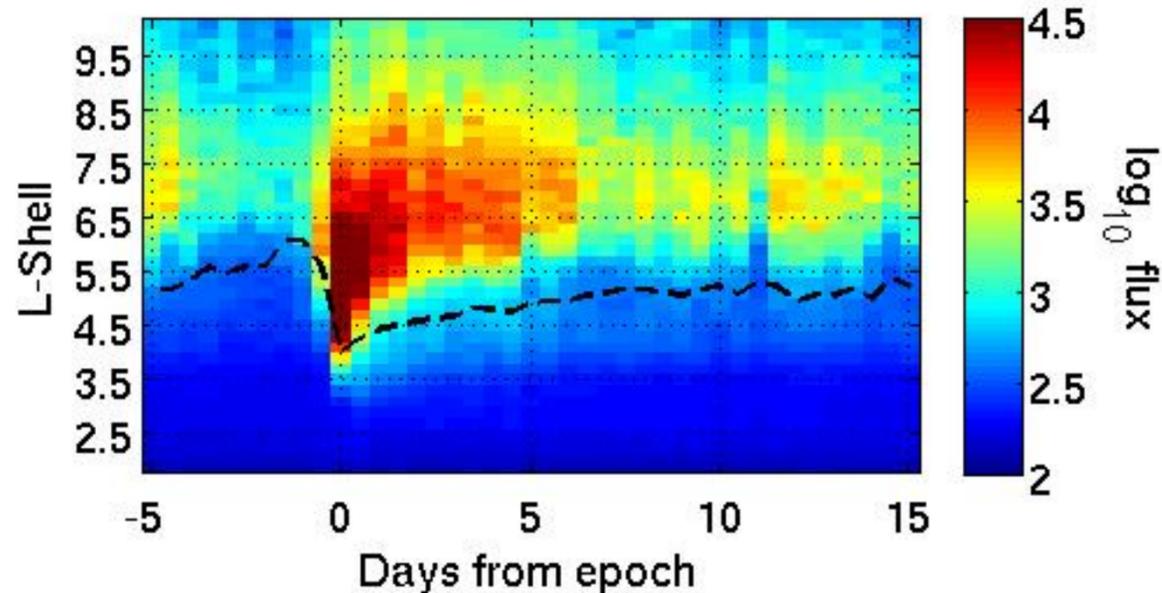


Spectral index morning MLT flux

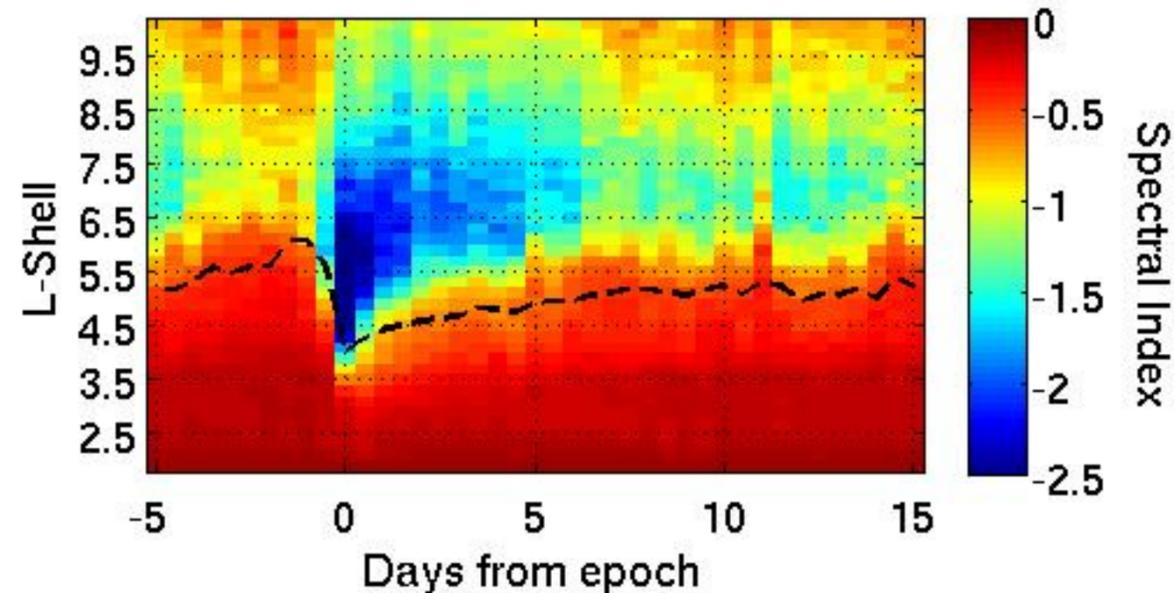




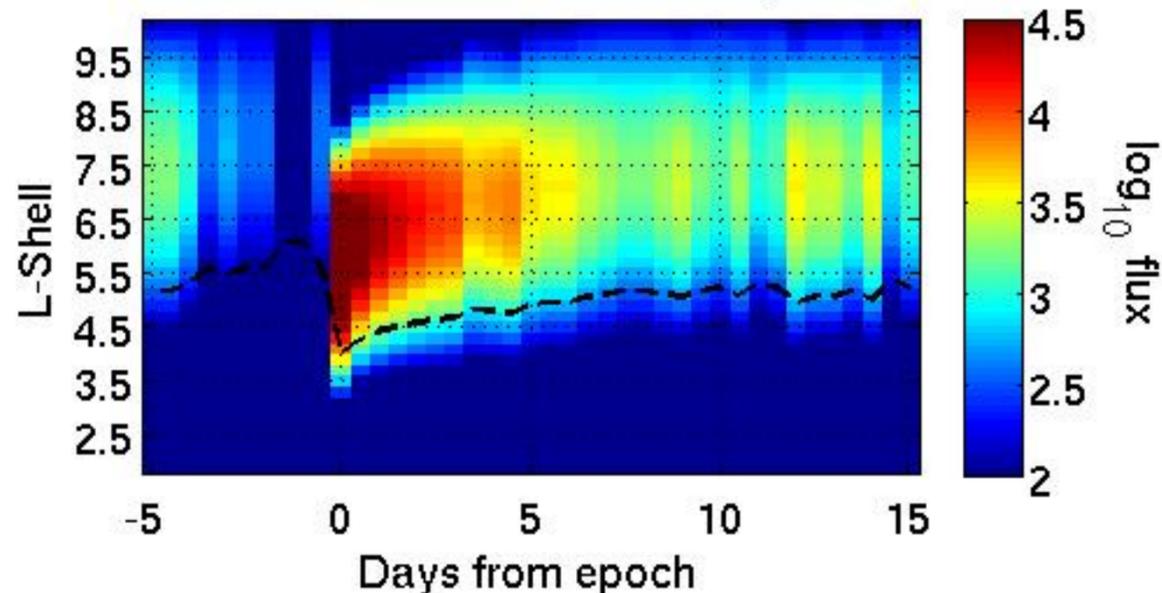
>30 keV observed flux morning MLT



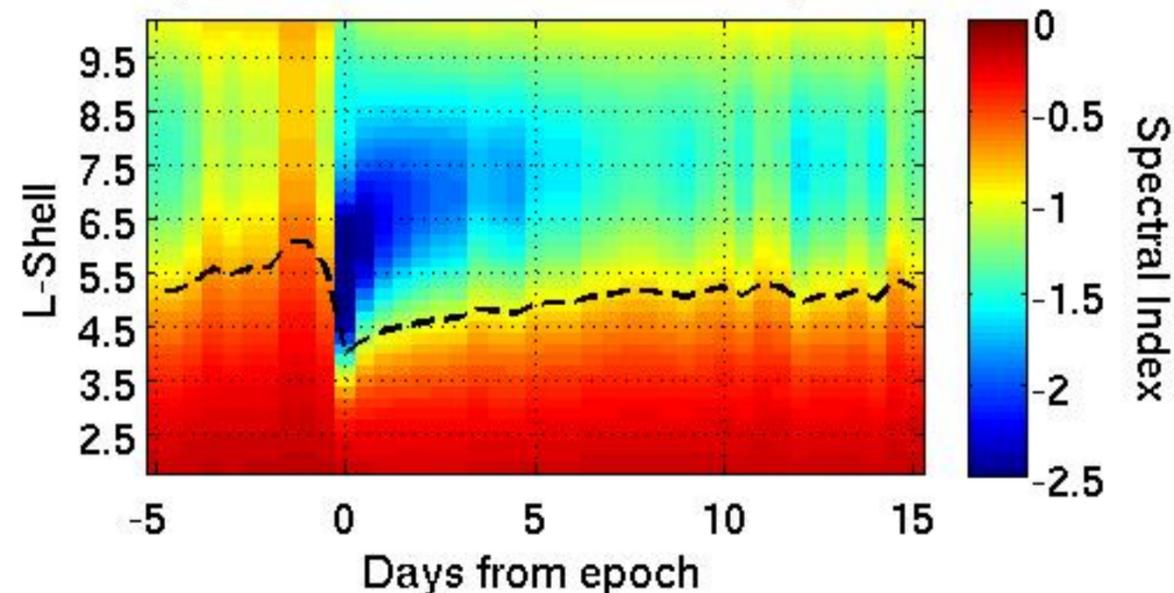
Spectral index observations morning MLT



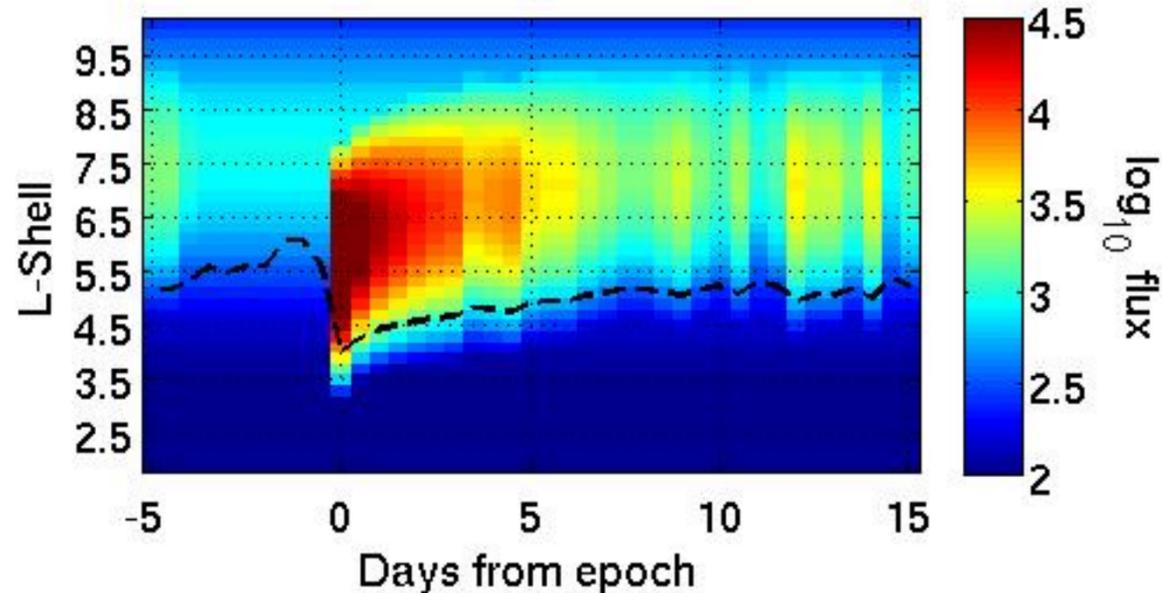
>30 keV simulated flux morning MLT



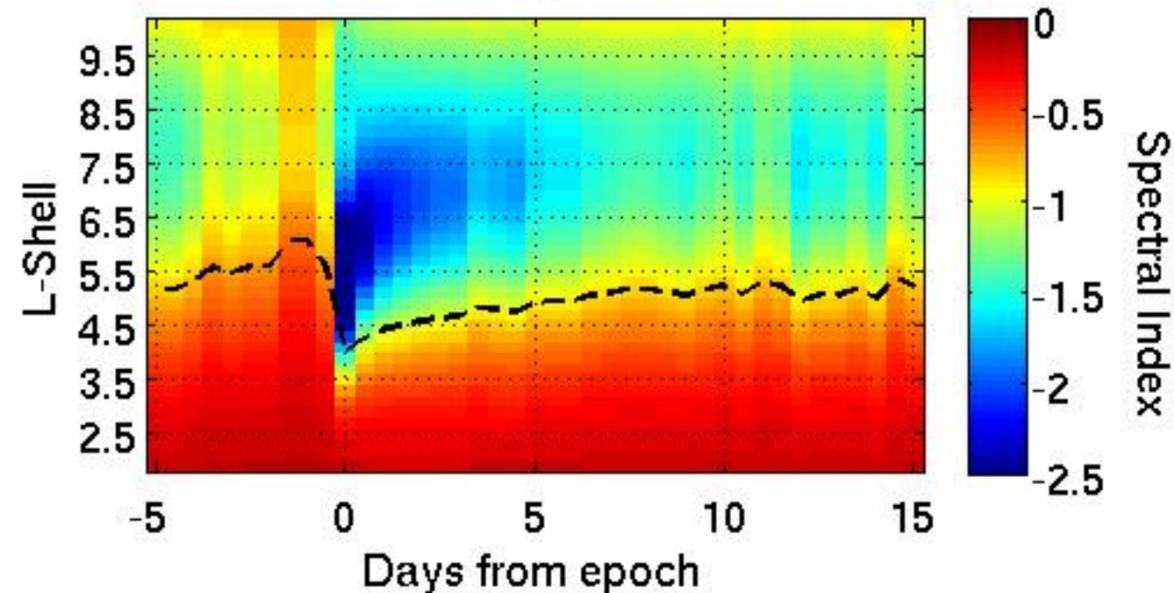
Spectral index simulation morning MLT



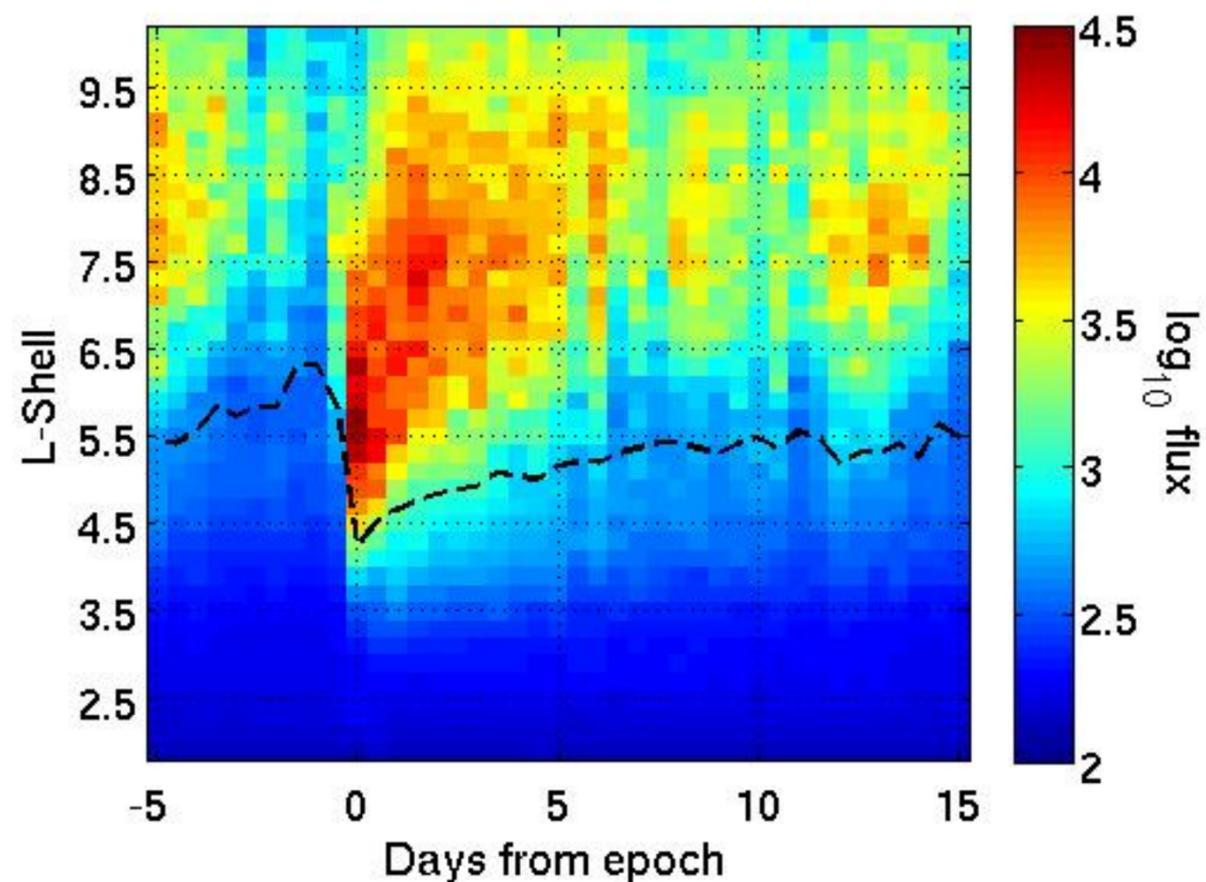
>30 keV simulated flux morning MLT with minimum flux filter



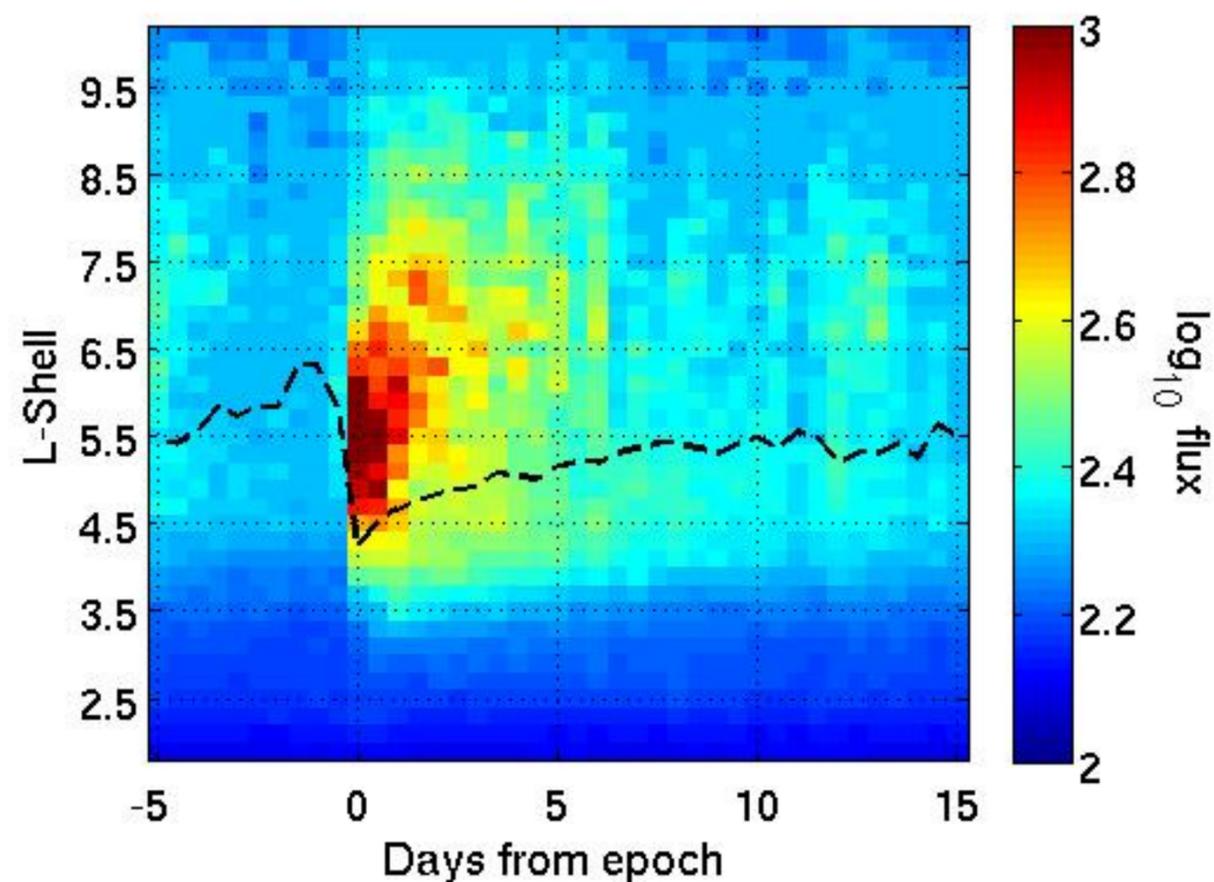
Spectral index simulation morning MLT with maximum index filter



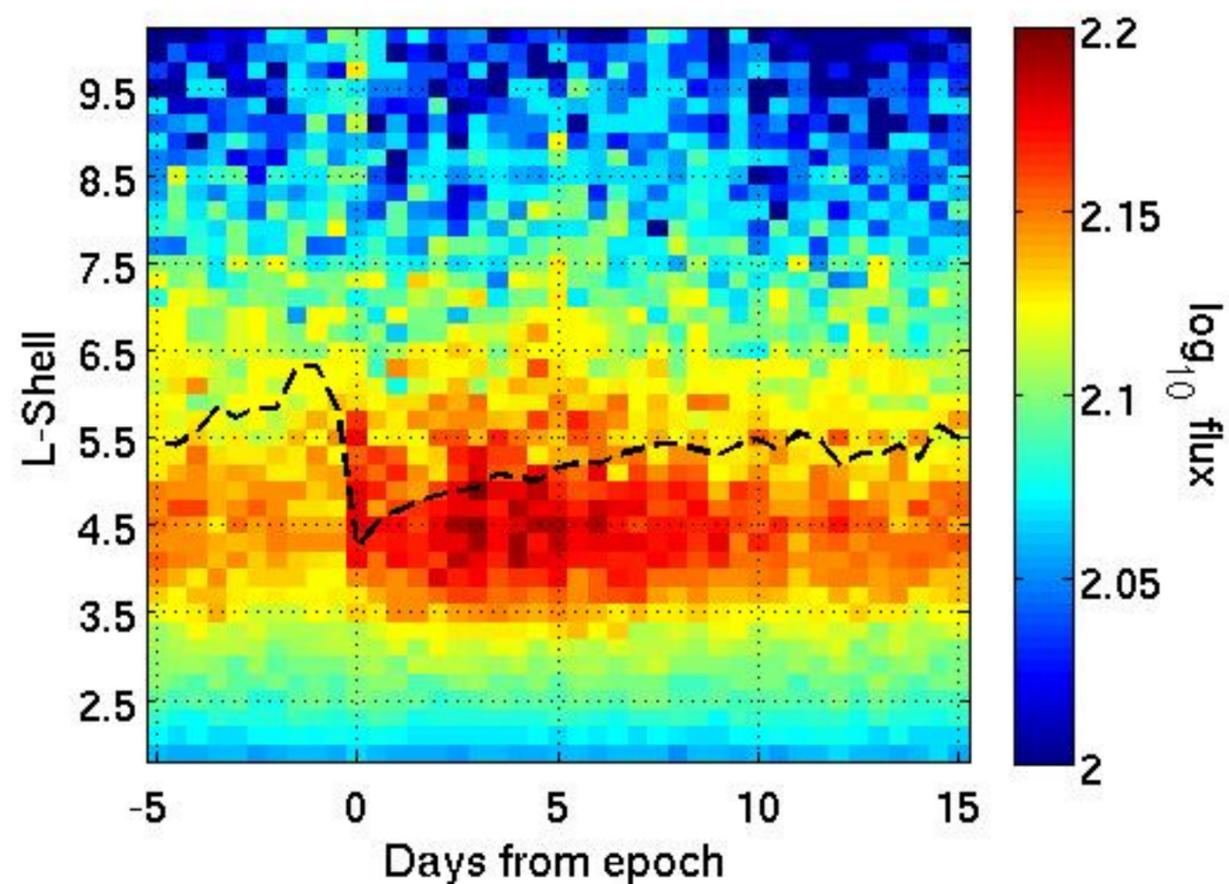
>30 keV Afternoon MLT flux



>100 keV Afternoon MLT flux



>300 keV Afternoon MLT flux



Relativistic electron afternoon MLT flux

